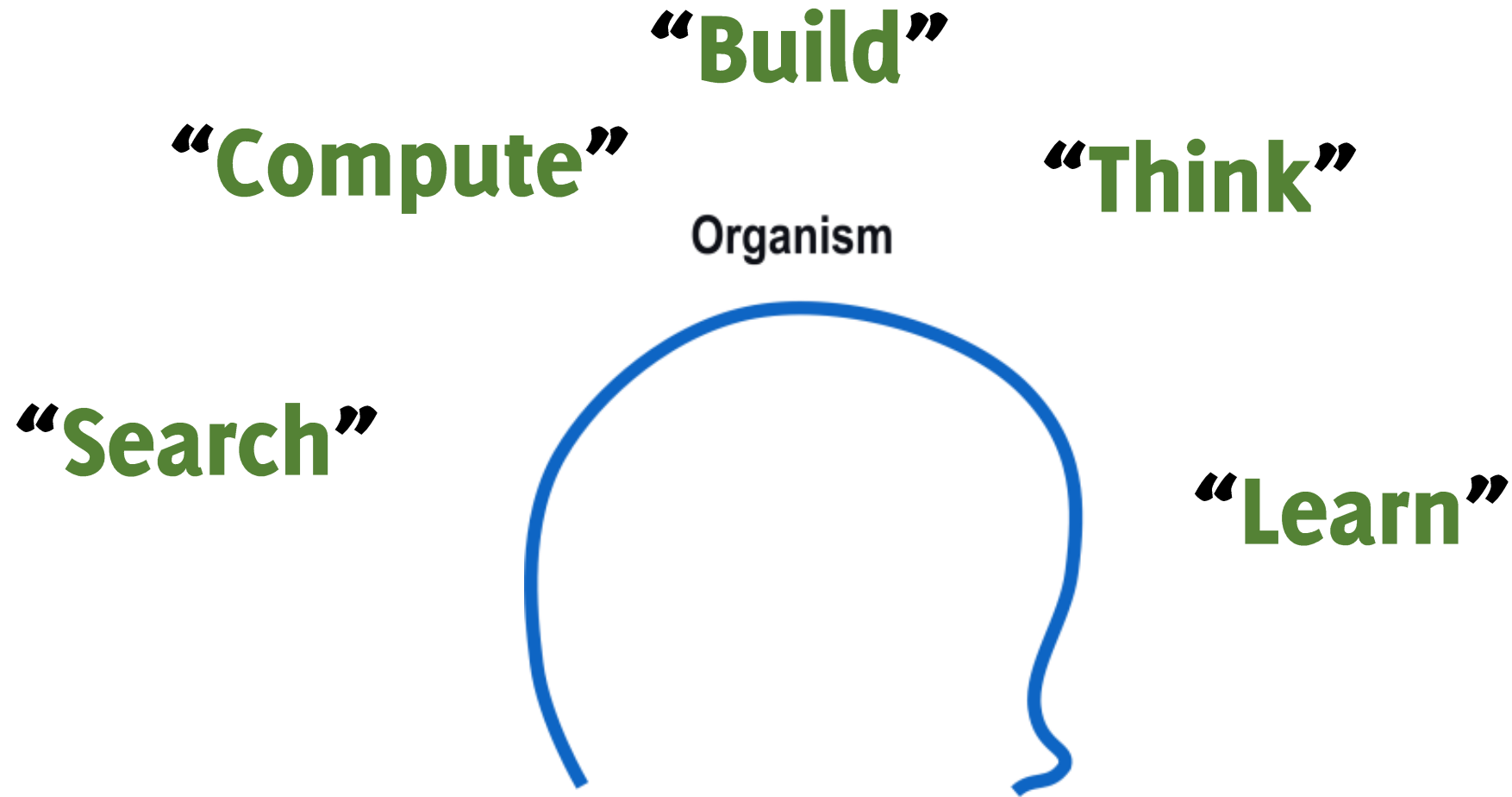

Evolutionary Algorithms for Efficient and Generalizable Tuning of Machine Control

Victor Parque

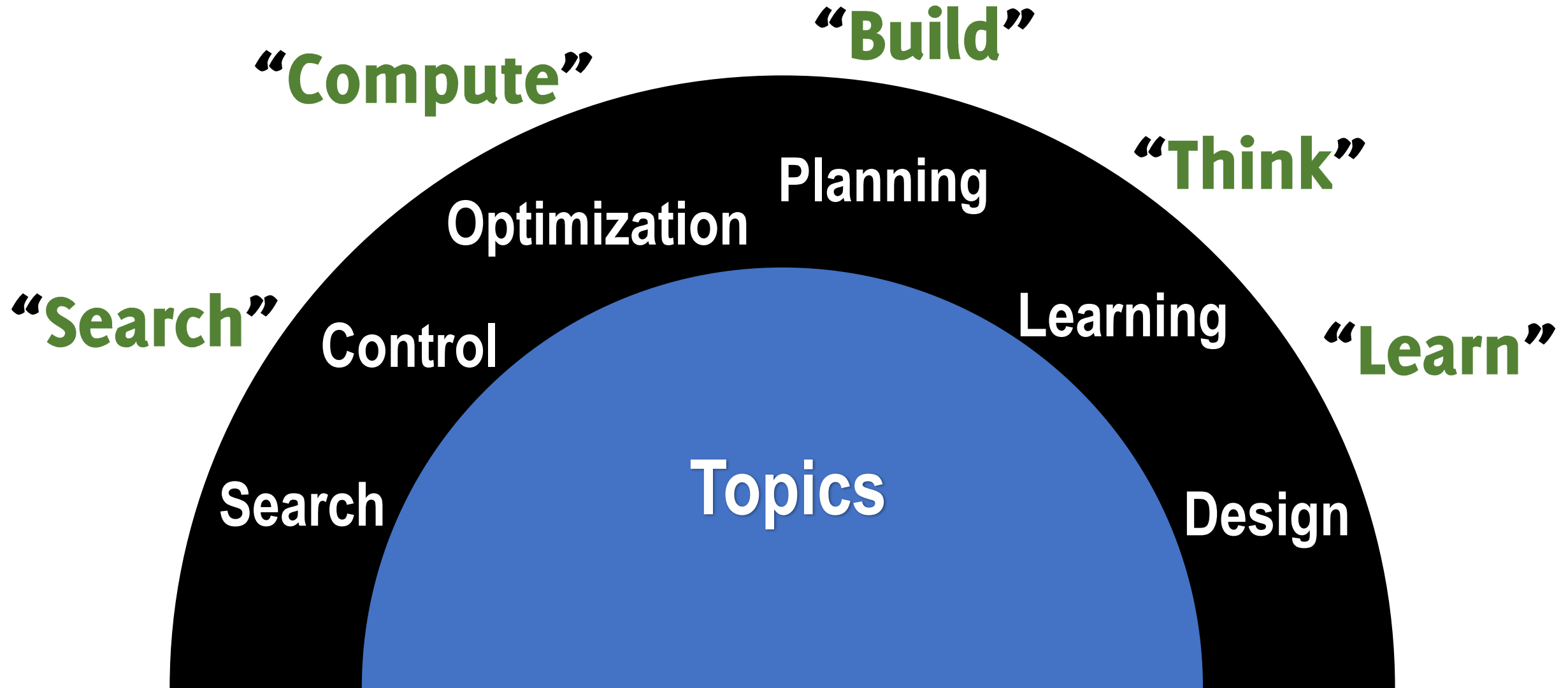
Hiroshima University

2025

Towards Living Organisms - Machines

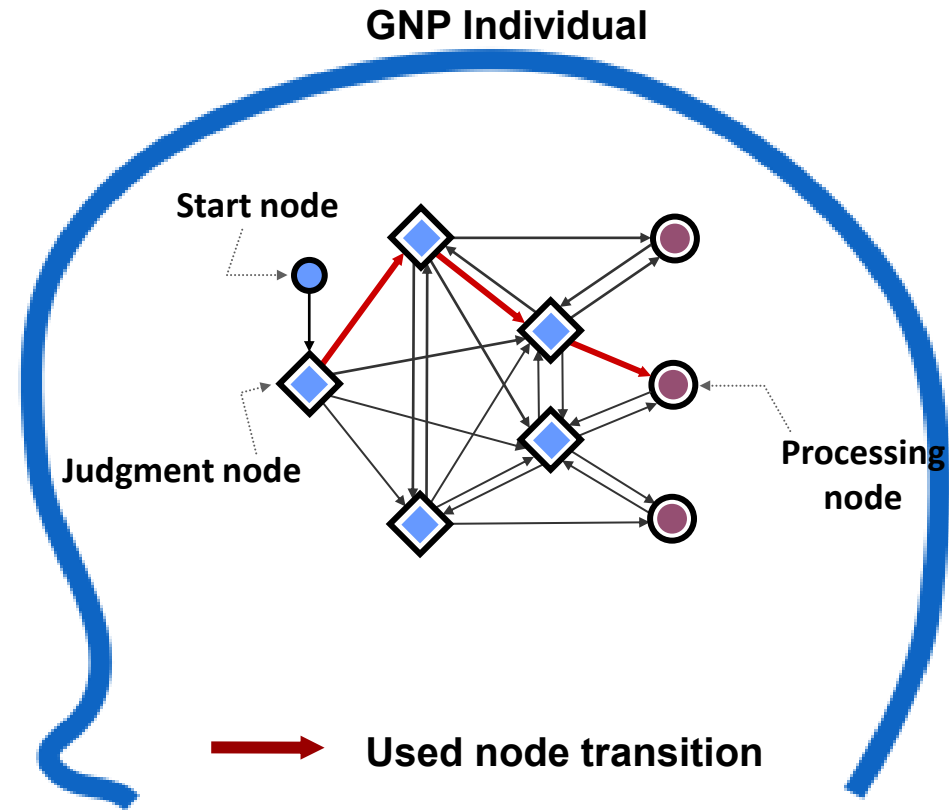


Towards Living Organisms - Machines



Genetic Network Programming (GNP)

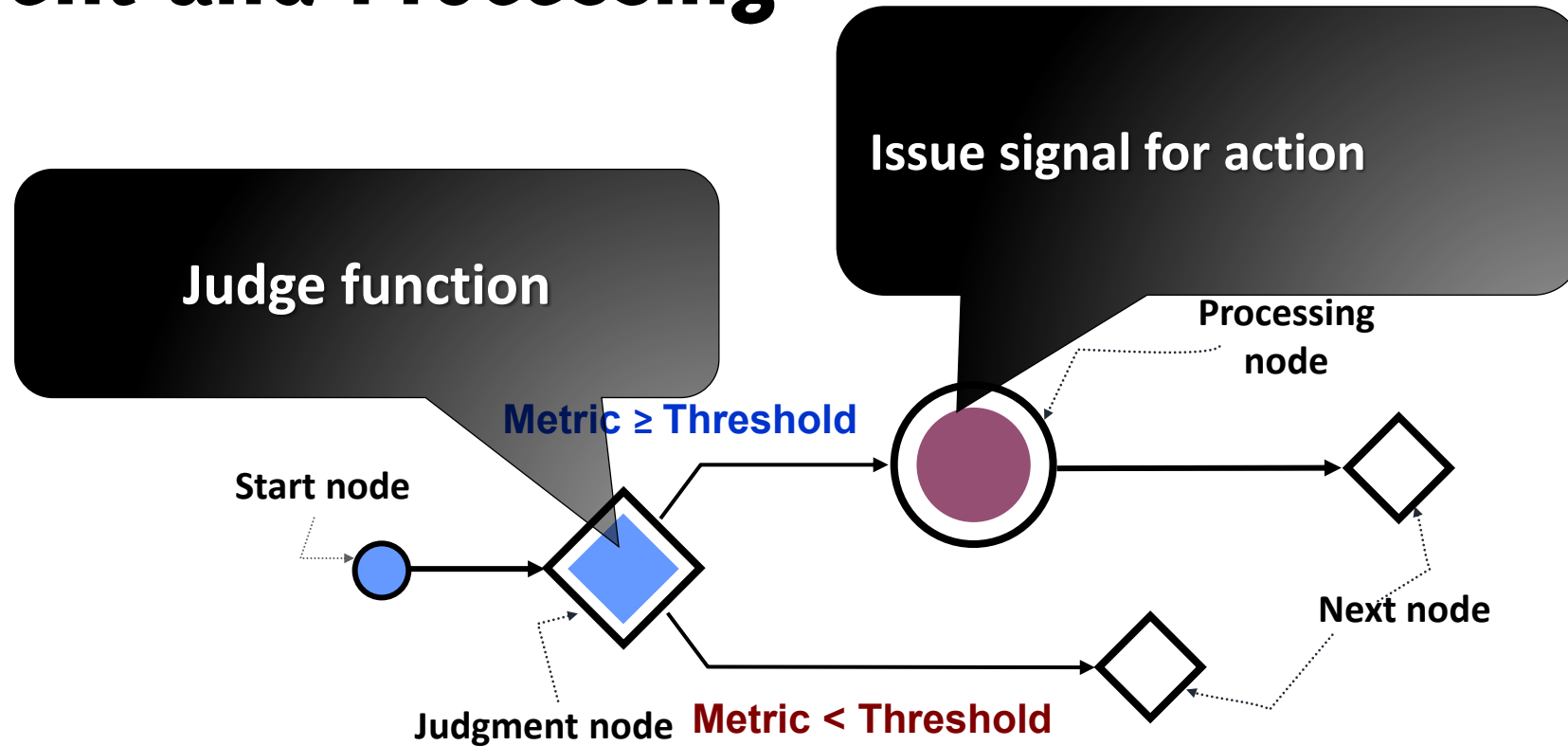
- **Evolutionary** optimization algorithm
 - *Population based*
 - *Selection, crossover, mutation*
- Phenotype is a directed **graph**
 - *GP handles trees.*
 - *GA handles strings.*
- Uses **judgement** and **processing** nodes.
 - *Effective for decision making.*



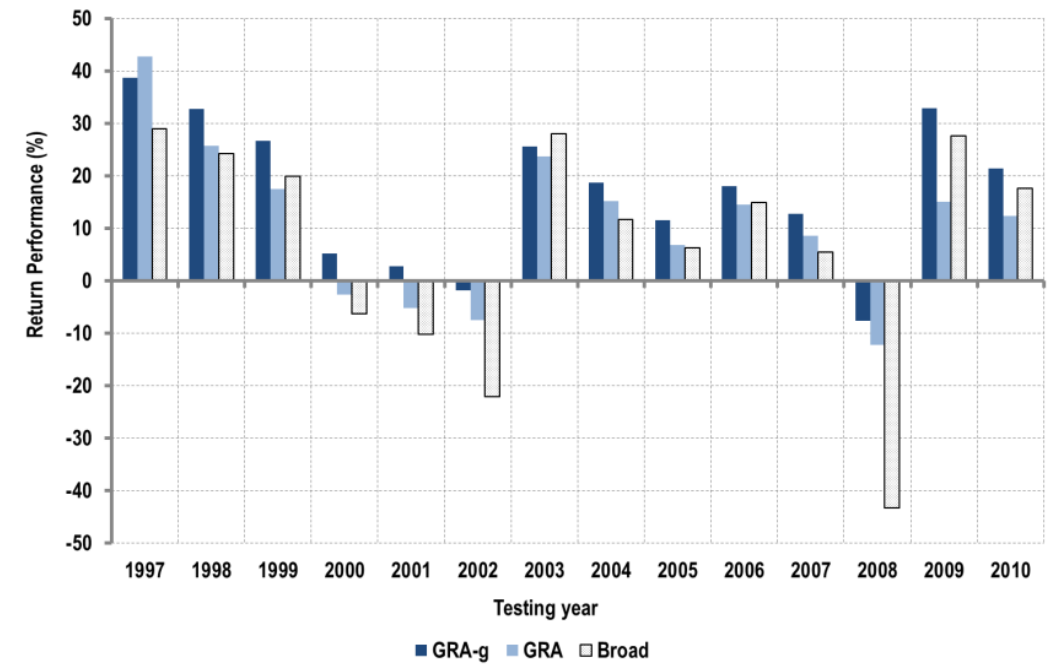
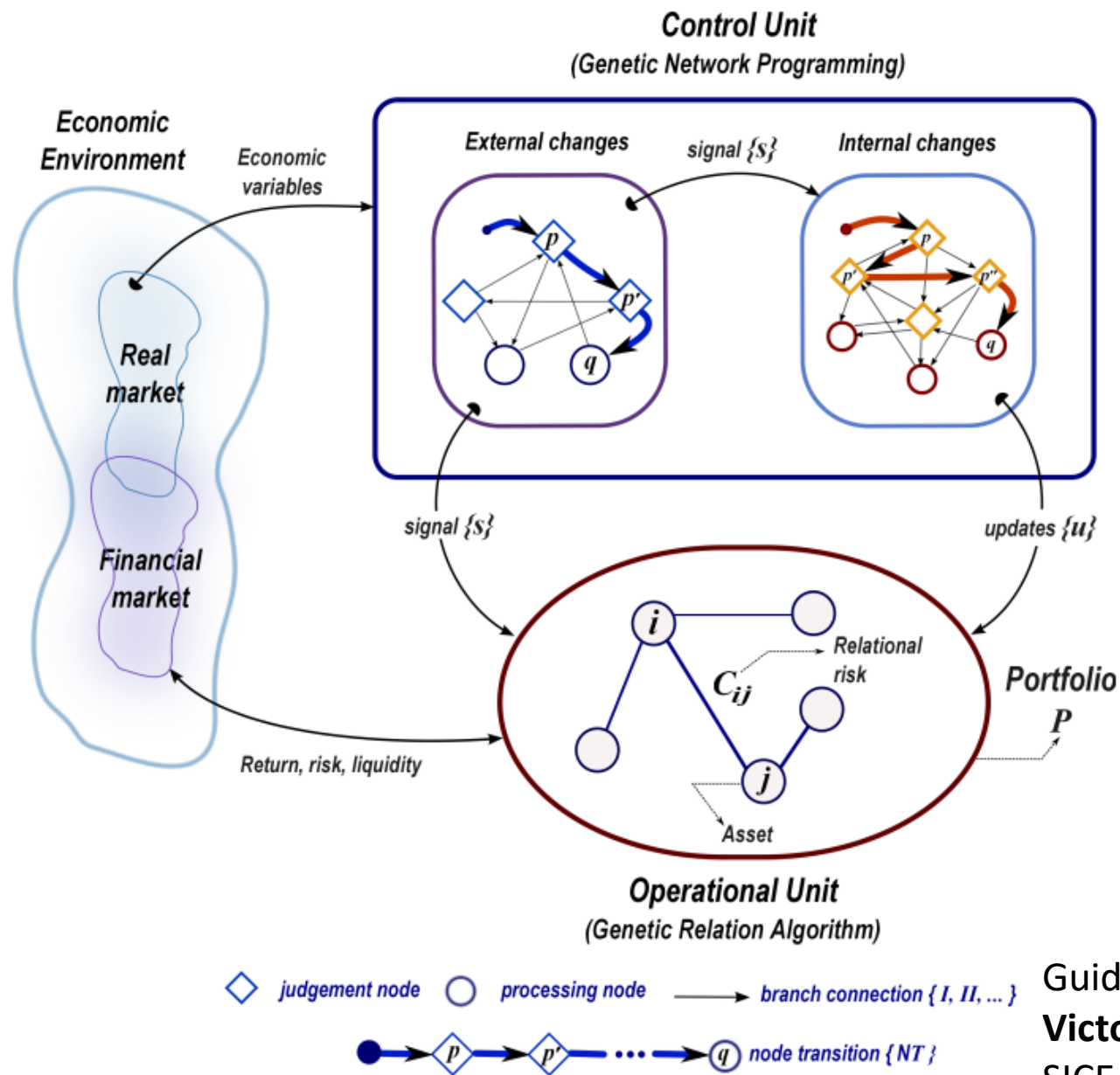
Shingo Mabu, **Kotaro Hirasawa**, Jinglu Hu

A Graph-Based Evolutionary Algorithm: Genetic Network Programming (GNP) and Its Extension Using Reinforcement Learning
Evolutionary Computation (2007) 15 (3): 369–398, MIT Press.

Judgment and Processing



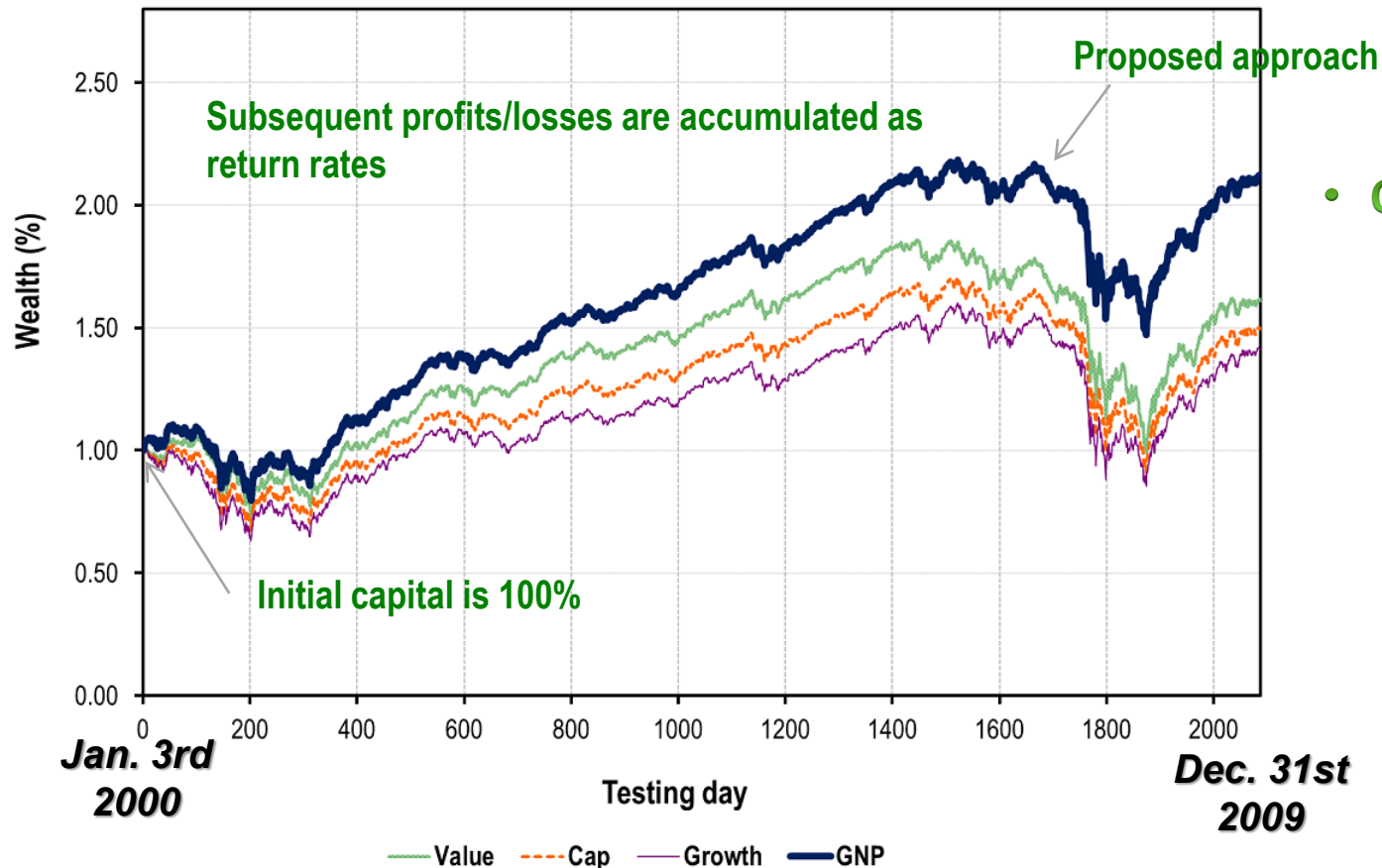
- GNP based (or other forecasting models)
 - Judgment nodes evaluate drivers that determine the states.
 - Processing nodes determine the state.
- Fitness



Guided Genetic Relation Algorithm on the Adaptive Asset Allocation
Victor Parque, Shingo Mabu and Kotaro Hirasawa
 SICE Annual Conference, Tokyo, Japan, 2011

Comparison in the testing period

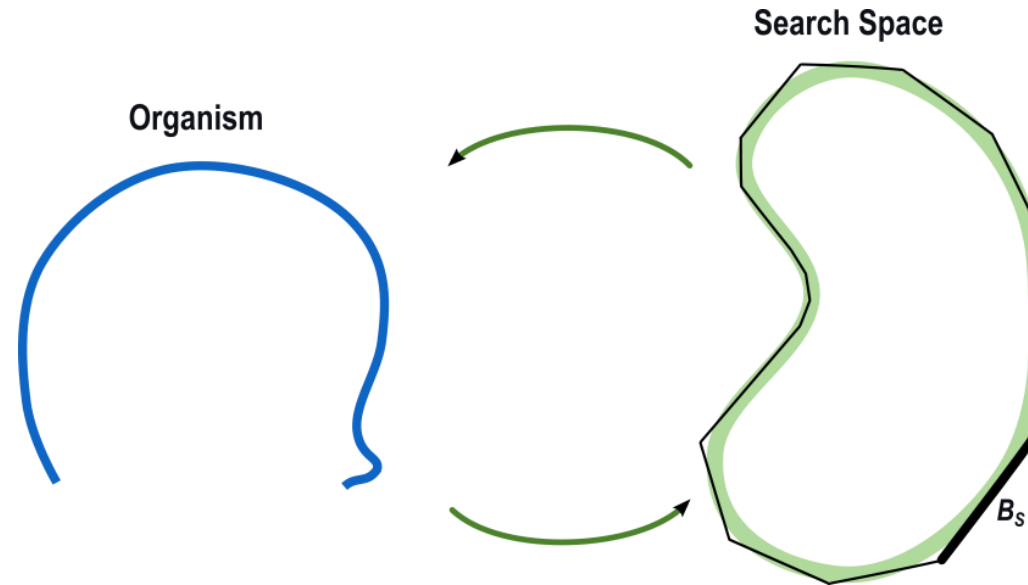
Accumulative wealth



- **Outperforms the benchmarks**
 - 1.38 times better in return accumulation over the long term.
 - 1.42 times better in return accumulation during the latest financial distress period.

Search

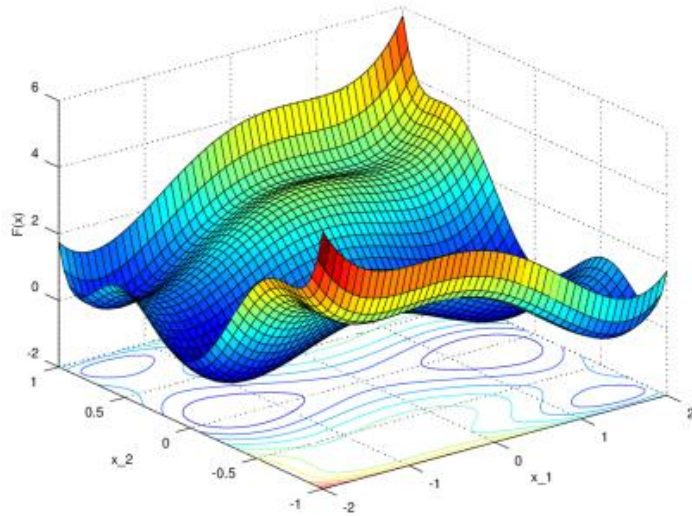
How to search for the global optimum?



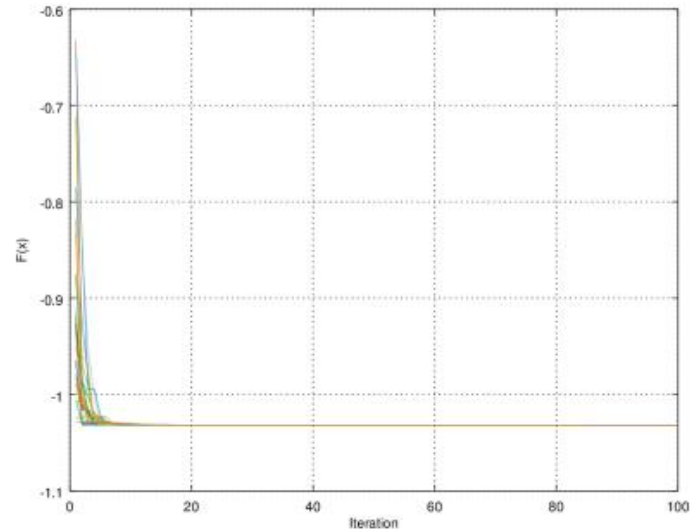
Enables to build almost anything

products, machines from scratch

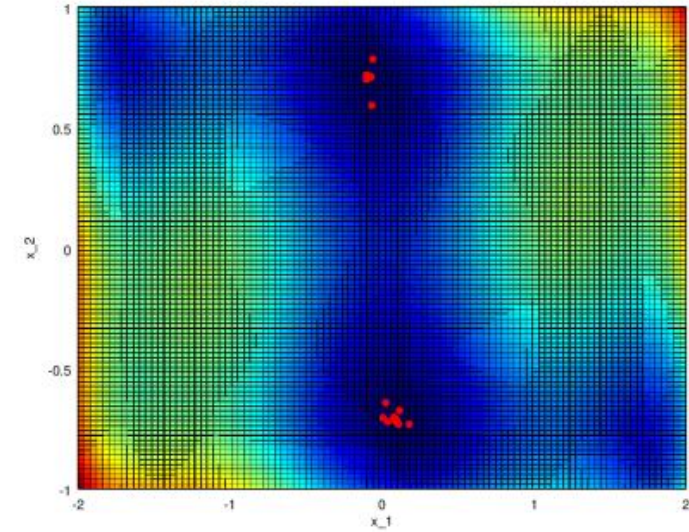
Global Optimization



Landscape

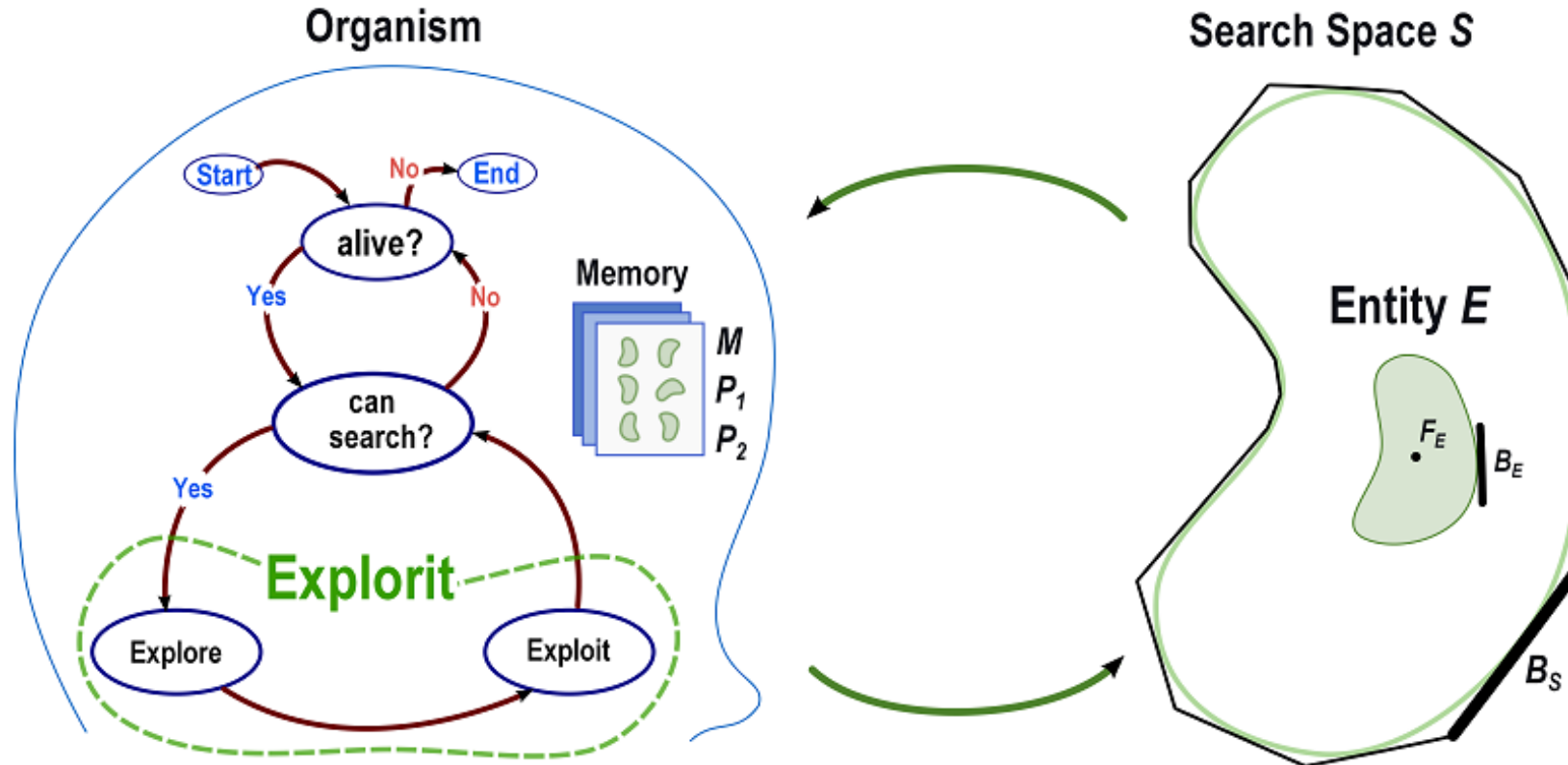


Convergence



Minimal Points

Exploration and Exploitation



INSTANCE	EXPLORIT		BENCHMARK	
	Evaluations	Performance	Evaluations	Performance
Synthetic	48 ± 15	$2.12\text{E-}6 \pm 1.41\text{E-}6$	87 ± 18	$1.29\text{E-}4 \pm 1.71\text{E-}4$
Multi-dimensional	3E6	$1.62\text{E}9 \pm 1.5\text{E}8$	3E6	$1.15\text{E}11 \pm 5.12\text{E}11$
Vehicle Powertrain	386 ± 71	(5.18, 0.58, 0.24, 0.27)	1020 ± 192	(5.59, 2.14, 0.25, 0.24)

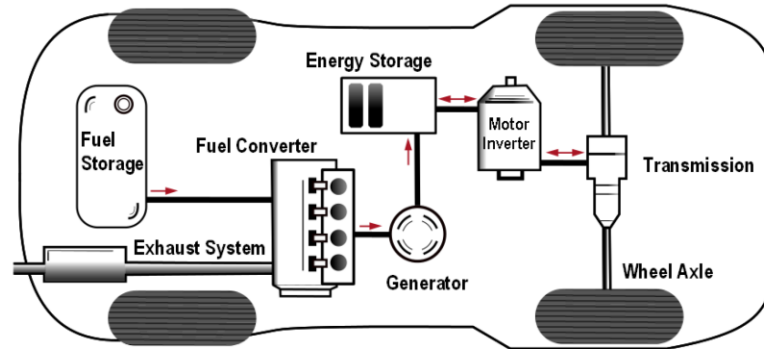
Victor Parque, Masakazu Kobayashi and Masatake Higashi. Explorit for Global Optimization
 5th NIPS Workshop on Optimization for Machine Learning, Lake Tahoe, Sierra Nevada, US, 2012

Case: Vehicle Powertrains

Simulator: **Advisor** (based on real world tests)

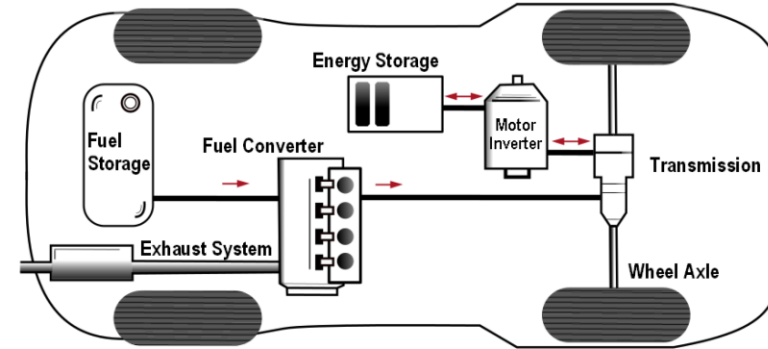
Goal: Maximize mileage, and minimize emissions

SHEV



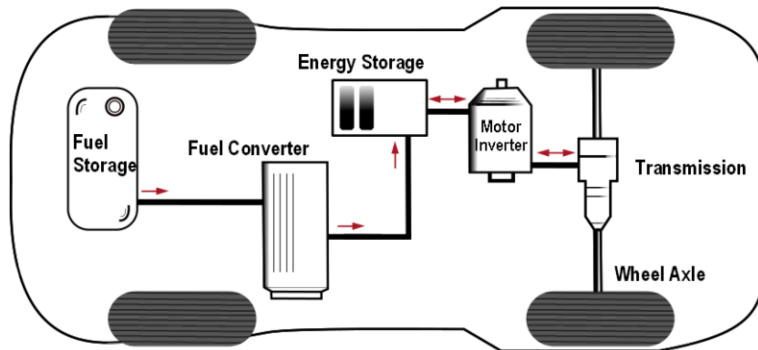
a) Series Hybrid Electric Vehicle (SHEV)

PHEV



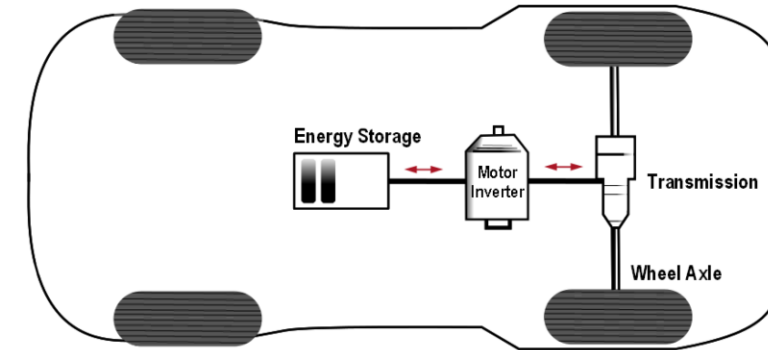
b) Parallel Hybrid Electric Vehicle (PHEV)

FCV



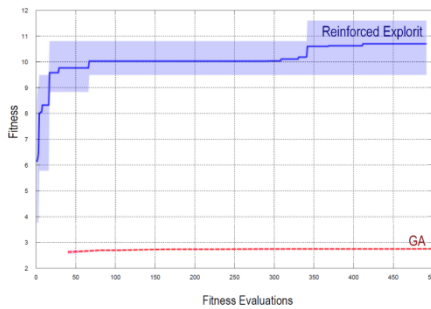
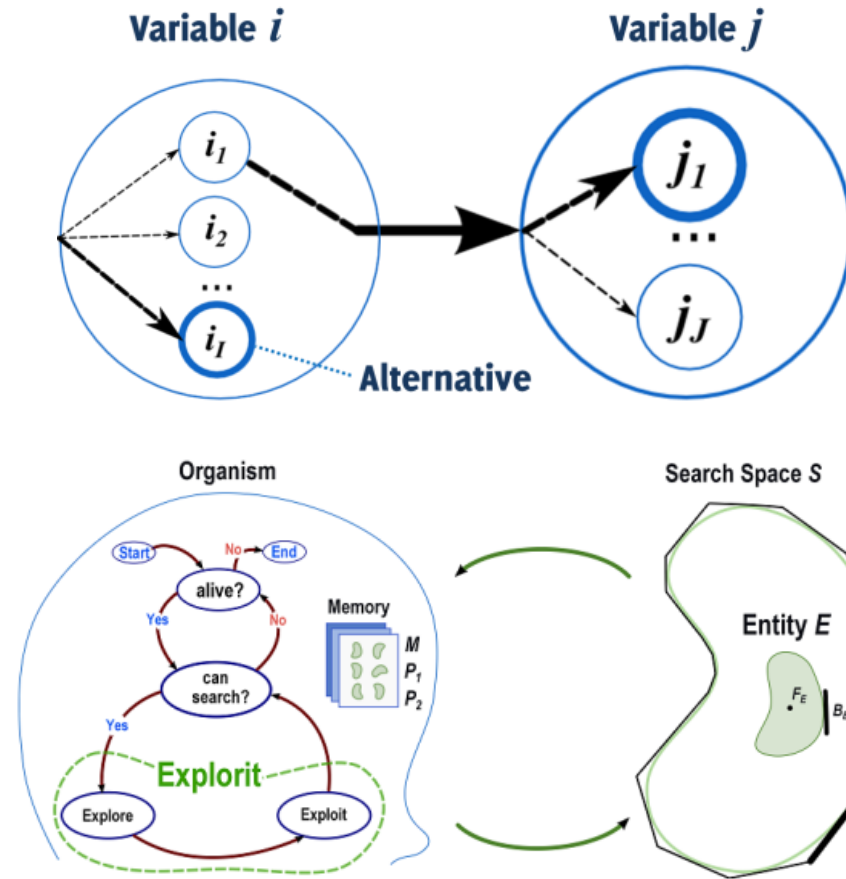
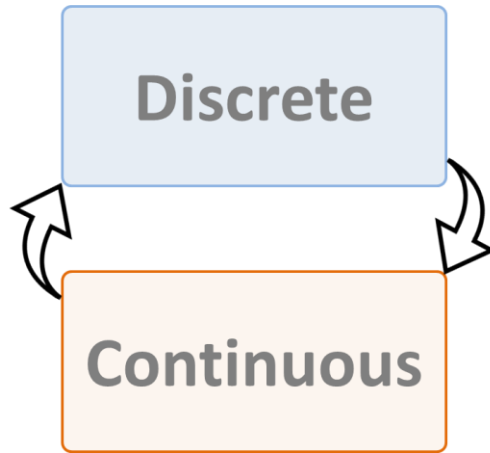
c) Fuel Cell Vehicle (FCV)

EV

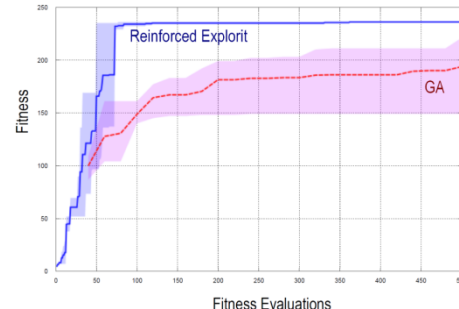


d) Electric Vehicle (EV)

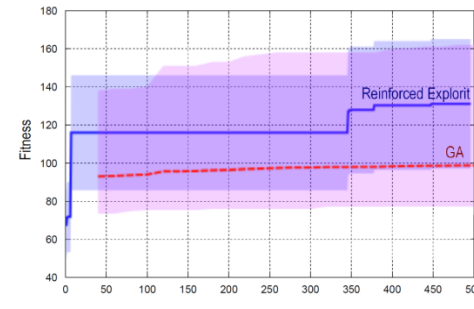
Reinforced Explorit



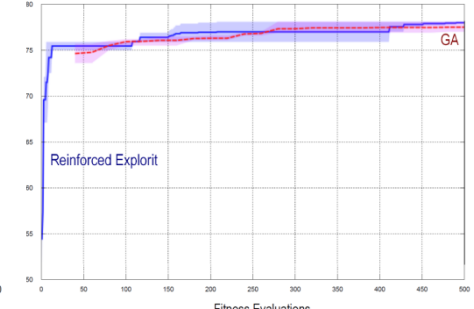
(a) Series Hybrid Electric Vehicle



(b) Parallel Hybrid Electric Vehicle



(d) Electric Vehicle



(c) Fuel Cell Vehicle

Serial HEV

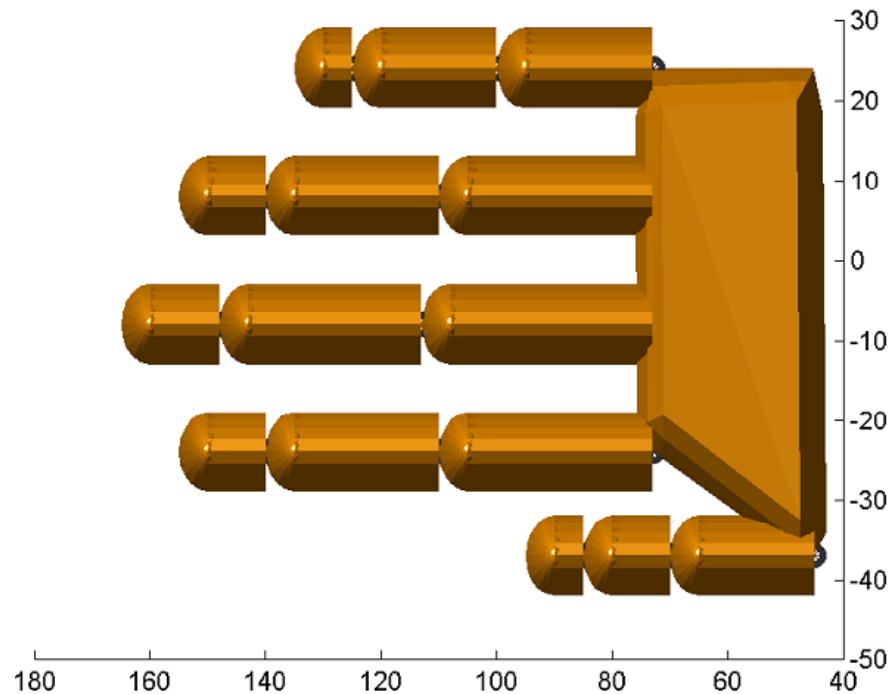
Parallel HEV

Electric

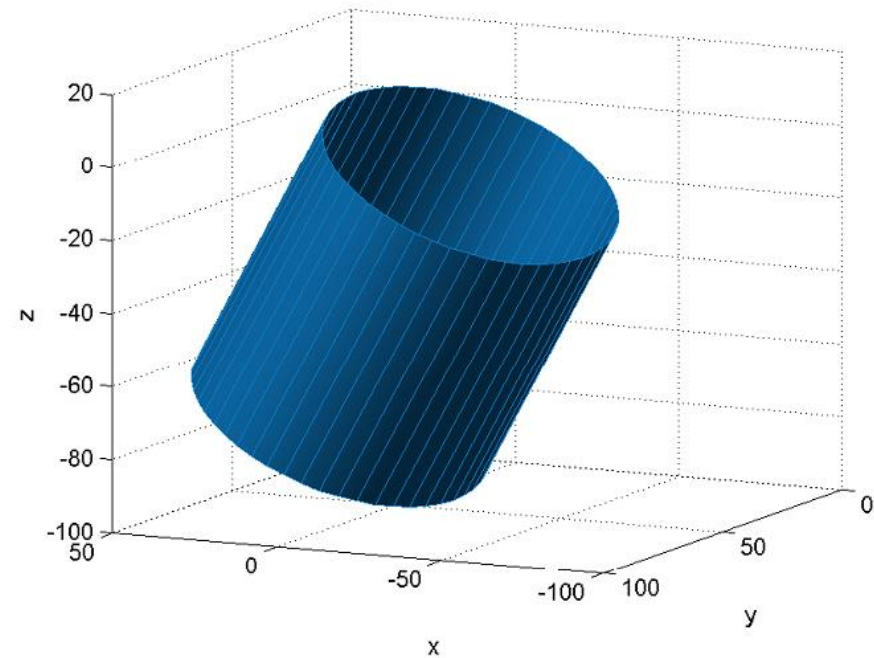
Fuel Cell

Neural Computing with Concurrent Synchrony

Robotic Hand

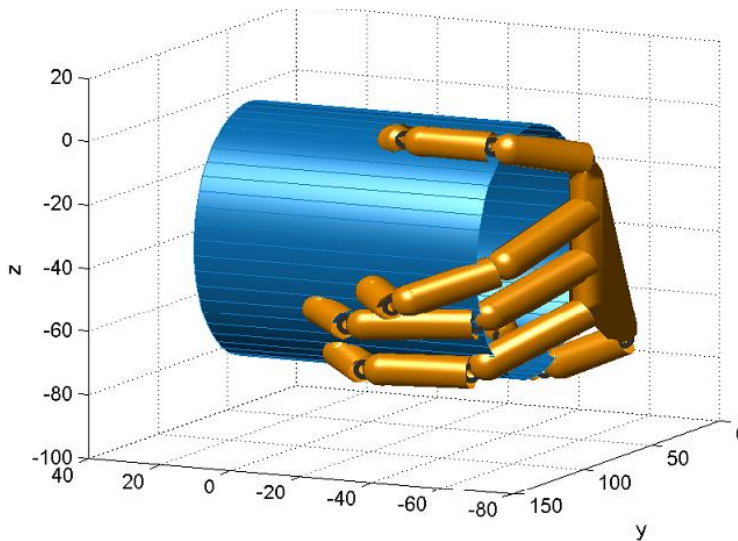
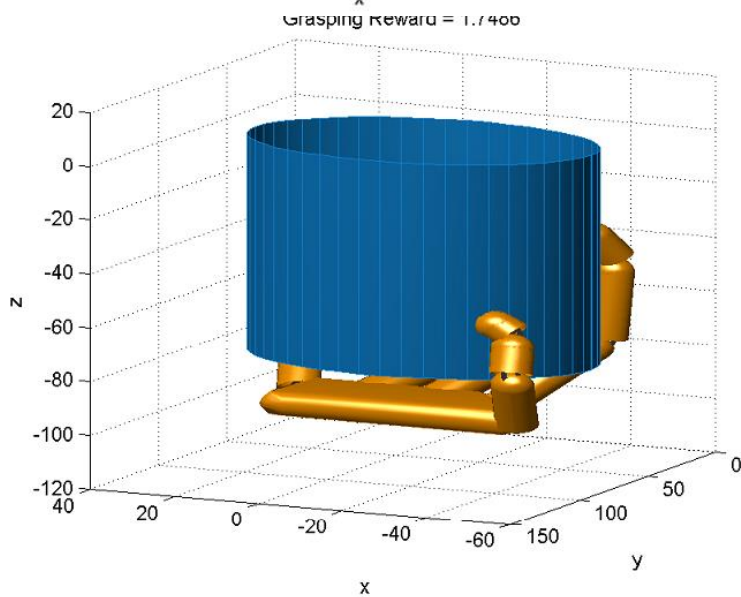
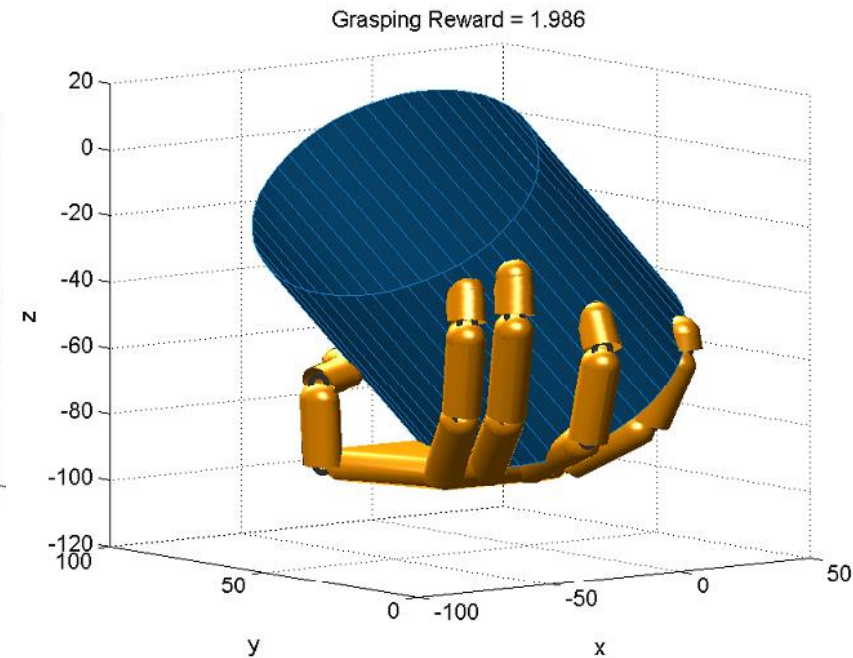
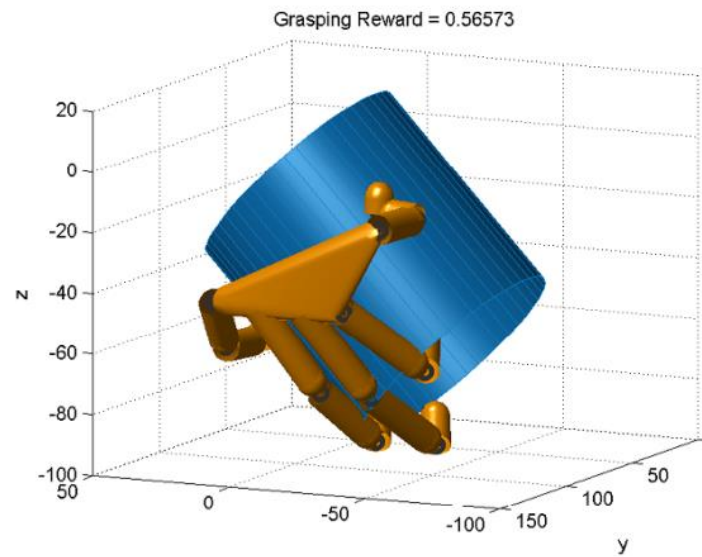


Object to Grasp



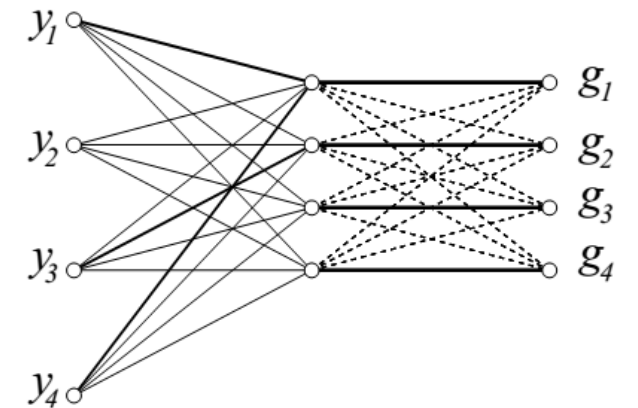
Victor Parque, Masakazu Kobayashi, Masatake Higashi:
Neural Computing with Concurrent Synchrony. ICONIP (1) 2014: 304-311

Grasping Results



Object

Action



Excitatory

 **Direct Transition**

Inhibitory

 **Indirect Transition**

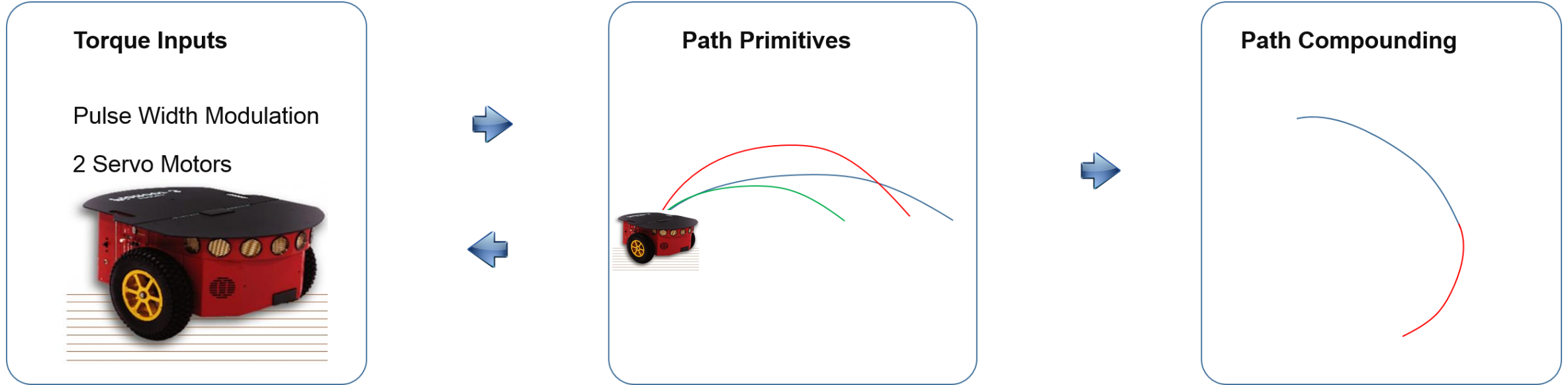
A Study of Fairness Functionals for Smooth Path Planning in Mobile Robots

Victor Parque

2021

How to compute smooth curves effectively?

e.g. safe path planning in robots



Dynamic Models



Principled



Unrealistic (noise)

Data-driven Models



Practical



Computationally intensive

Curvature

$$\mathbf{r}(u) = \sum_{i=0}^n B_i^n(u) \mathbf{p}_i, \quad u \in [0, 1]$$

Bézier curve

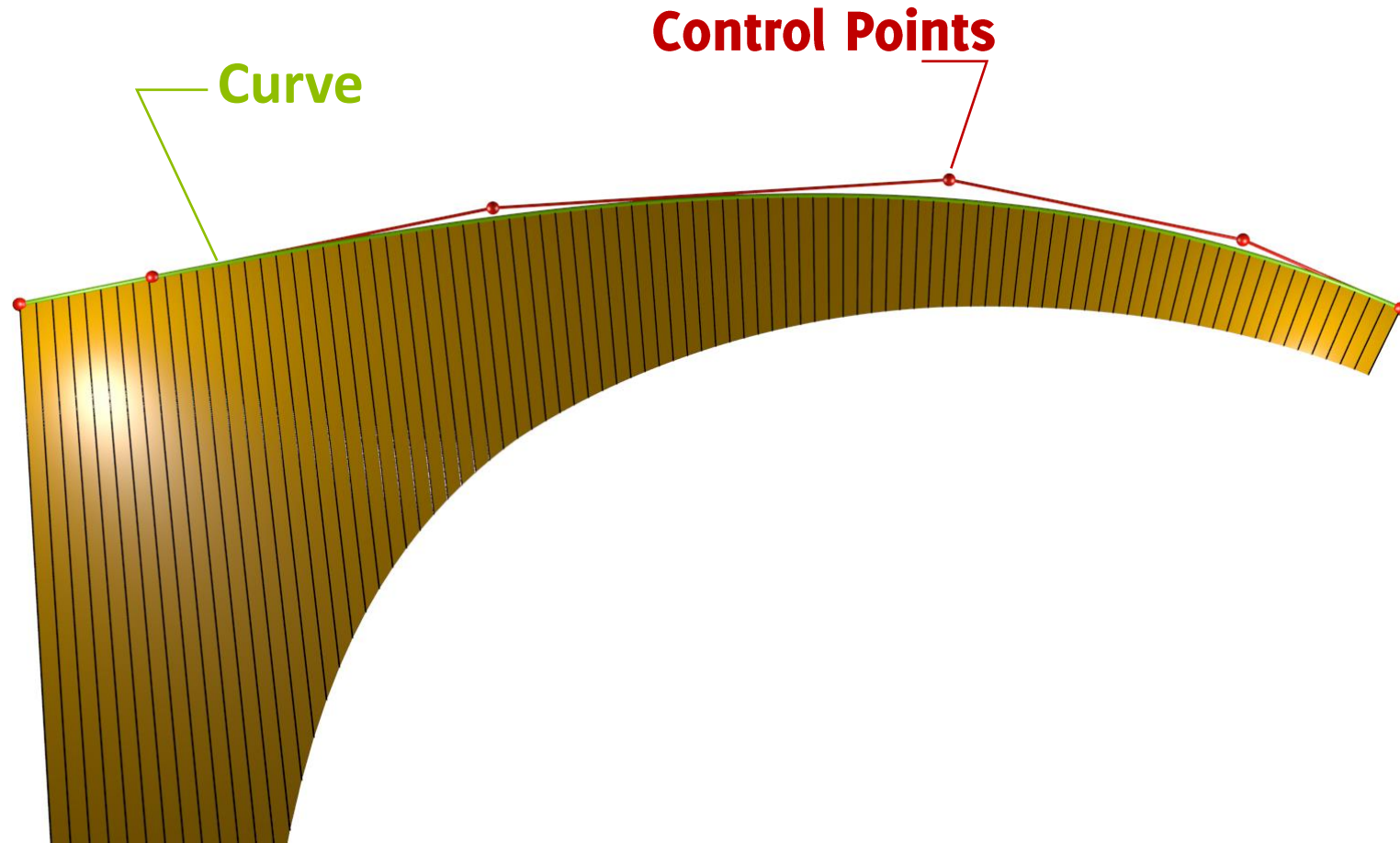
$$B_i^n(u) = \binom{n}{i} u^i (1-u)^{n-i}$$

Bernstein polynomial

$$\kappa = \frac{\|\mathbf{r}' \times \mathbf{r}''\|}{\|\mathbf{r}'\|^3}$$

Curvature

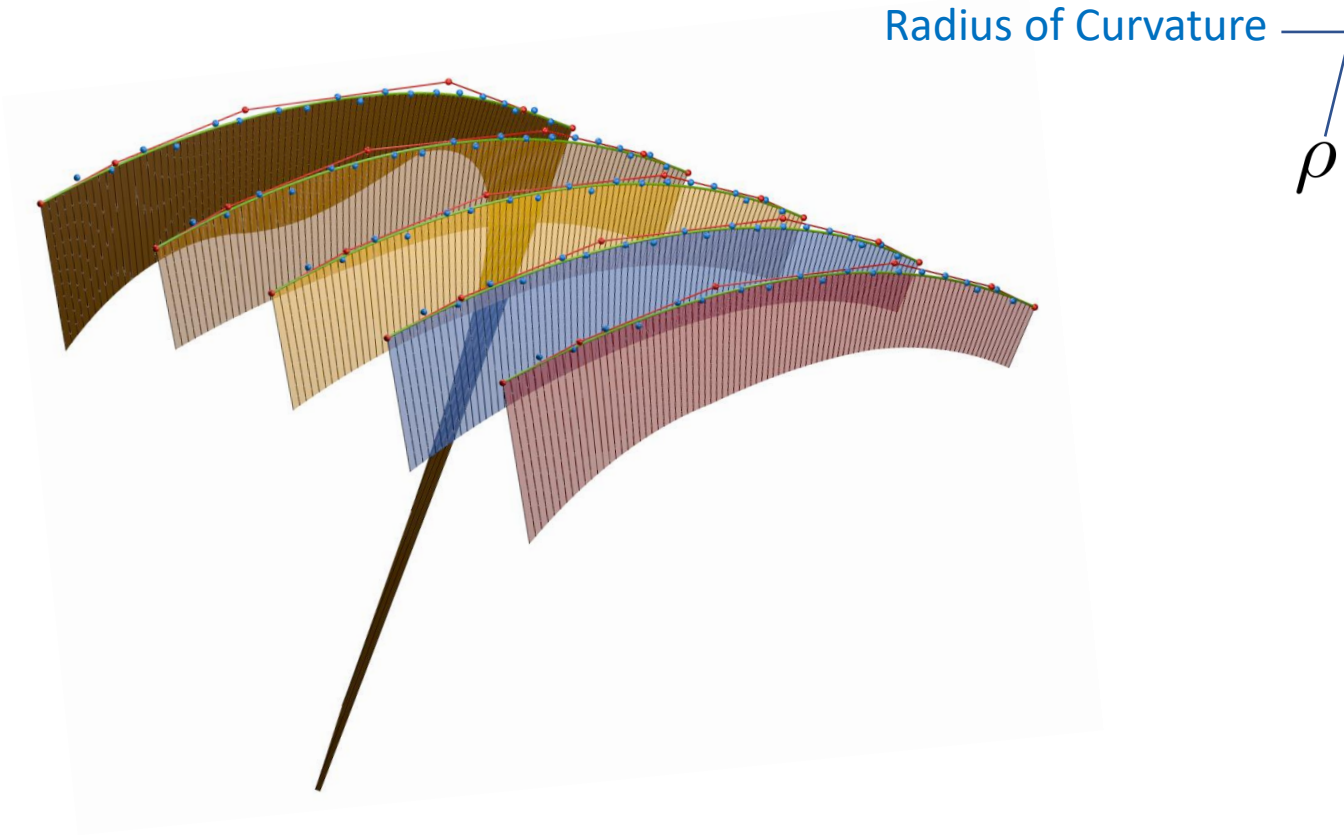
Curvature Profile



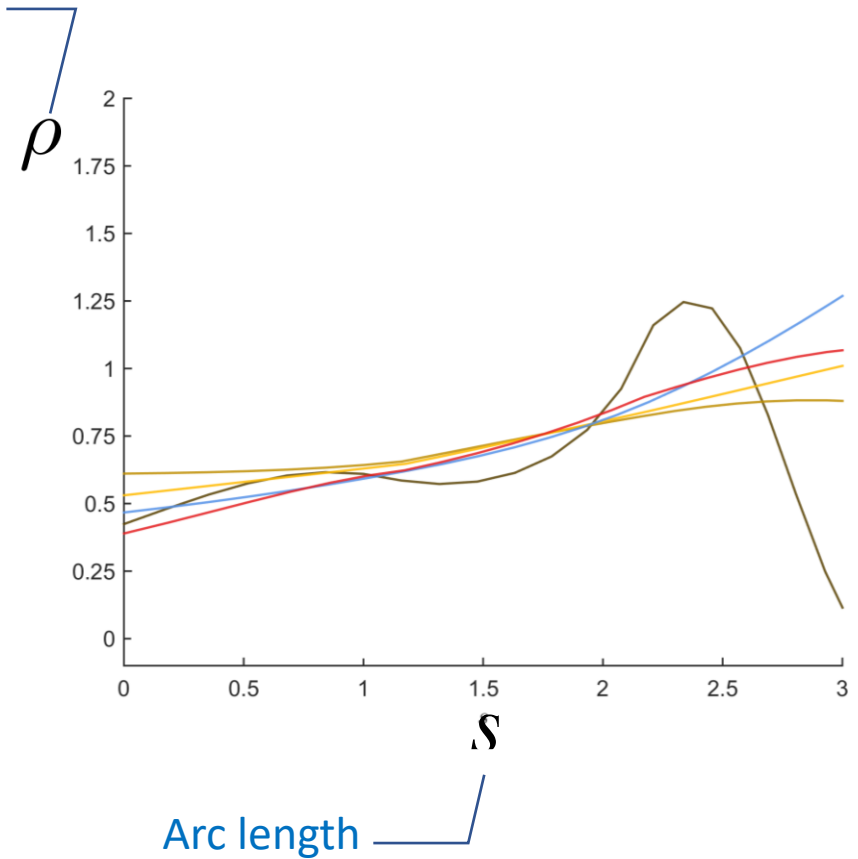
Curvature Profile

Radius of curvature

Curve profiles



Curvature Profiles



Computing Smooth Curves

$$\min_{p_i} F = E + \lambda H$$

Fit to anchor points

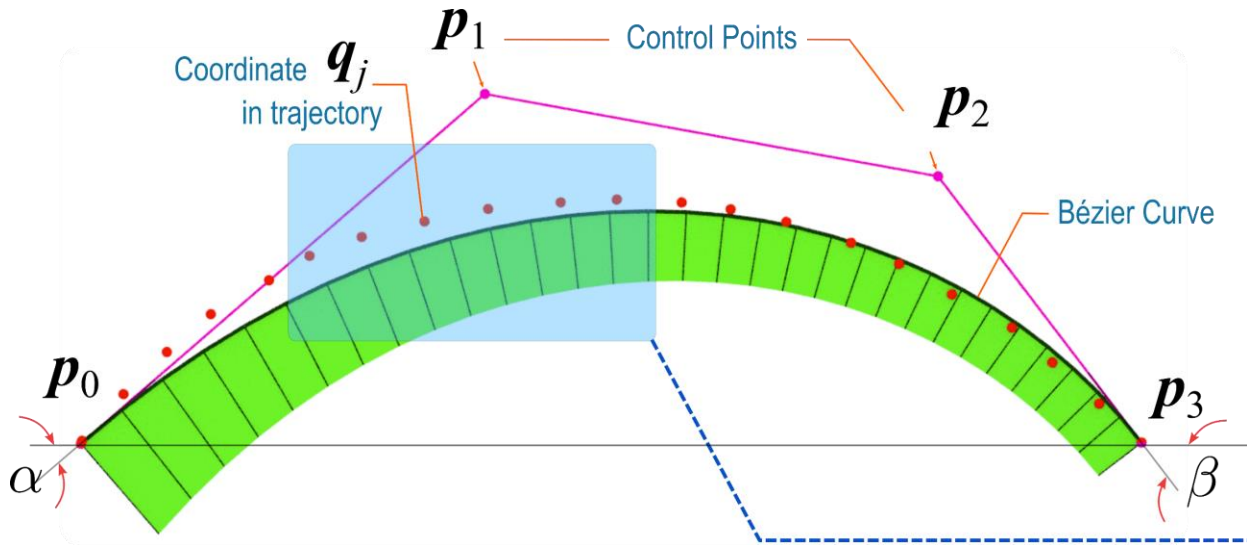
$$E = \sum_{j=1}^m \|a_j\|^2$$

Fairness functional

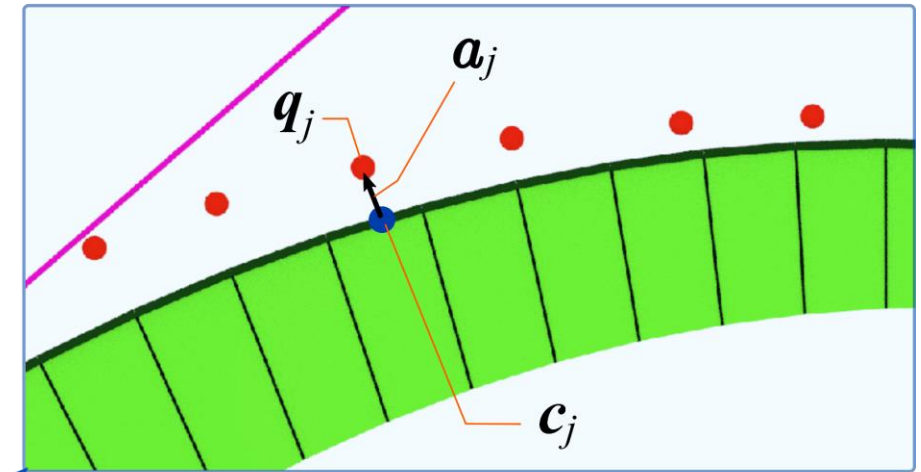
$$H(\kappa) = \int \left(h(\kappa) \right)^2 ds$$

curvature

arc length



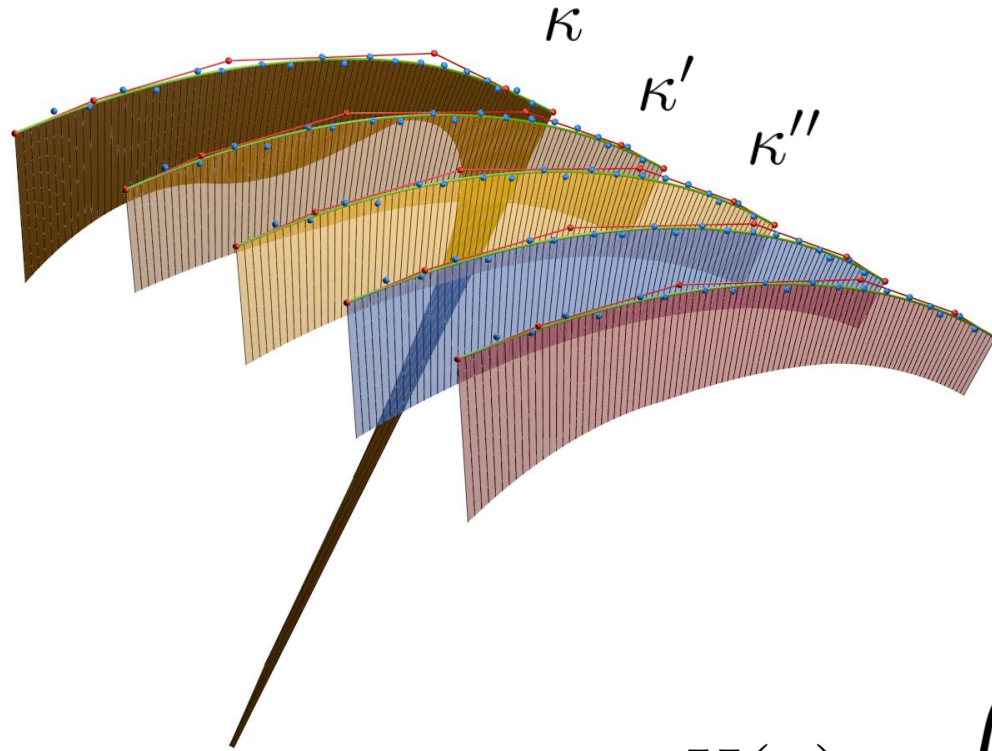
(a) Curvature Profile



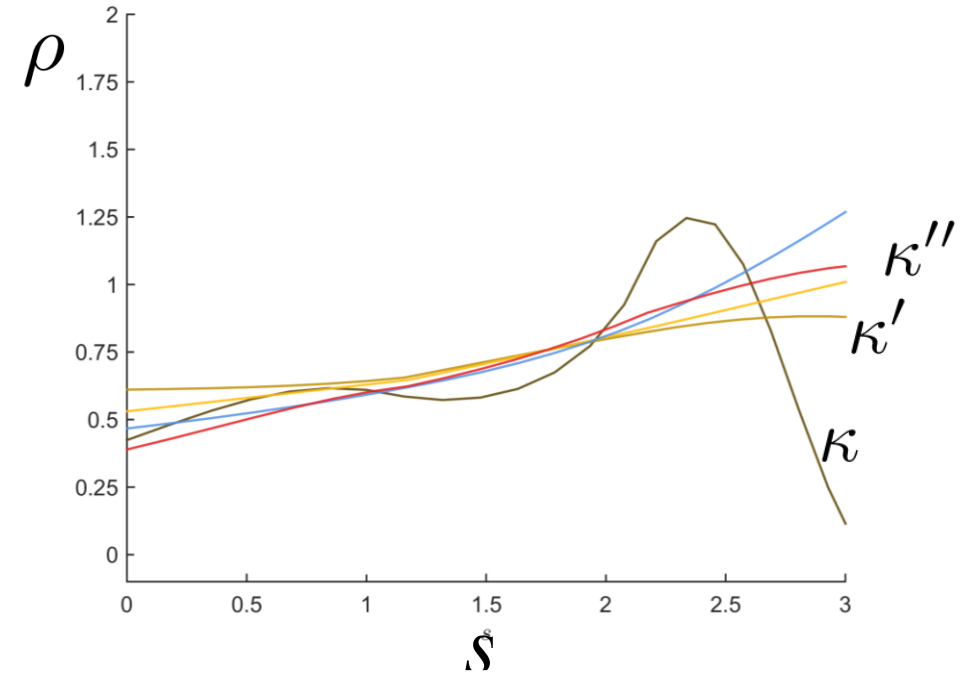
(b) Vector a_j

Smoothness: Fairness Functionals

Curve profiles



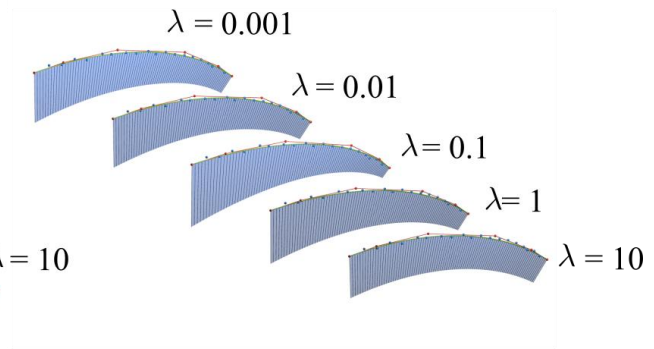
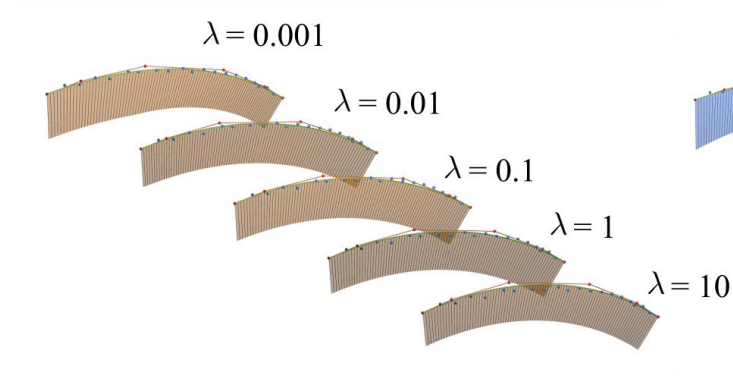
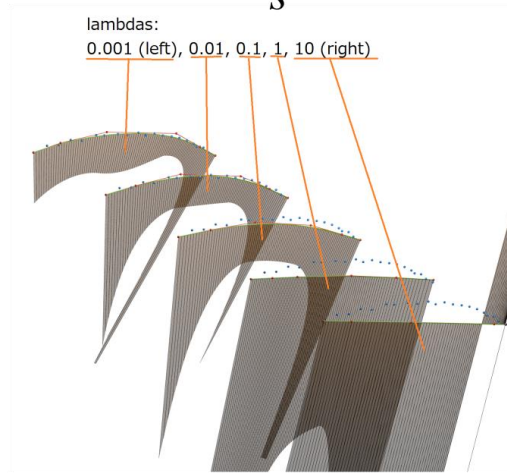
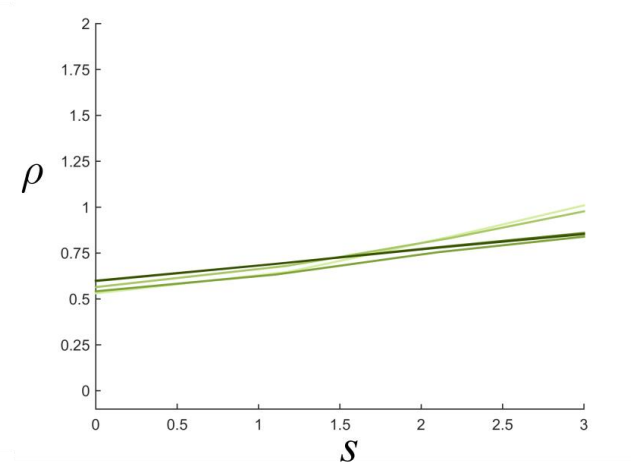
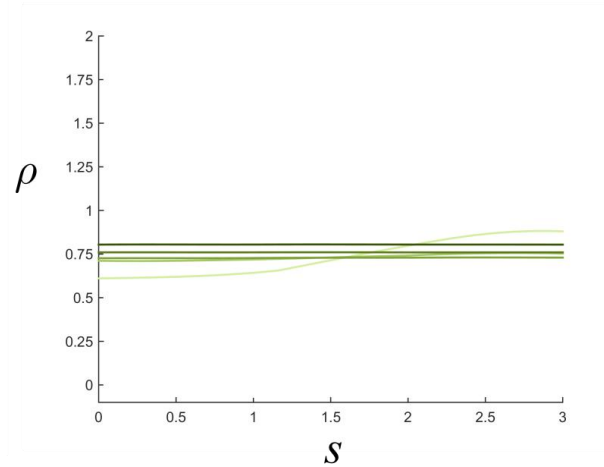
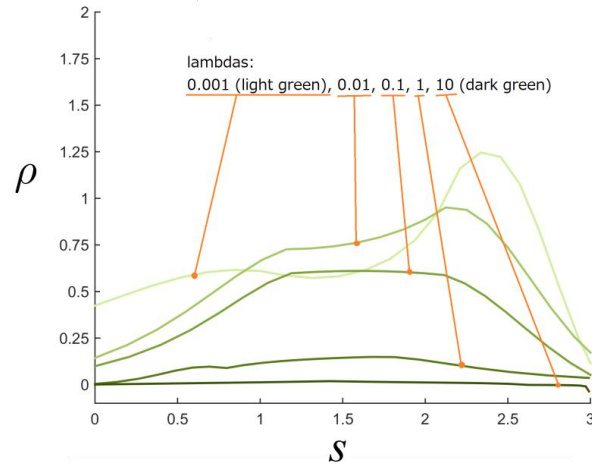
Curvature Profiles



$$H(\kappa) = \int \left(h(\kappa) \right)^2 ds$$

Computing Smooth Curves

The functional $h(\kappa) = \kappa''$ is robust



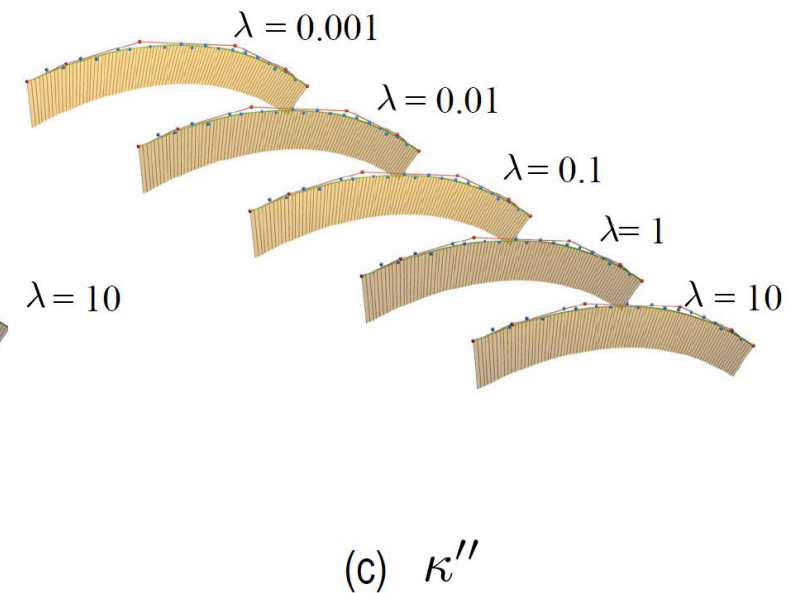
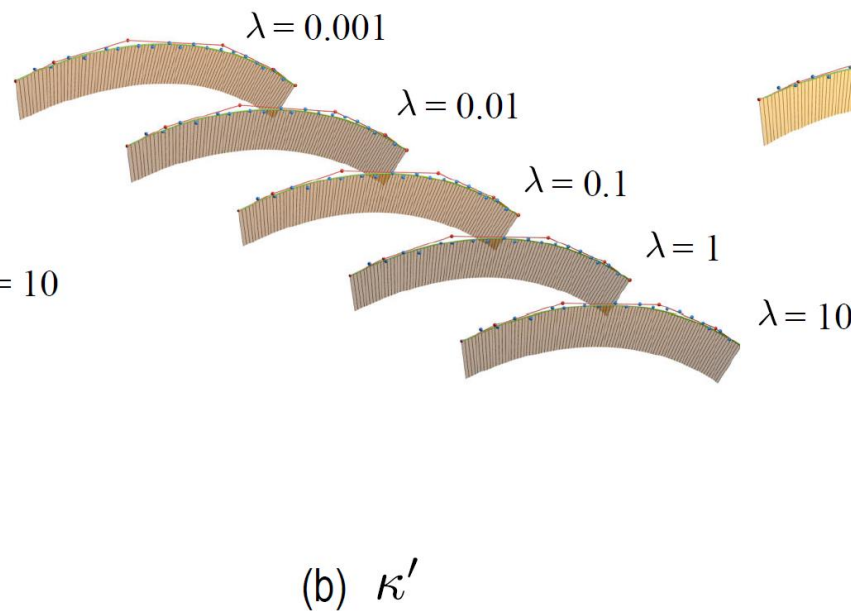
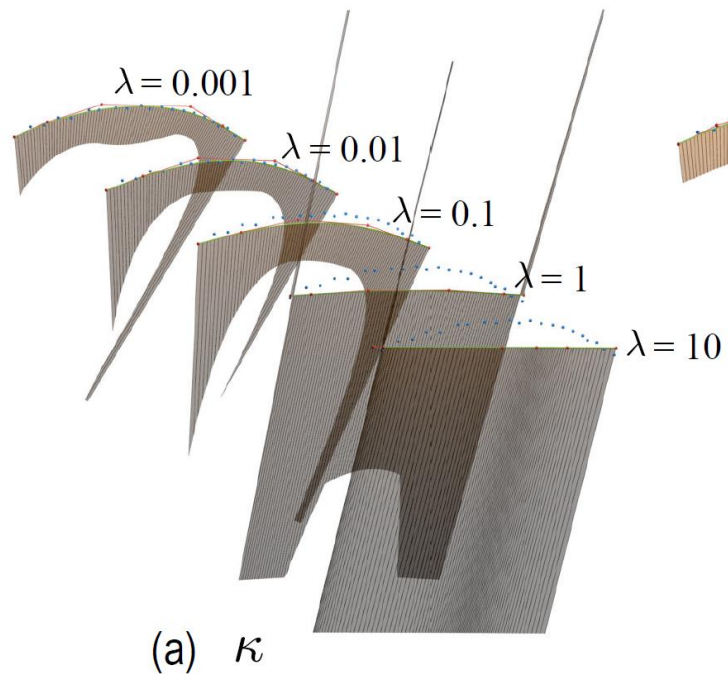
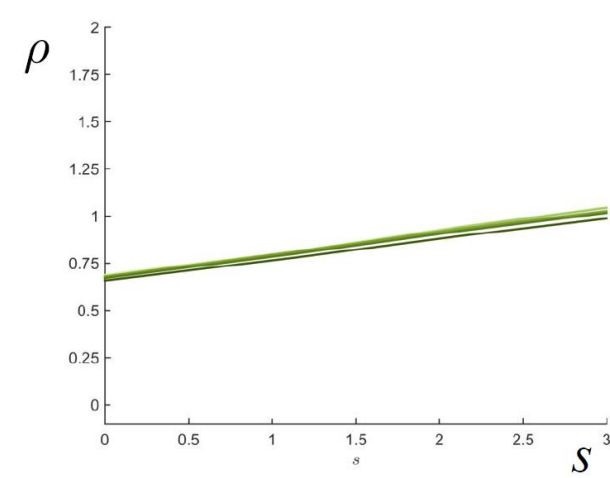
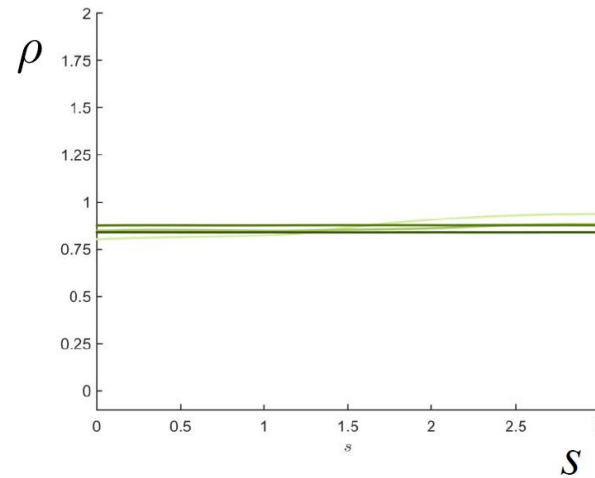
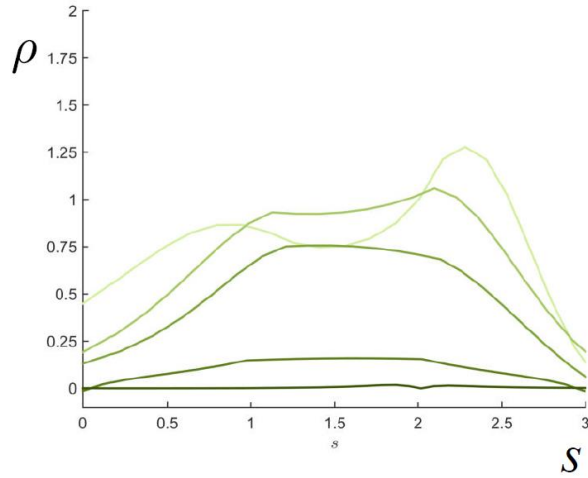
(a) κ

(b) κ'

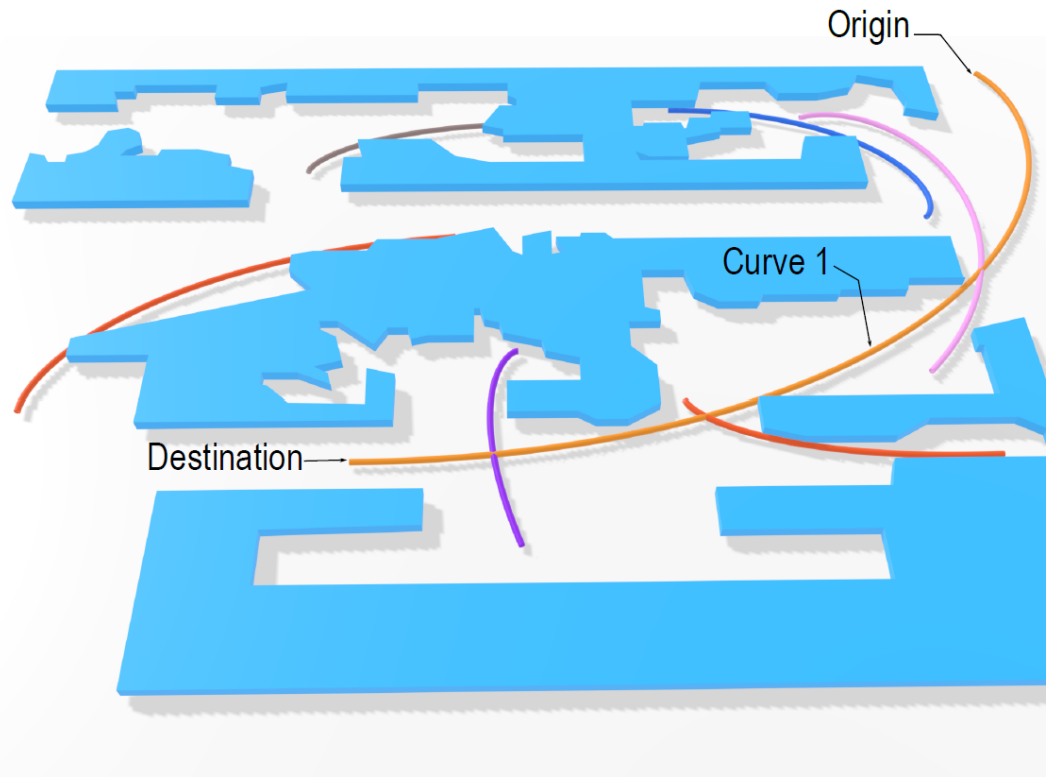
(c) κ''

Computing Smooth Curves

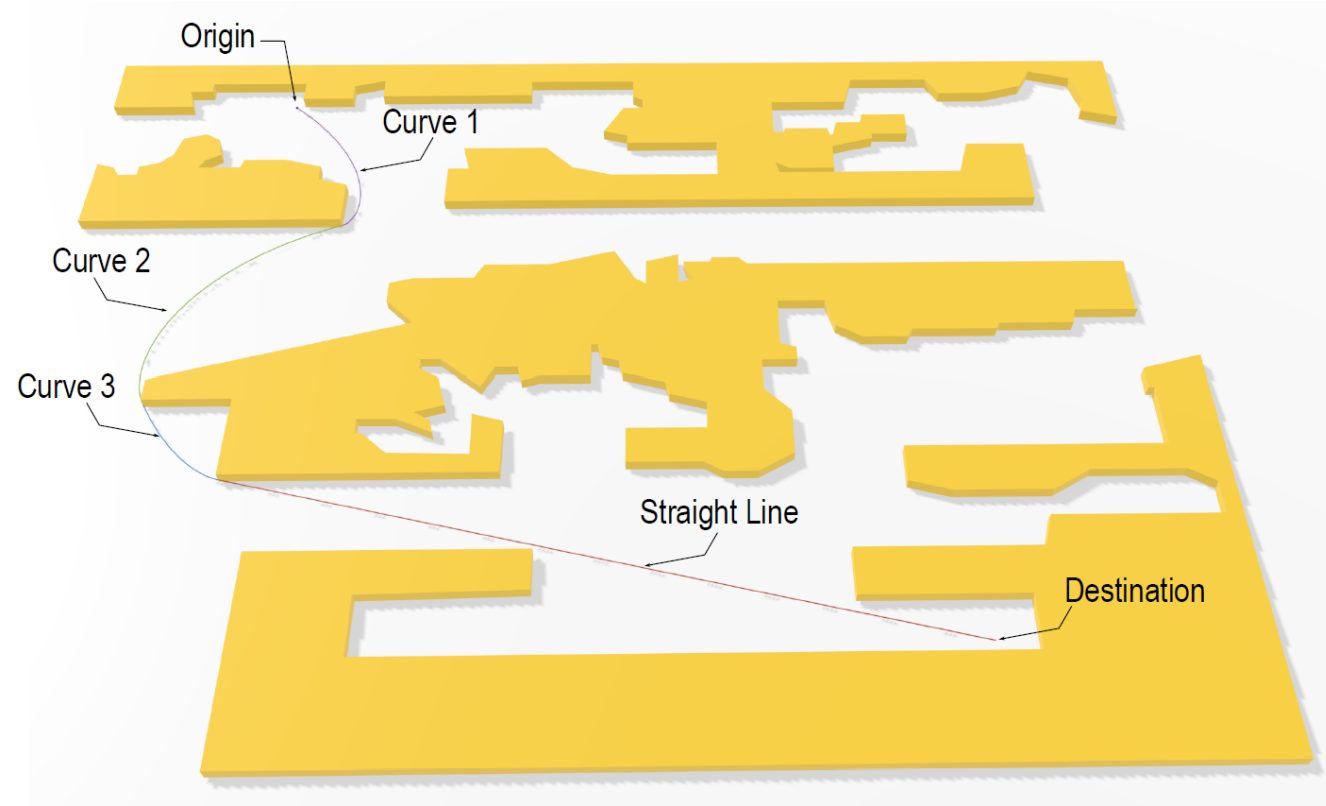
The functional $h(\kappa) = \kappa''$ is robust



Examples in Path Planning



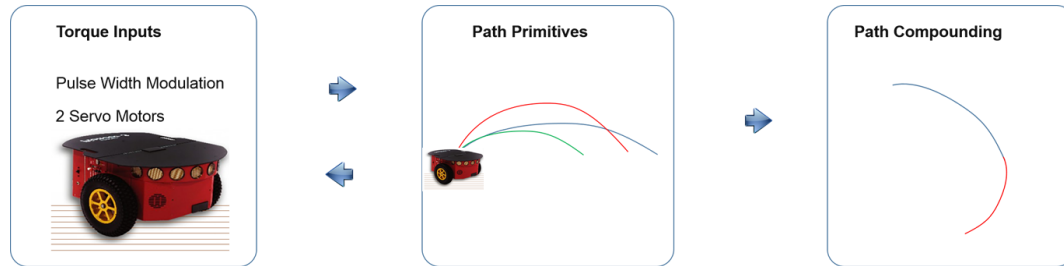
(a) Single Curves



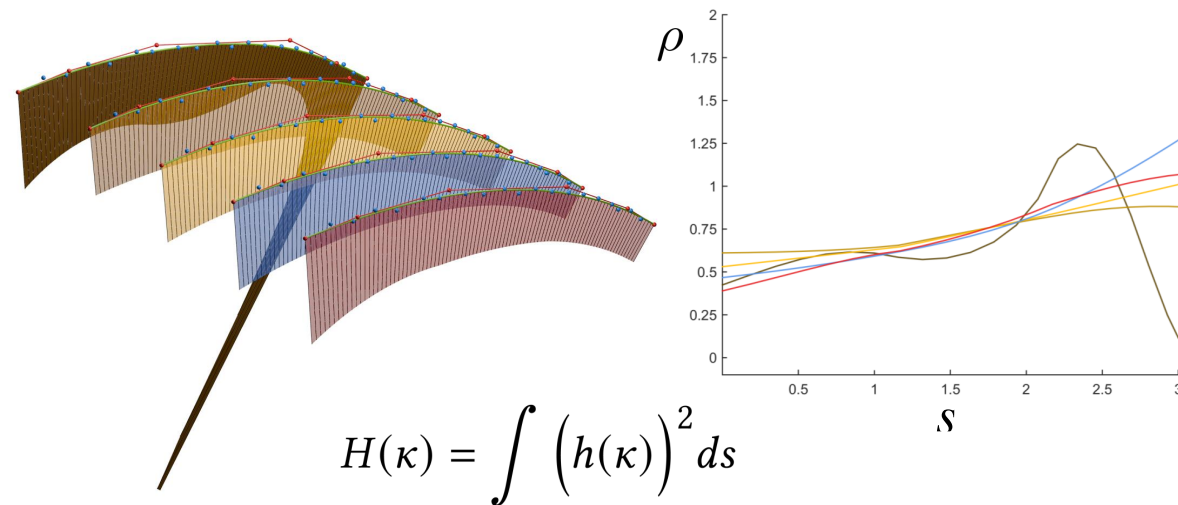
(b) Compounded curves

How to compute smooth curves effectively?

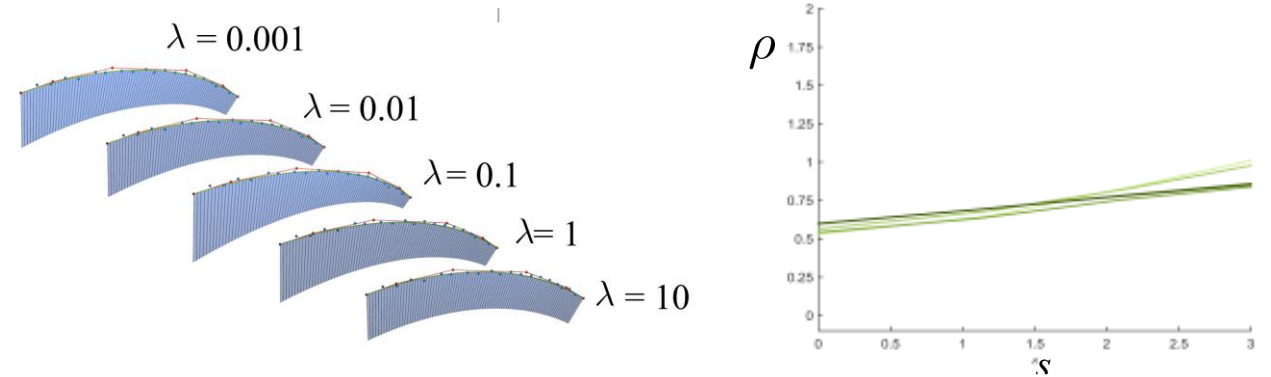
e.g. safe path planning in robots



Lesson 1. The fairness functional is key!

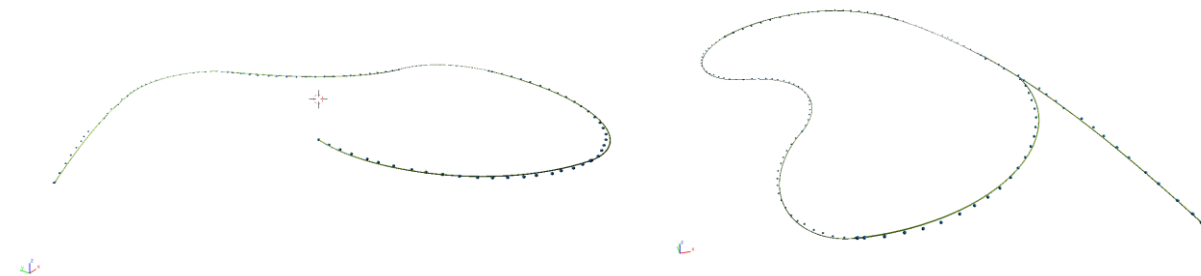


Lesson 2. The functional $h(\kappa) = \kappa''$ is robust...

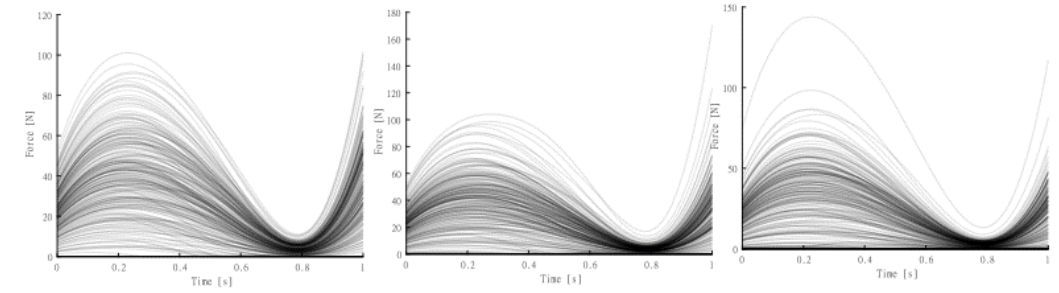
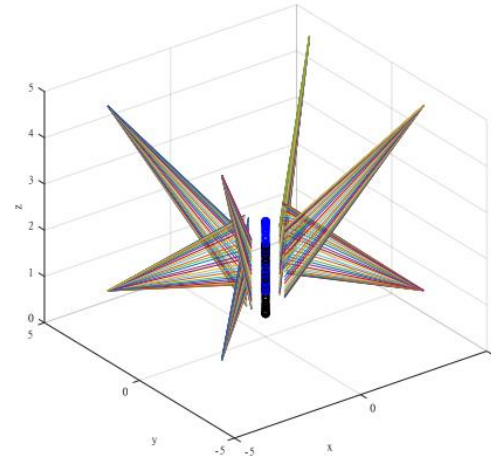
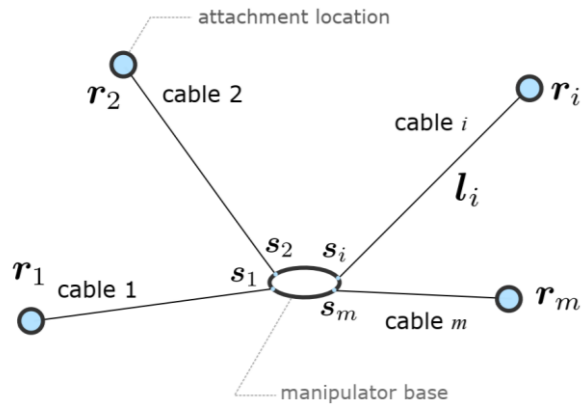


$$\min_{p_i} F = E + \lambda H$$

... to compute smooth curves efficiently!



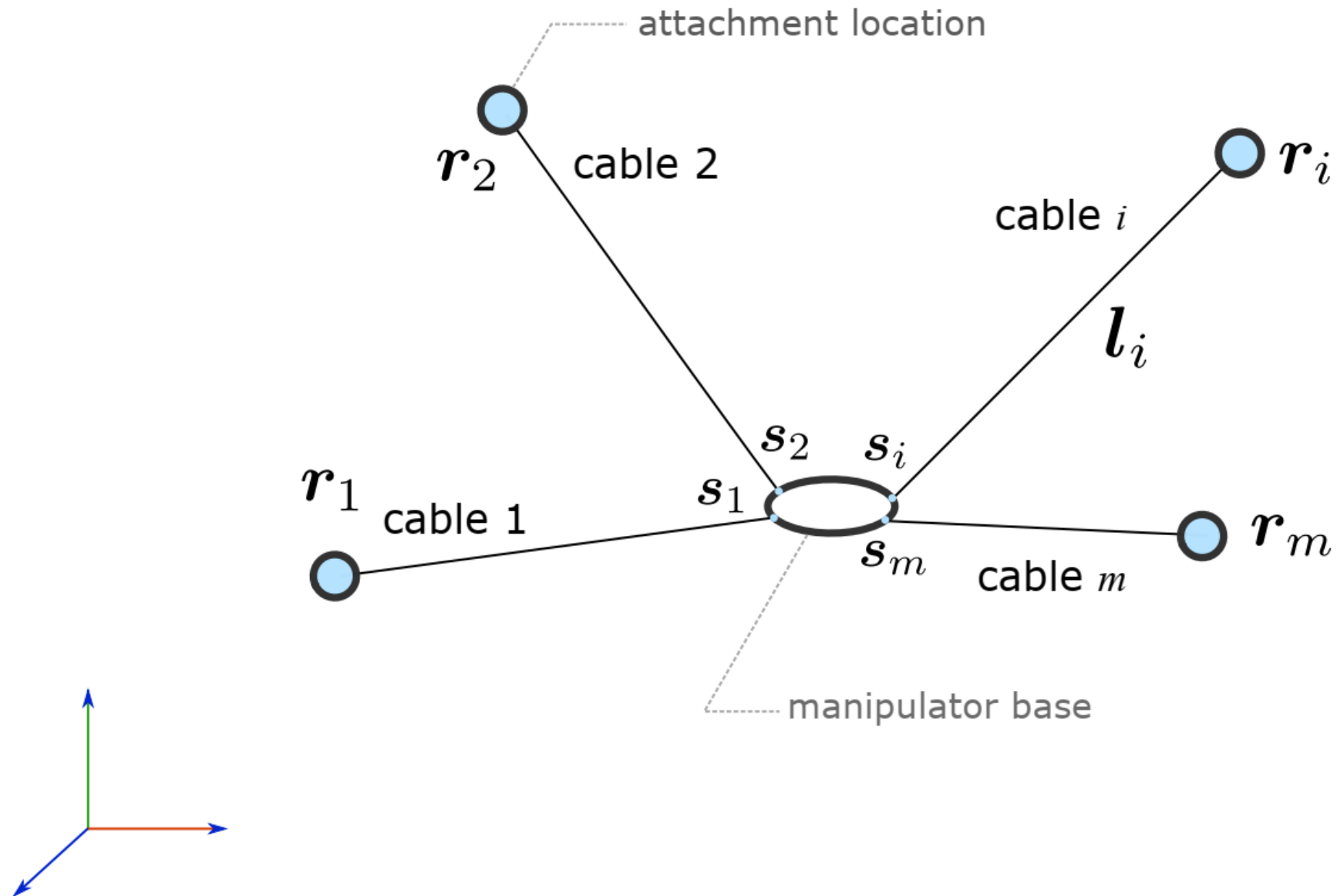
A Study of Fairness Functionals for Smooth Path Planning in Mobile Robots



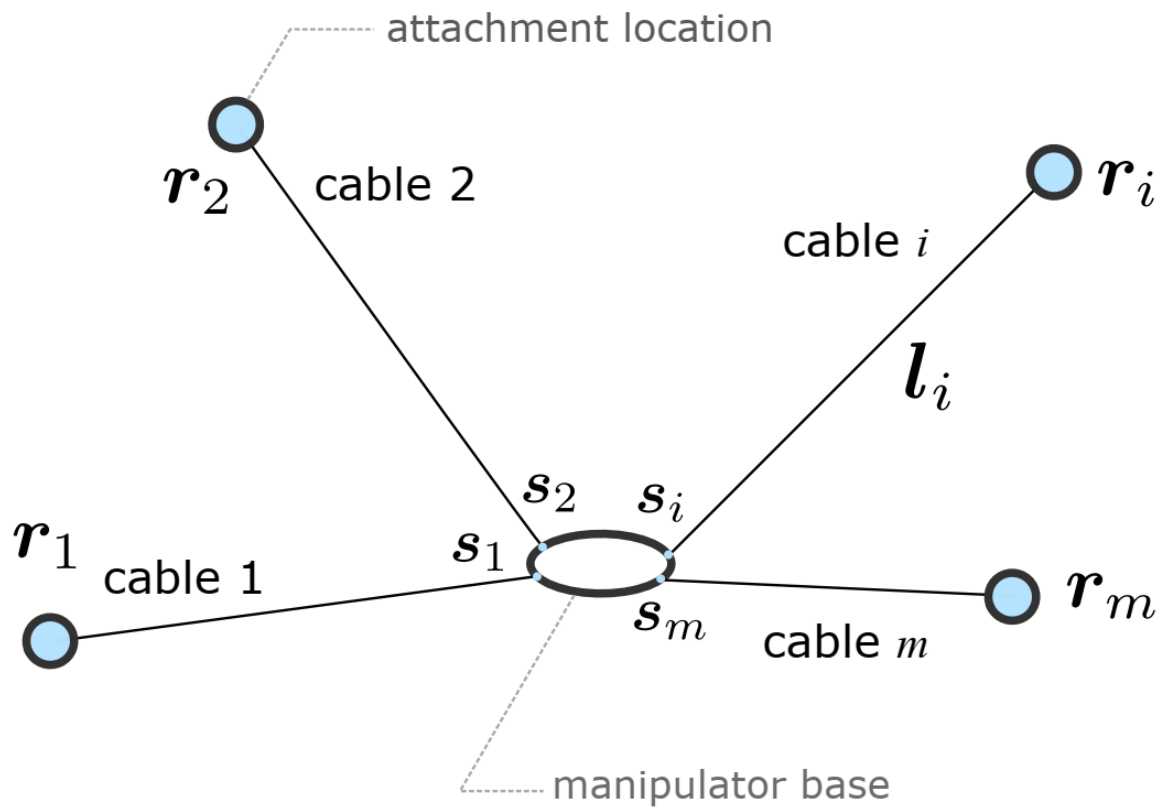
Optimal Design of Cable-Driven Parallel Robots by Particle Schemes

Victor Parque, Tomoyuki Miyashita

Cable-driven Parallel Robot



Cable-driven Parallel Robot



$$\dot{l} = L(q)\dot{q},$$

Cable lengths

Jacobian Matrix

Manipulator pose

$$M(q)\ddot{q} + C(\dot{q}, q) + G(q) + w_e = -L^T(q)f$$

Inertia Matrix

Centrifugal vector

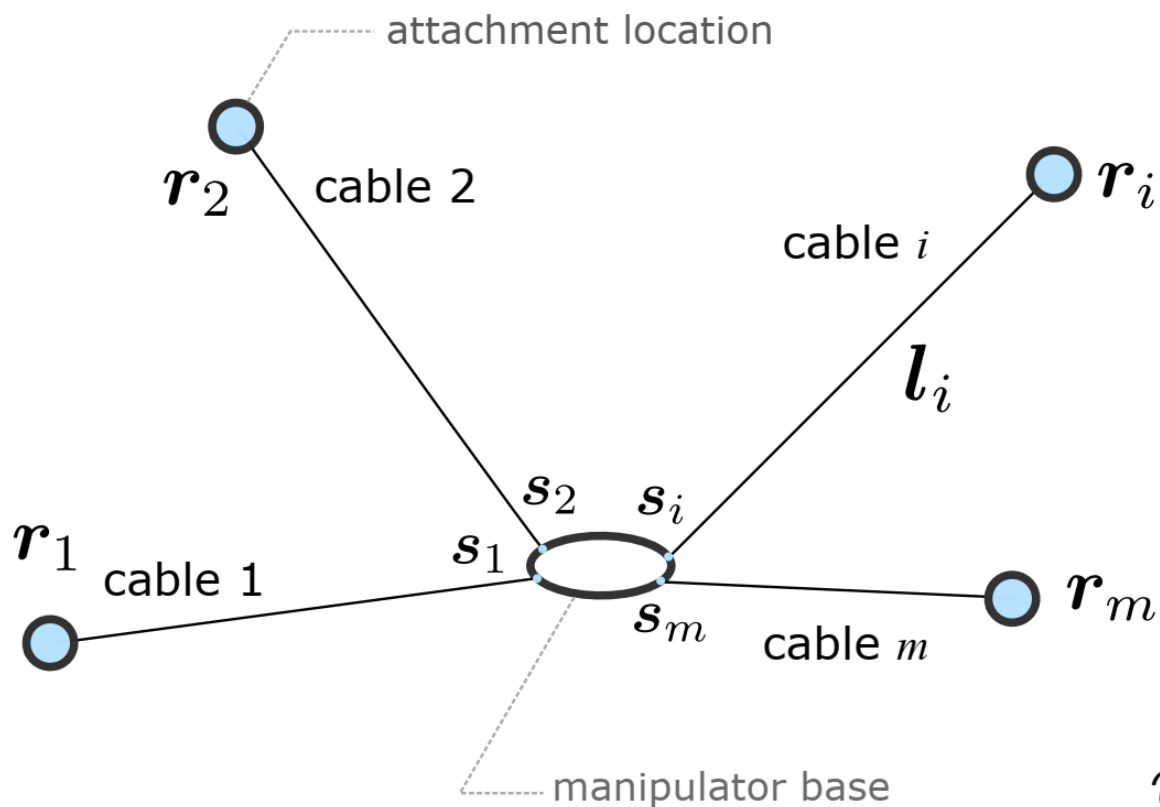
Gravity vector

External wrench

Cable Forces

$$0 \leq f_{\min} \leq f \leq f_{\max}$$

Tension Distribution Problem



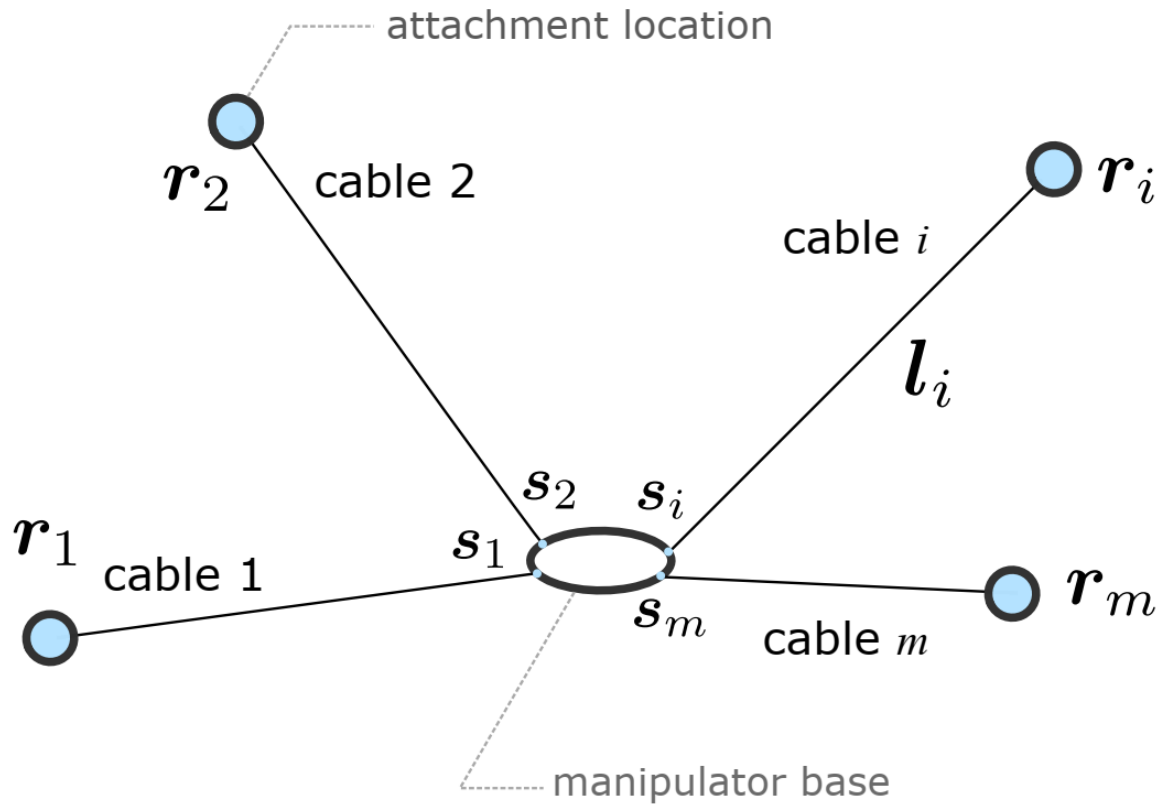
Find cable forces by solving:

$$\begin{aligned} &\underset{\mathbf{f}}{\text{Minimize}} \quad \frac{1}{2} \mathbf{f}^\top H \mathbf{f} \\ &\text{s.t.} \quad \mathbf{f} \in [\mathbf{f}_{\min}, \mathbf{f}_{\max}] \\ &\quad \quad -L^\top(\mathbf{q}) \mathbf{f} = \mathbf{w} \end{aligned}$$

$$\mathbf{w} = \overset{\text{Inertia Matrix}}{M(\mathbf{q})} \ddot{\mathbf{q}} + \overset{\text{Centrifugal vector}}{C(\dot{\mathbf{q}}, \mathbf{q})} + \overset{\text{Gravity vector}}{G(\mathbf{q})}$$

Trajectory tasks

Cable Configuration Problem



Find cable attachment locations by

$$\begin{aligned} &\text{Minimize}_{\mathbf{r}, \mathbf{s}} \sum_{t \in [0, t_{\max}]} \sum_{i=1}^m (f_i^{*2} + \lambda) \\ &\text{s.t. } \mathbf{r} \in \mathcal{R}, \mathbf{s} \in \mathcal{S} \end{aligned}$$

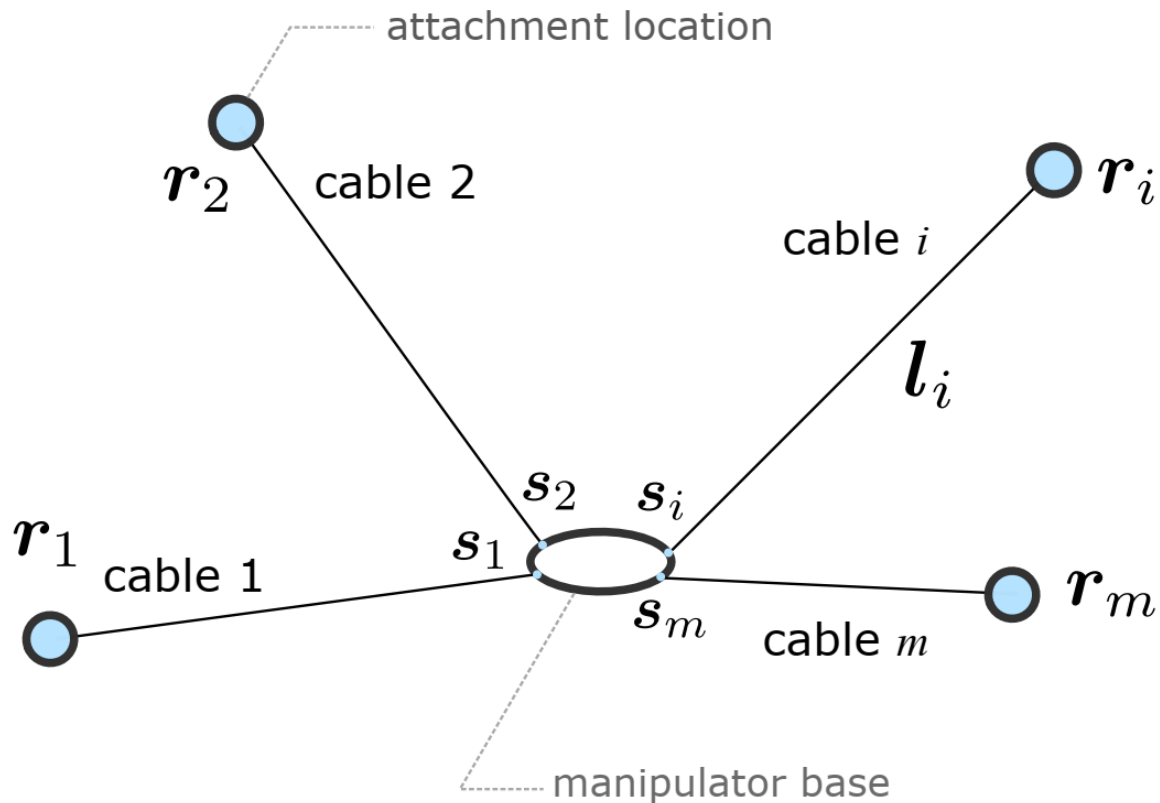
Number of cables m

Penalty for constraint violation λ

Optimal force in tension distribution problem f_i^*

Time in user-defined trajectory $t \in [0, t_{\max}]$

Cable Configuration Problem: Challenges



Geometry Methods



Intuitive, Principled



Specific to the robot architecture

Optimization Methods



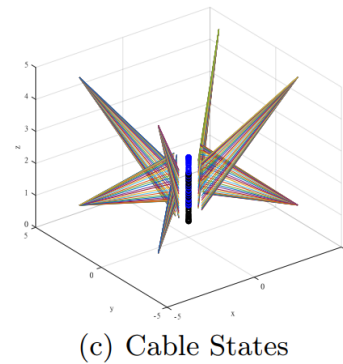
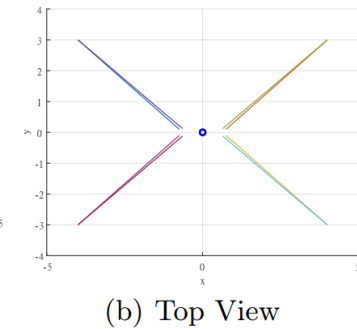
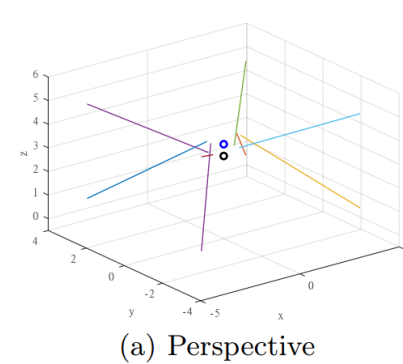
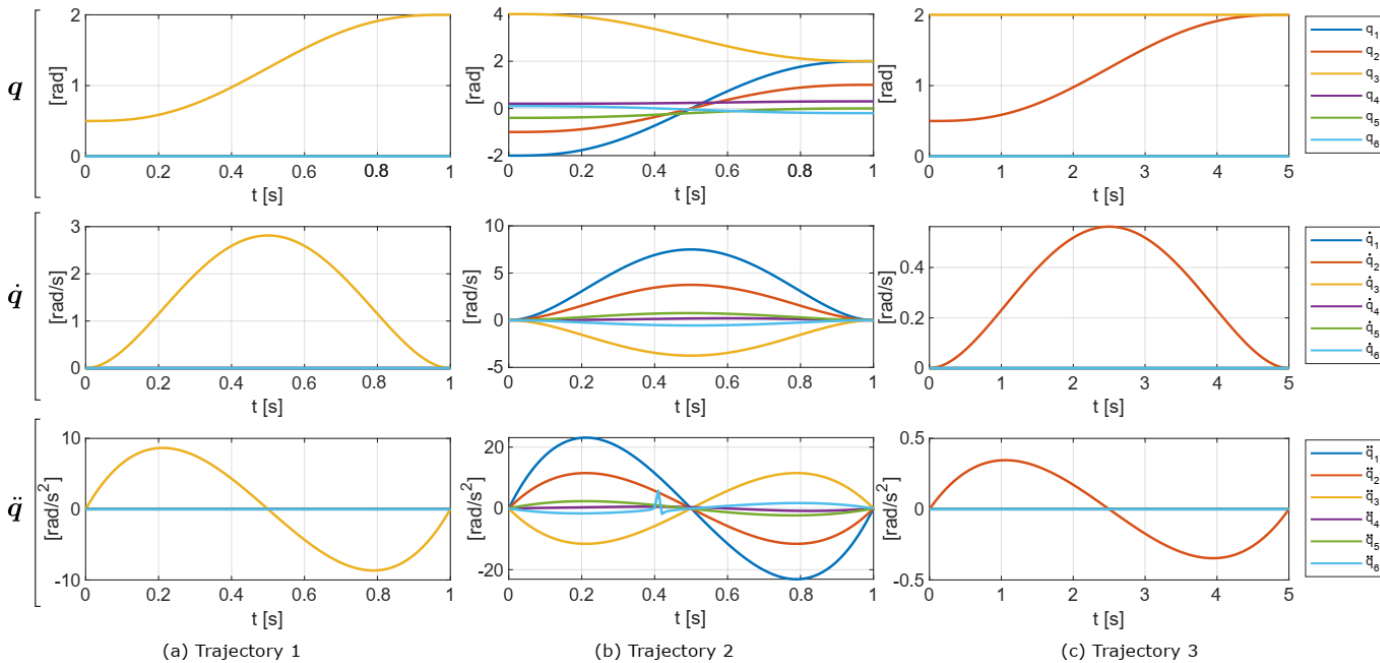
Applicable to various architectures



No design principles

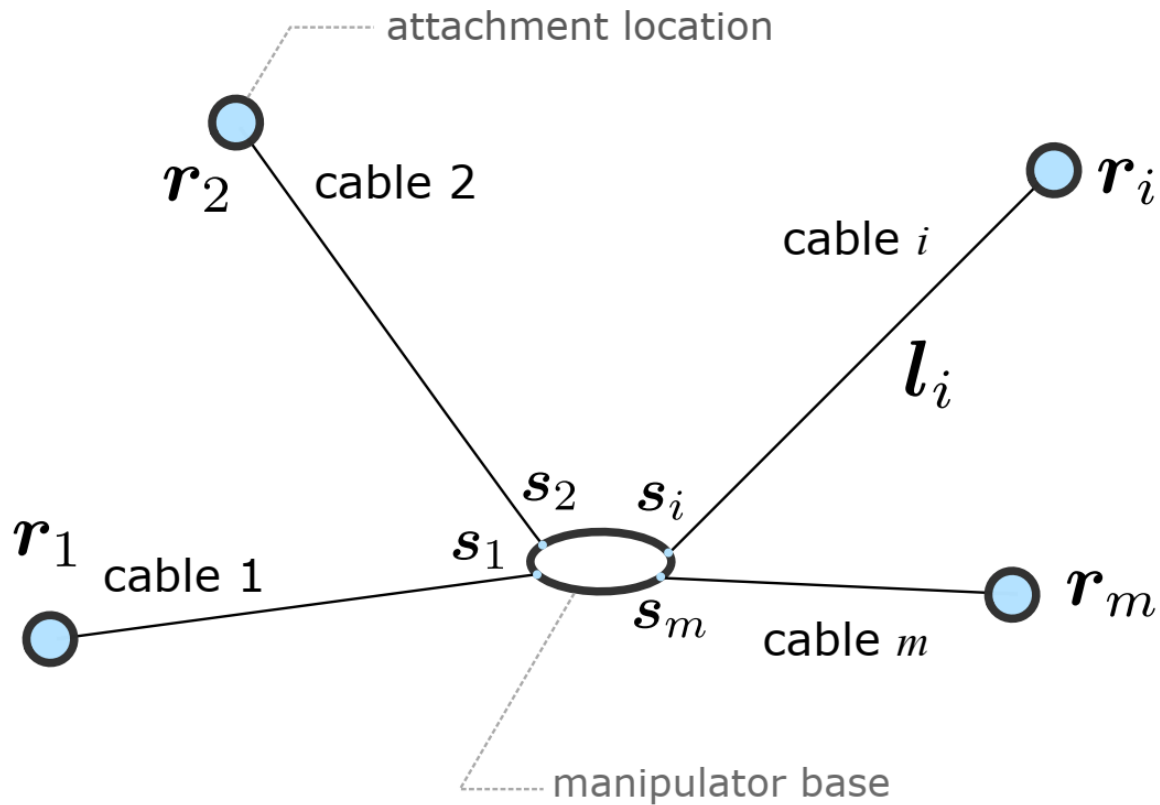
Cable Configuration Problem: 8 cables, 6DOF

Trajectory tasks



Pott et al, **IPAnema**: A family of Cable-Driven Parallel Robots for Industrial Applications, 2013

Cable Configuration Problem



Find cable attachment locations by

$$\begin{aligned} &\text{Minimize}_{\mathbf{r}, \mathbf{s}} \sum_{t \in [0, t_{\max}]} \sum_{i=1}^m (f_i^{*2} + \lambda) \\ &\text{s.t. } \mathbf{r} \in \mathcal{R}, \mathbf{s} \in \mathcal{S} \end{aligned}$$

Annotations for the equation:

- $\sum_{t \in [0, t_{\max}]}$: Time in user-defined trajectory
- $\sum_{i=1}^m$: Number of cables
- f_i^{*2} : Optimal force in tension distribution problem
- λ : Penalty for constraint violation

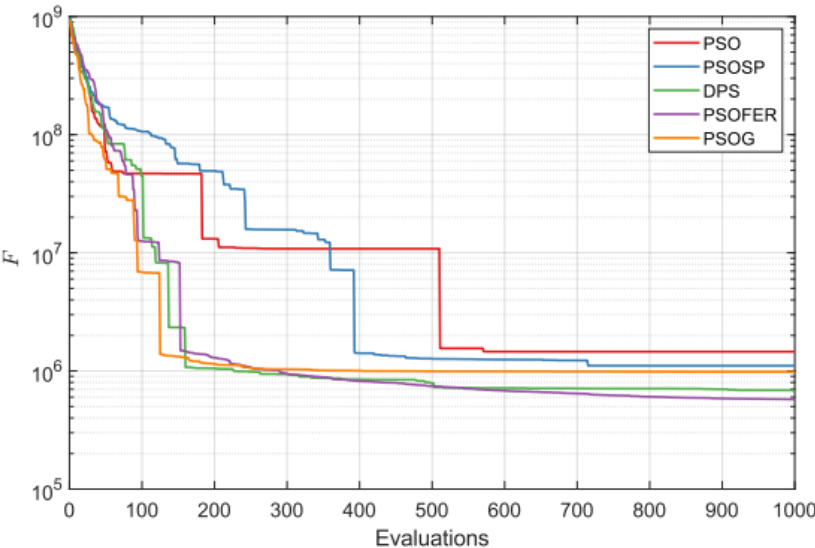
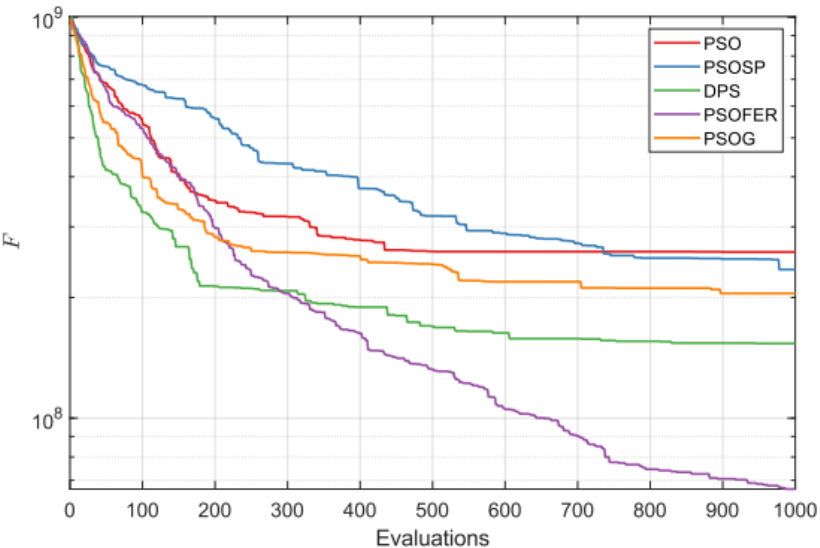
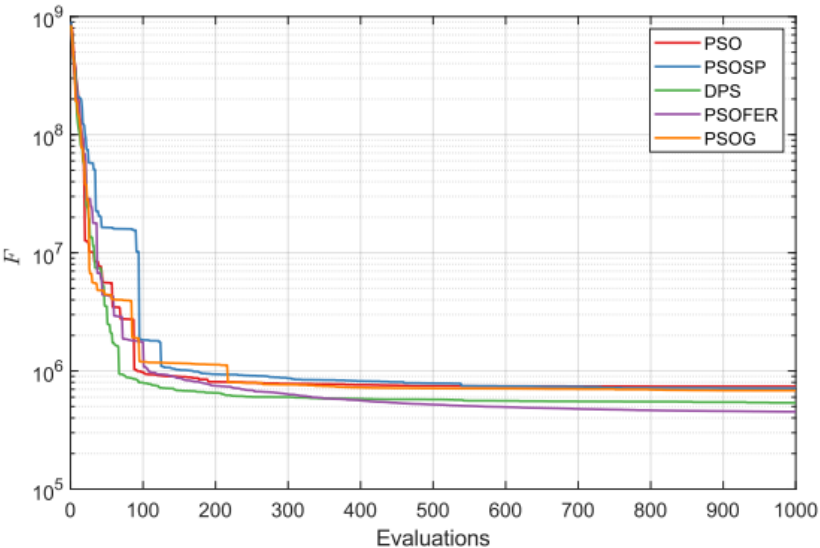
Non-linear Problem: We compare several Particle Swarm Heuristics

Cable Configuration Problem: Particle Schemes

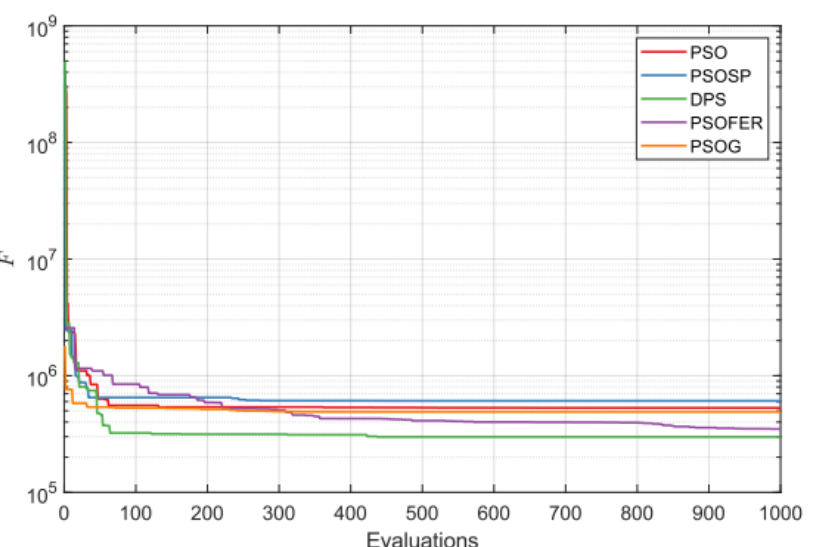
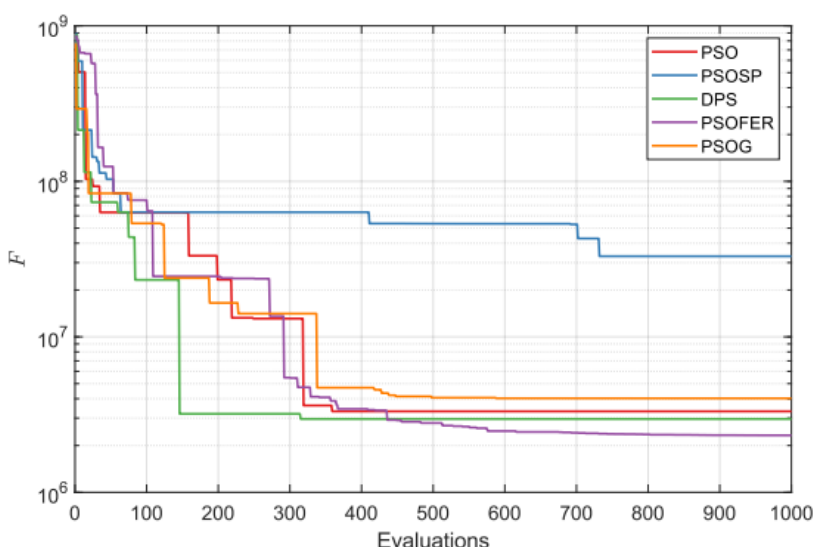
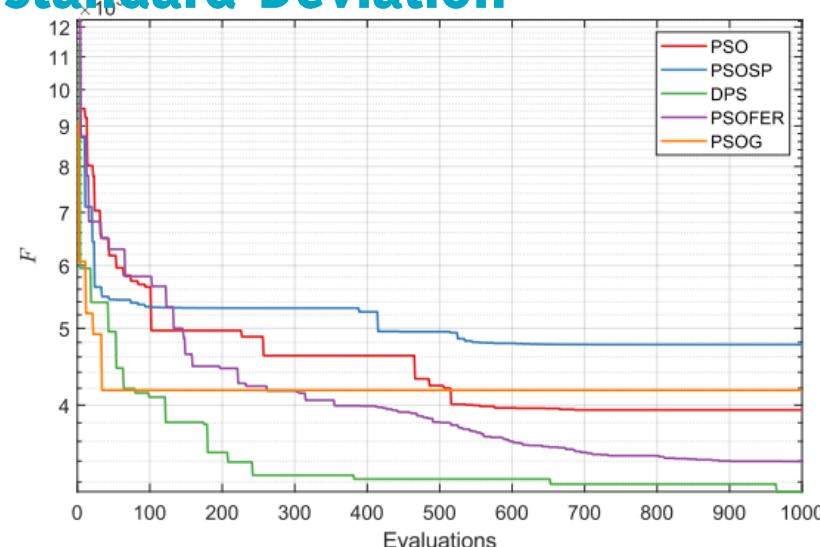
- Particle Swarm Optimization (PSO)
- Particle Swarm with **Speciation** (PSOSP)
- **Differential Particle** Scheme (DPS)
- Particle Swarm **with Fitness Euclidean Ratio**(PSOFER)
- Particle Swarm Optimization with **Global Explorative Strategy**(PSOG)

1000 function evaluations, 30 independent runs

Mean Convergence



Standard Deviation



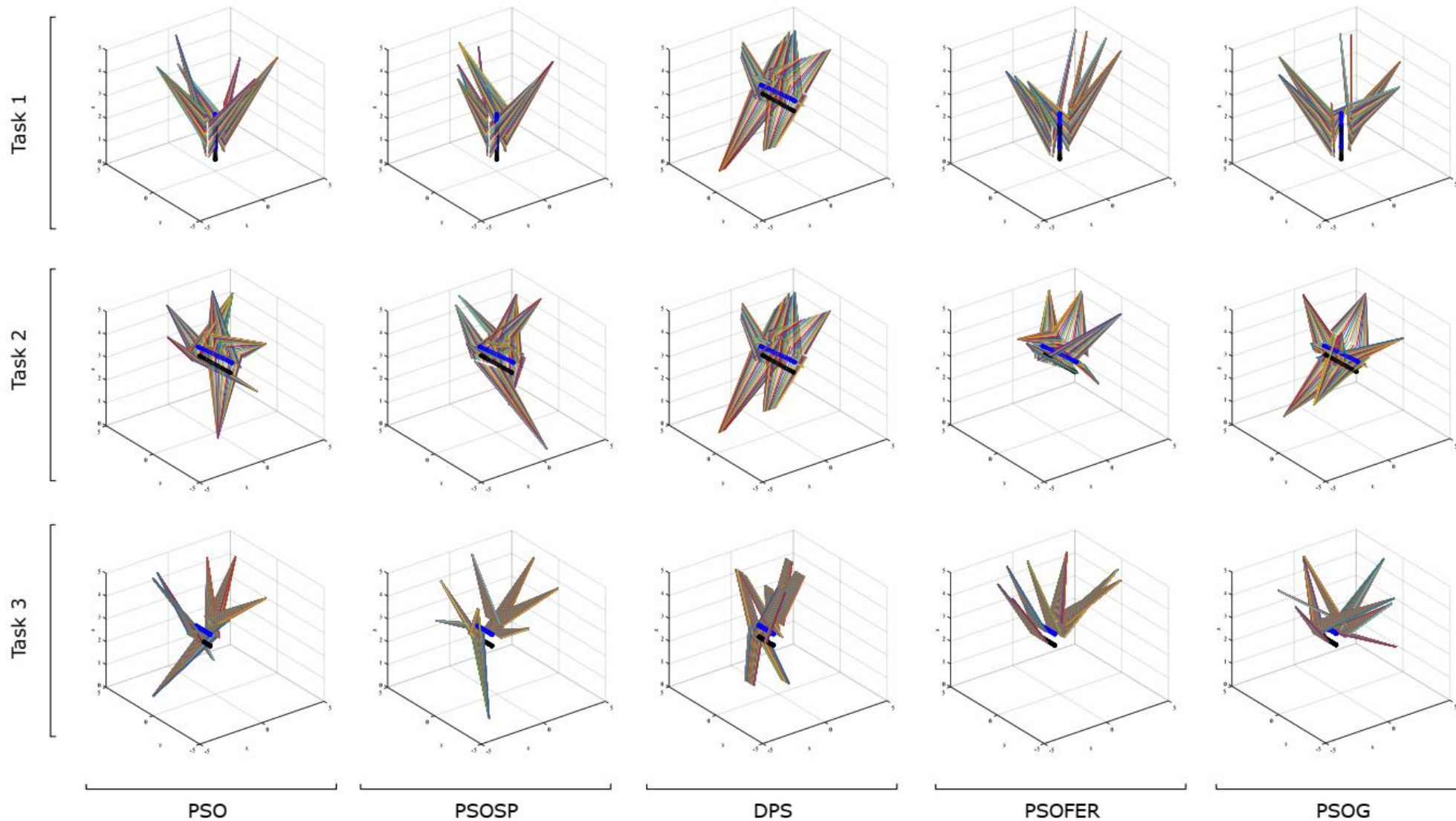
(a) Task 1

(b) Task 2

(c) Task 3

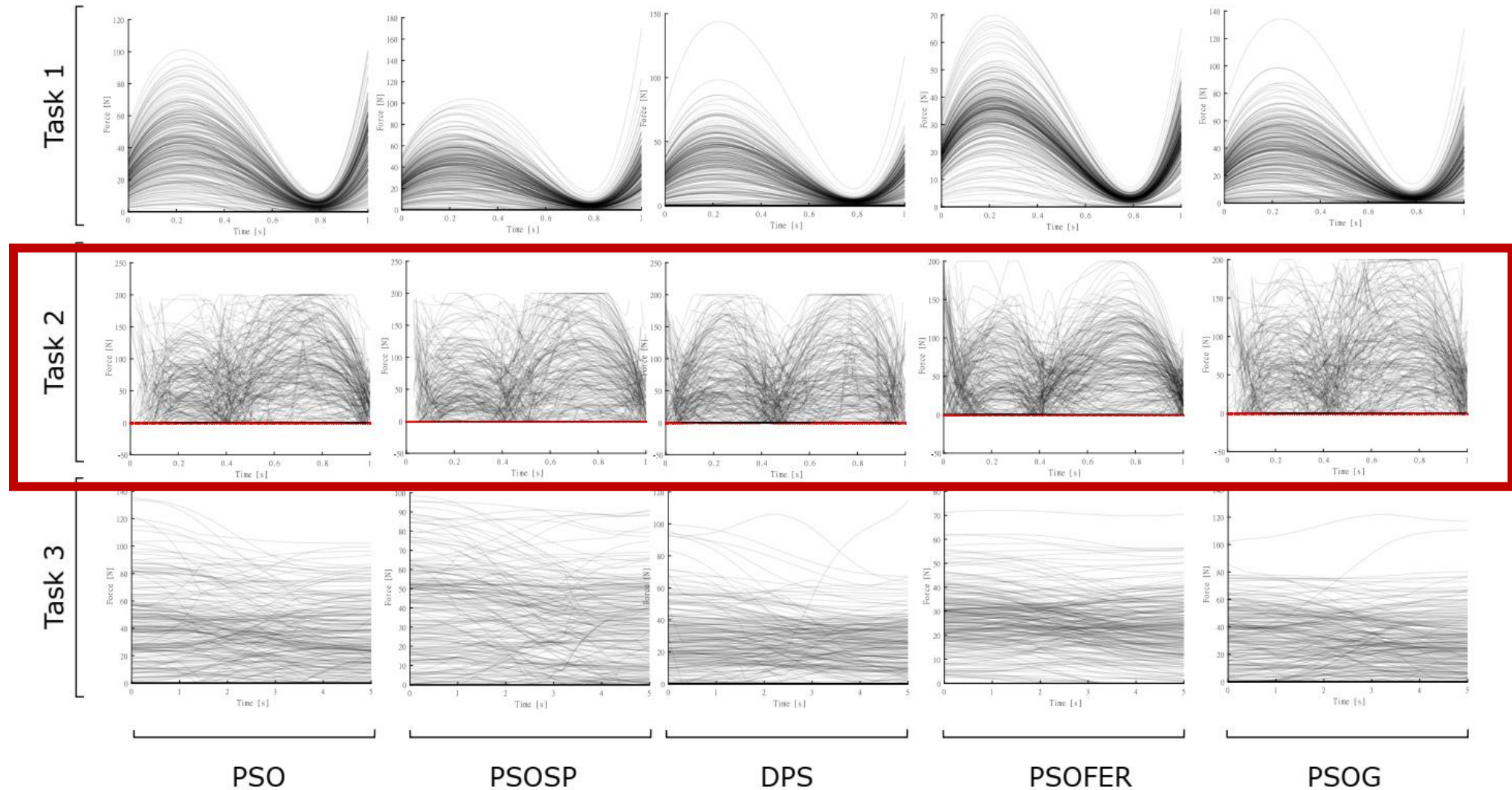
PSOFR and DPS converge faster in 200 - 800 evaluations

Cable Configuration Problem – Best Configurations (out of 30 runs)



Each algorithm converges to distinct configurations

Force Distribution Problem – Solutions over 30 runs



Solutions to the tension problem are not always smooth

Statistical Comparison – Solutions over 30 runs

	PSO	PSOSP	DPS	PSOFER	PSOG
PSO		[=] 1.12e-01	[-] 2.15e-06	[-] 6.52e-09	[=] 7.98e-02
PSOSP	[=] 1.12e-01		[-] 1.04e-04	[-] 2.92e-09	[=] 6.41e-01
DPS	[+] 2.15e-06	[+] 1.04e-04		[-] 2.92e-02	[+] 8.12e-04
PSOFER	[+] 6.52e-09	[+] 2.92e-09	[+] 2.92e-02		[+] 2.60e-08
PSOG	[=] 7.98e-02	[=] 6.41e-01	[-] 8.12e-04	[-] 2.60e-08	

(a) Task 1

	PSO	PSOSP	DPS	PSOFER	PSOG
PSO		[=] 5.01e-01	[-] 7.96e-03	[-] 2.78e-07	[=] 1.62e-01
PSOSP	[=] 5.01e-01		[-] 1.99e-02	[-] 3.01e-07	[=] 4.46e-01
DPS	[+] 7.96e-03	[+] 1.99e-02		[-] 1.24e-03	[=] 1.54e-01
PSOFER	[+] 2.78e-07	[+] 3.01e-07	[+] 1.24e-03		[+] 5.27e-06
PSOG	[=] 1.62e-01	[=] 4.46e-01	[=] 1.54e-01	[-] 5.27e-06	

(b) Task 2

	PSO	PSOSP	DPS	PSOFER	PSOG
PSO		[-] 2.24e-02	[-] 4.11e-07	[-] 3.82e-09	[-] 6.55e-04
PSOSP	[+] 2.24e-02		[-] 1.09e-05	[-] 2.19e-08	[=] 2.12e-01
DPS	[+] 4.11e-07	[+] 1.09e-05		[=] 5.01e-01	[+] 2.39e-04
PSOFER	[+] 3.82e-09	[+] 2.19e-08	[=] 5.01e-01		[+] 6.05e-07
PSOG	[+] 6.55e-04	[=] 2.12e-01	[-] 2.39e-04	[-] 6.05e-07	

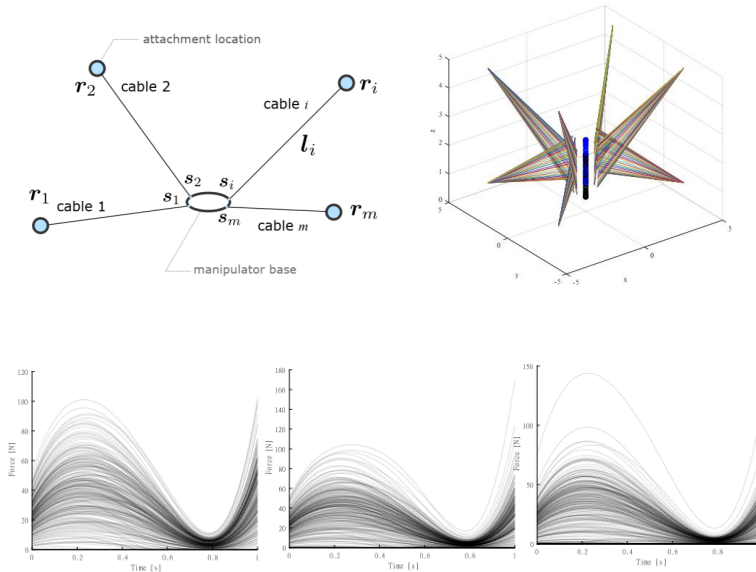
(c) Task 3

PSOFER (niching) and DPS (stagnation avoidance) outperform other optimization algorithms

Conclusion

Final Notes

Results



We tackle the **configuration problem** in cable-driven parallel robots.



Cable configuration problems are solvable quite **efficiently (10^3 evaluations)**, but force solutions are not always smooth.



Strategies for **niching** and **stagnation** avoidance outperform other heuristics.

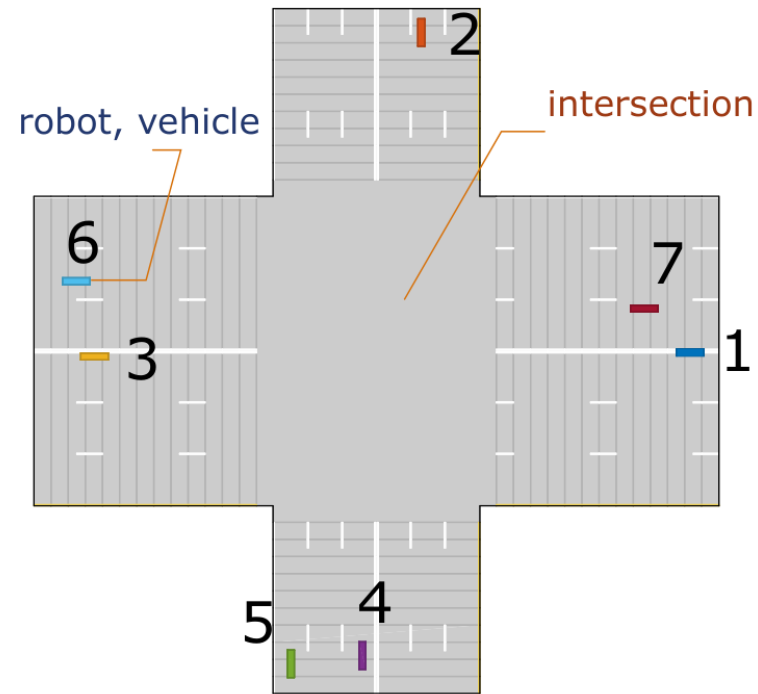
Future Work



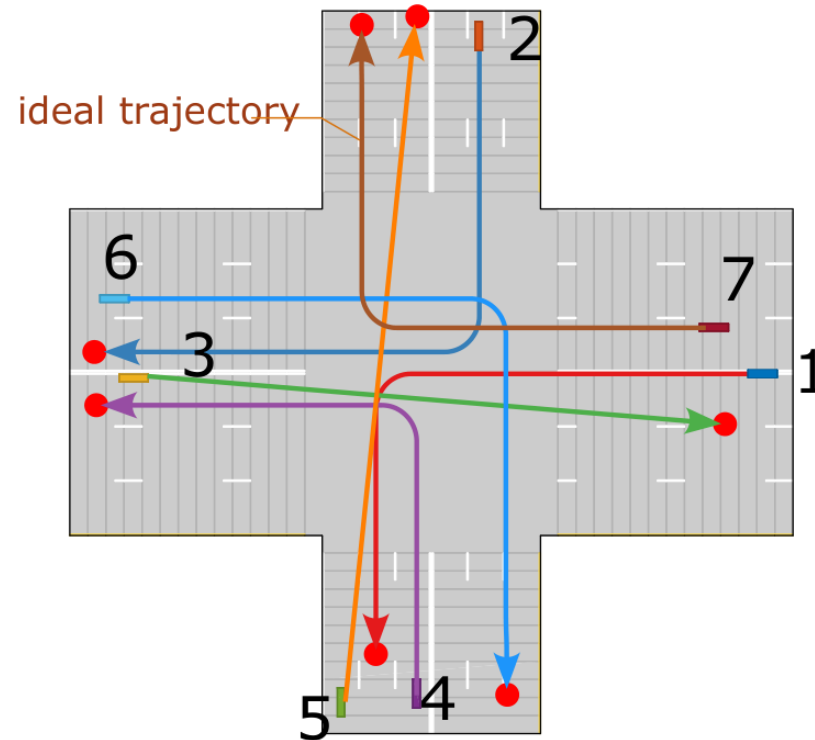
Applications: Robot Leg (Cable-driven), Arm Exoskeleton, Manipulation

A Hybrid Evolutionary Approach for Multi Robot Coordinated Planning at Intersections

Background



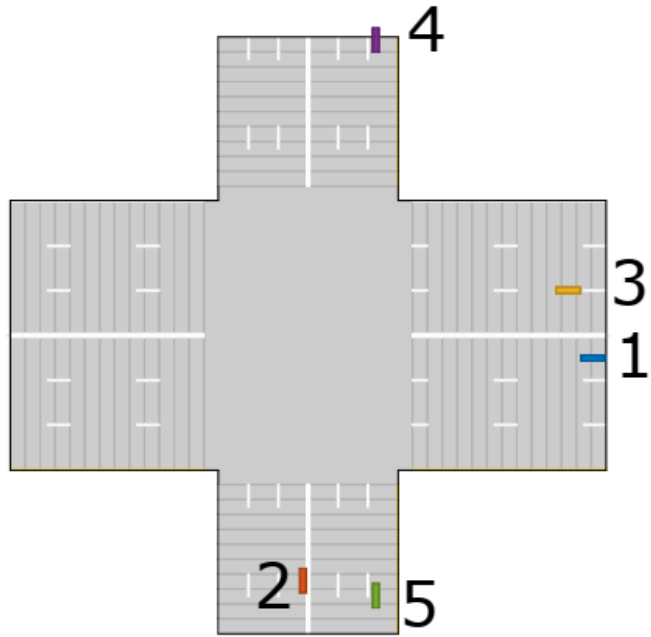
Vehicles at Intersections



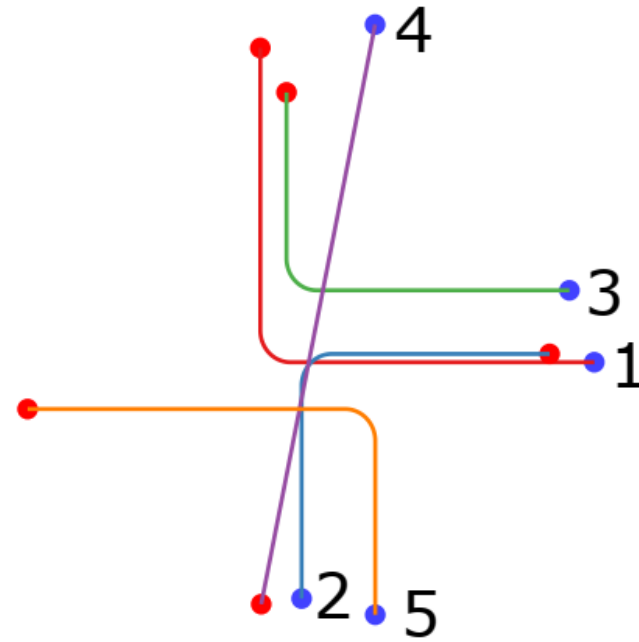
Desirable Trajectories, and Kinematic Constraints

How to plan at intersections?

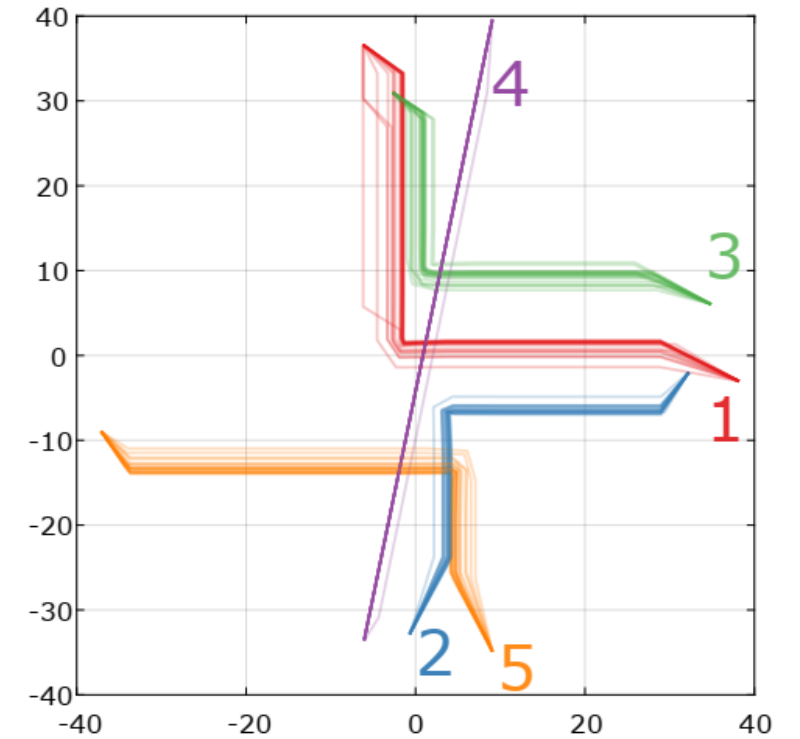
Background



Robots at intersections

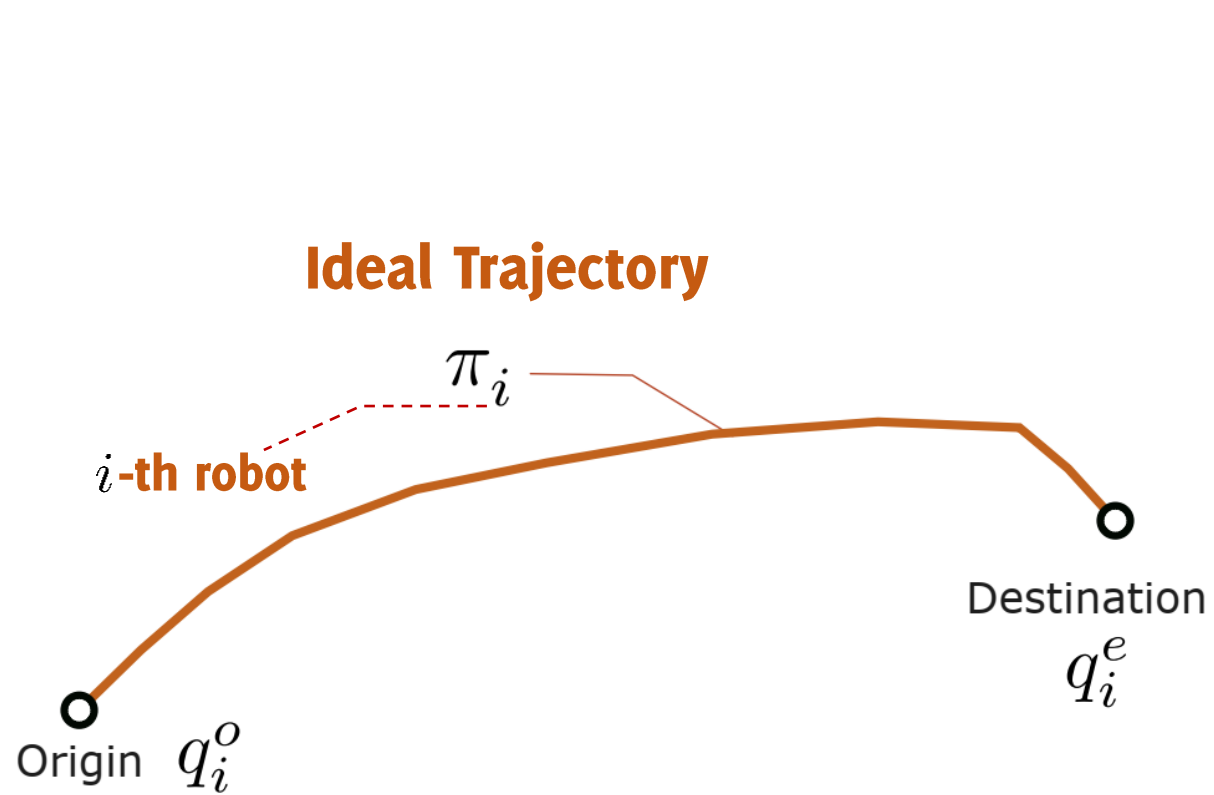


Ideal trajectories
Origin - Destination

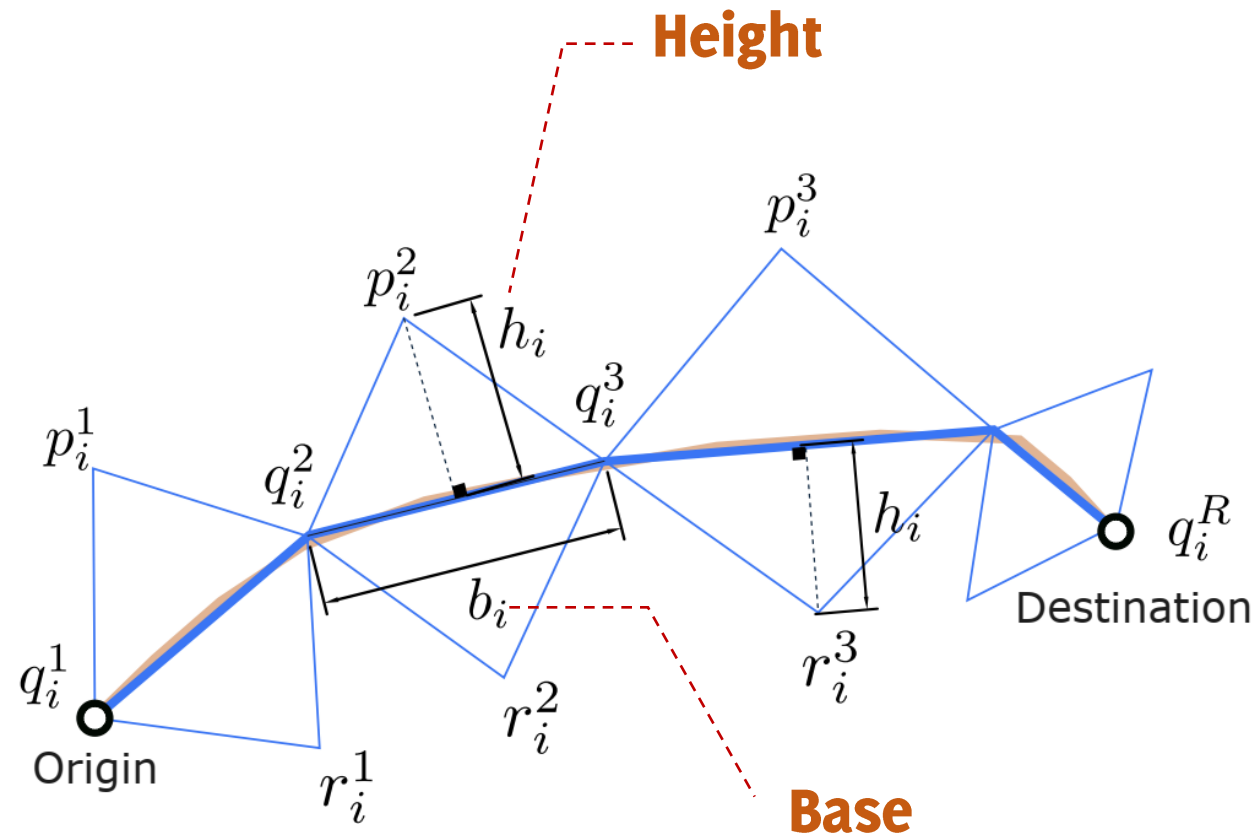


Coordinated trajectory planning

Lattice Configuration



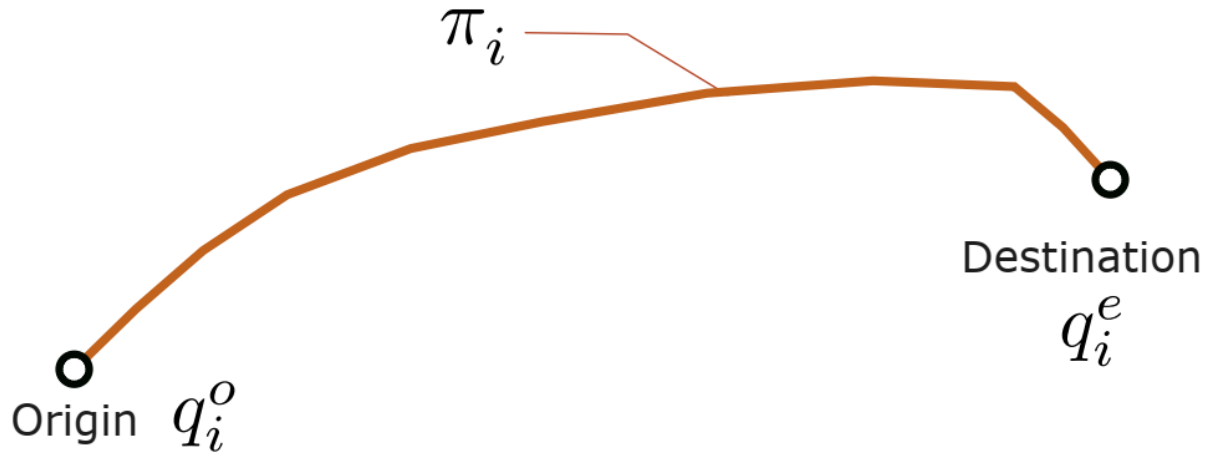
Origin - Destination



Triangulation

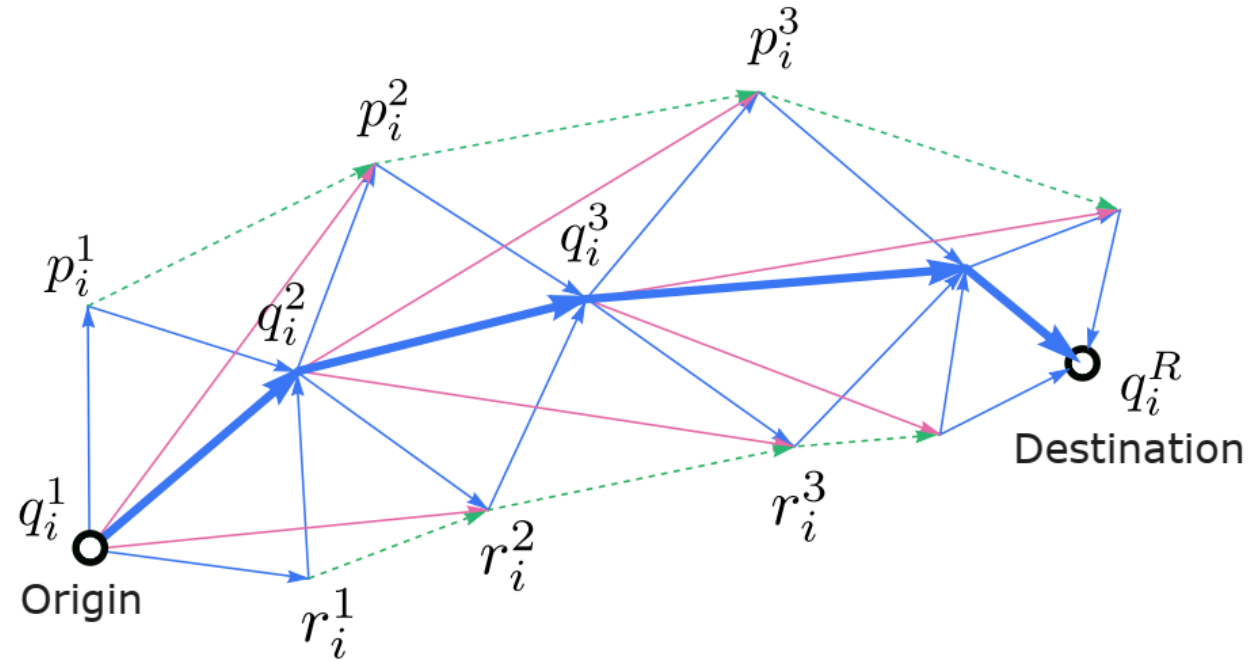
Lattice Configuration

Ideal Trajectory



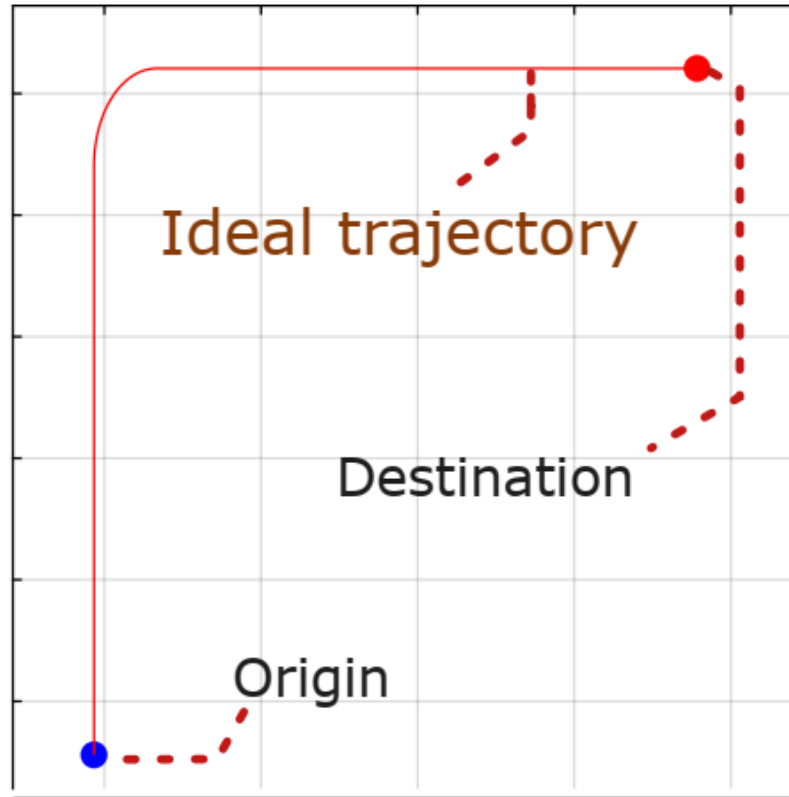
Origin - Destination

Directed Graph $G_i = (V_i, E_i)$

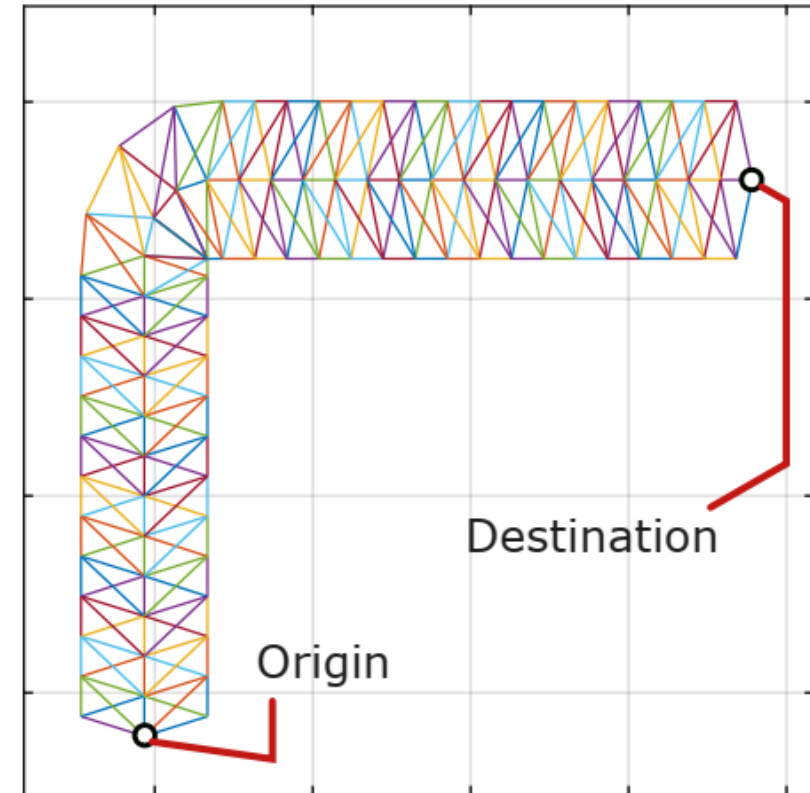


Triangulation

Lattice Configuration - Example

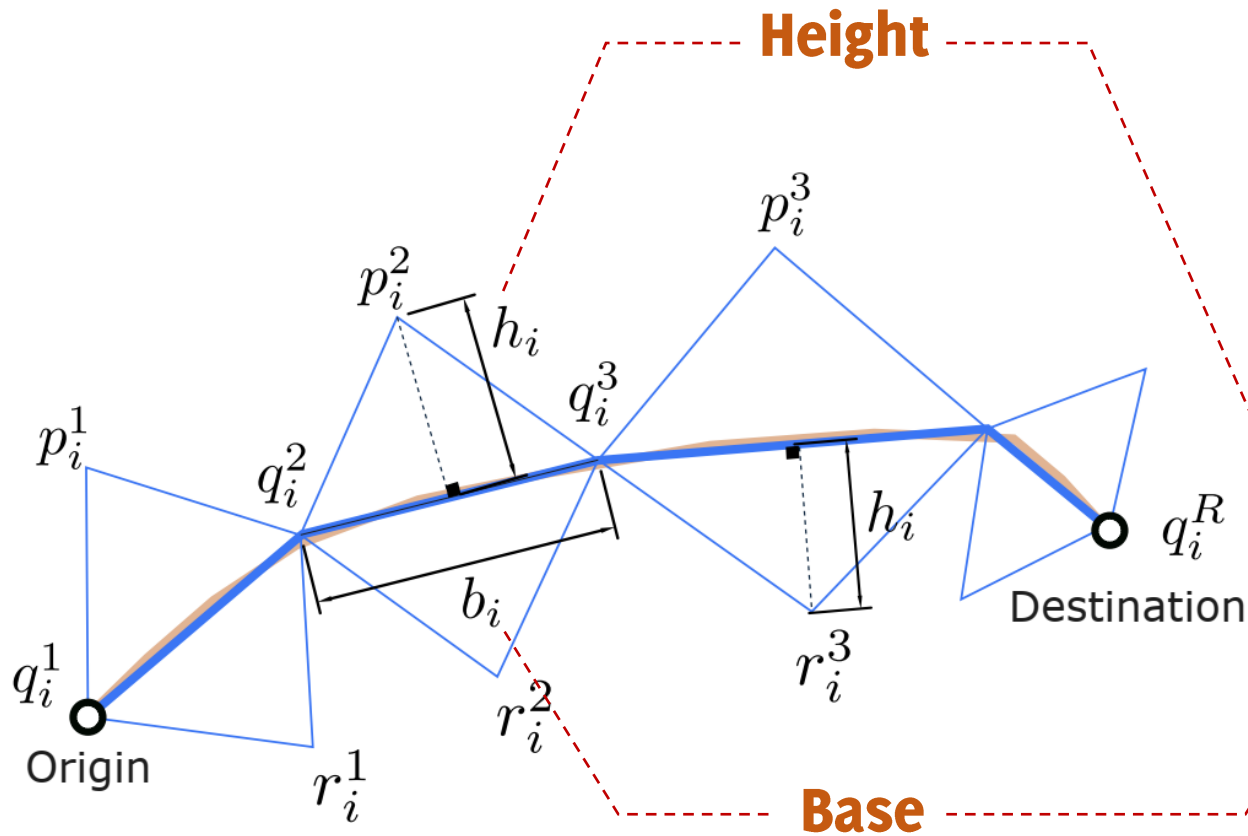


Origin - Destination



Triangulation

Multi-Robot Coordinated Path Planning



Lattice-based Roadmap

Minimize $\sum_{i=1}^N L(P_i)$ subject to $P_i \subset E_i, i = 1, \dots, N.$

$x = (b_i, h_i)_{i \in \{1, \dots, N\}}$

Annotations: #Robots N , Length of path $L(P_i)$, dRRT* shortest path, Roadmap (triangulation) E_i .

Gradient-Free Optimization

RADES: Rank-Based Differential Evolution with Successful Archive

Solution vector

$$\mathbf{x}_{i,t+1} = \begin{cases} \mathbf{u}_{i,t}, & \text{for } f(\mathbf{u}_{i,t}) < f(\mathbf{x}_{i,t}) \\ \mathbf{x}_{i,t}, & \text{otherwise} \end{cases}$$

Objective function

Reference vector

Crossover vector (binary)

$$\mathbf{u}_{i,t} = \mathbf{x}_{i,t}^r + \mathbf{b}_{i,t} \circ (\mathbf{v}_{i,t} - \mathbf{x}_{i,t}^r)$$

Stagnation counter

$$\mathbf{x}_{i,t}^r = \begin{cases} \mathbf{x}_{i,t}, & q_i \leq Q \\ \mathcal{A}_{i,t}, & \text{otherwise} \end{cases}$$

Archive

Scalar

$$\mathbf{v}_{i,t} = \begin{cases} \mathbf{x}_{\text{best}} + F(\mathbf{x}_{r_1} - \mathbf{x}_{r_2}), & q_i \leq Q \\ \mathcal{A}_{\text{best}} + F(\mathcal{A}_{r_1} - \mathcal{A}_{r_2}), & \text{otherwise} \end{cases}$$

Whitley Distribution

$$r_{1,2} = \left\lfloor \frac{|\mathcal{P}|}{2\beta - 1} \left(\beta - \sqrt{\beta^2 - 4(\beta - 1)r} \right) \right\rfloor$$

$Q = 128 \quad F = 0.7 \quad \beta = 2$

Algorithm 1: RADES

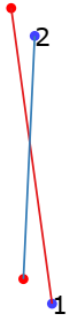
```

1   $FES = 0, t = 0, q_i = 0;$ 
2  Generate a set of  $N$  individuals randomly as initial
    population set  $\mathcal{P}$ ;
3  Initialize the archive  $\mathcal{A}$  from the population set  $\mathcal{P}$ ;
4  Initialize the  $F$  and  $CR$ ;
5   $FES = FES + N$ ;
6  while  $FES \leq MaxFES$  do
7       $t = t + 1$ ;
8      Find out the best individual  $\mathbf{x}_{\text{best}}$  and  $\mathcal{A}_{\text{best}}$  from
        the population and the archive  $\mathcal{A}$  respectively;
9      for  $i = 1$  to  $NP$  do
10         Generate  $r_1$  and  $r_2$  using (10);
11         Generate the mutant vector  $\mathbf{v}_{i,t}$ 
12         Generate the trial vector  $\mathbf{u}_{i,t}$ 
13         if  $f(\mathbf{u}_{i,t}) < f(\mathbf{x}_{i,t})$  then
14              $\mathbf{x}_{i,t+1} = \mathbf{u}_{i,t}$ ;
15              $\mathbf{u}_{i,t} \rightarrow \mathcal{A}$ ;
16             Delete an element from  $\mathcal{A}$  if  $|\mathcal{A}| > |\mathcal{P}|$ ;
17              $q_i = 0$ ;
18         else
19              $\mathbf{x}_{i,t+1} = \mathbf{x}_{i,t}$ ;
20              $q_i = q_i + 1$ ;
21         end
22          $FES = FES + 1$ ;
23     end
24 end

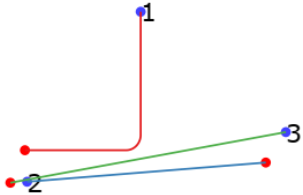
```

Computational Experiments

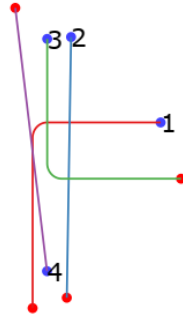
Instance 1, 2 robots



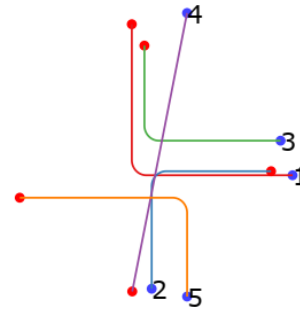
Instance 2, 3 robots



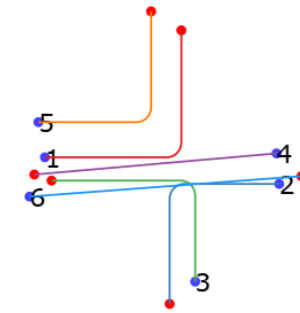
Instance 3, 4 robots



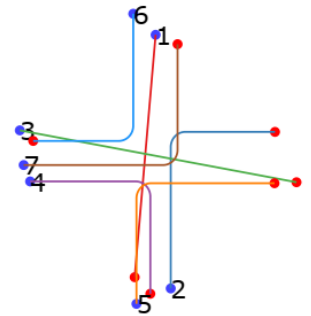
Instance 4, 5 robots



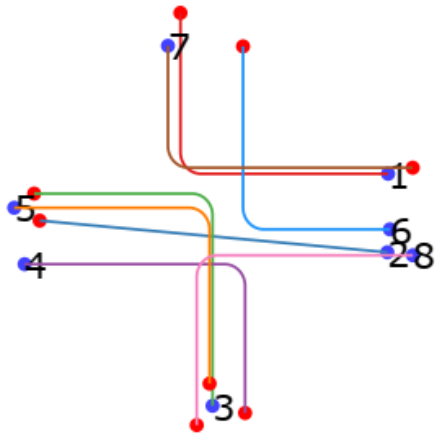
Instance 5, 6 robots



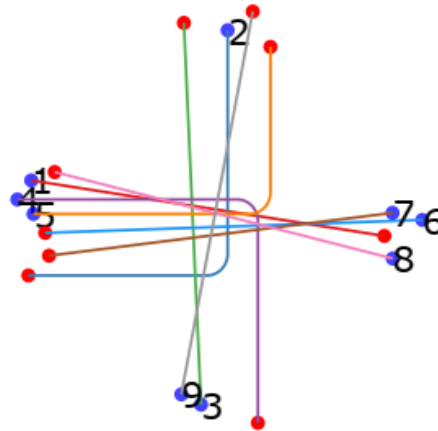
Instance 6, 7 robots



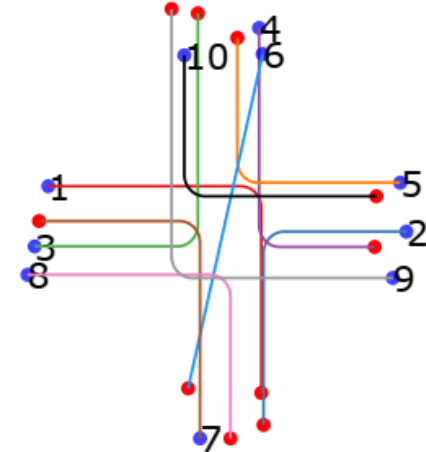
Instance 7, 8 robots



Instance 8, 9 robots



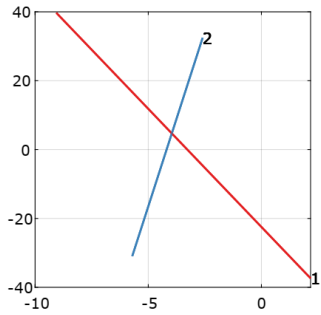
Instance 9, 10 robots



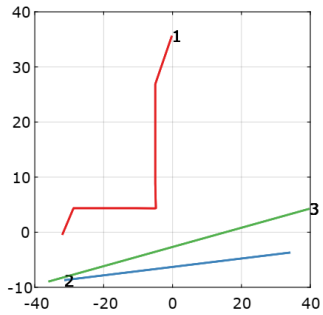
10 scenarios, diverse origin-destination and configurations

Computational Experiments

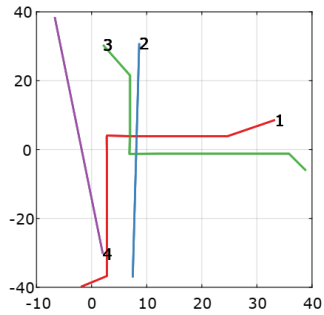
Instance 1



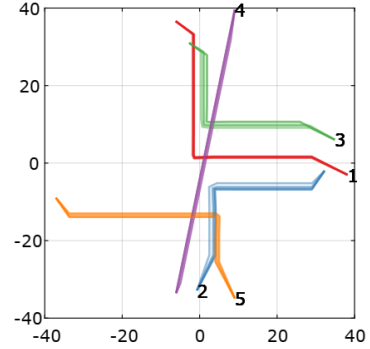
Instance 2



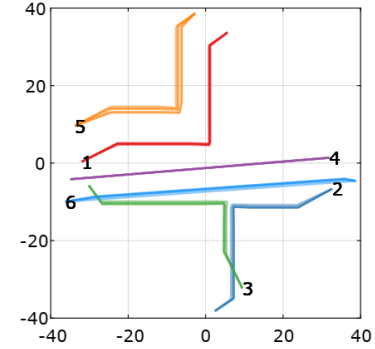
Instance 3



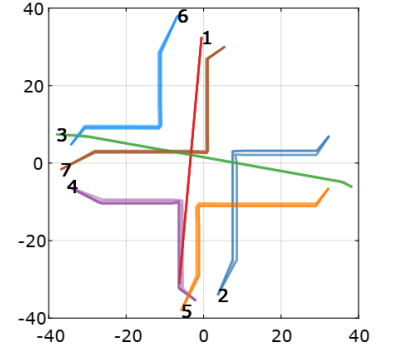
Instance 4



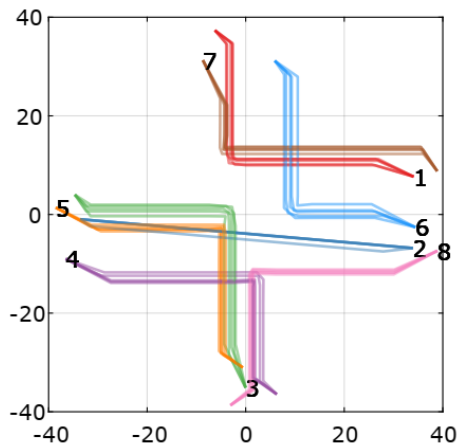
Instance 5



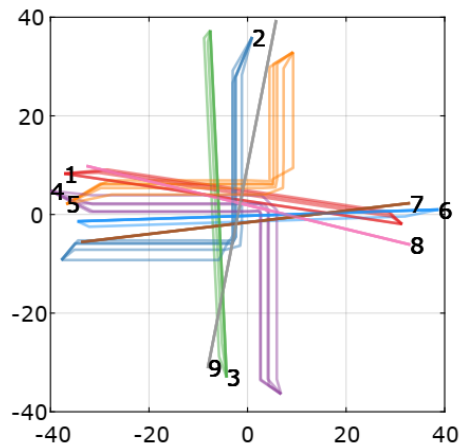
Instance 6



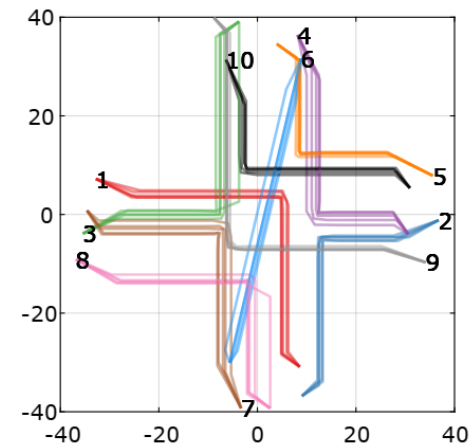
Instance 7



Instance 8

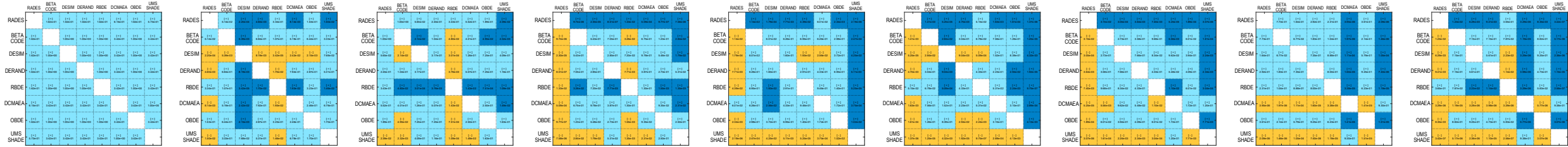


Instance 9



It is possible to compute feasible collision-free multi-robot trajectories

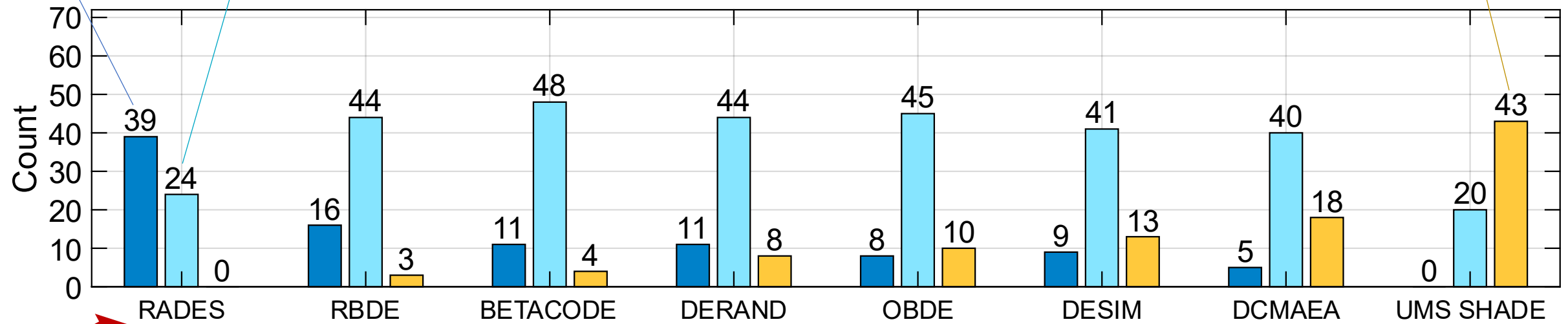
Statistical Comparisons



Number of cases of **outperformance**

Number of cases of **equal outperformance**

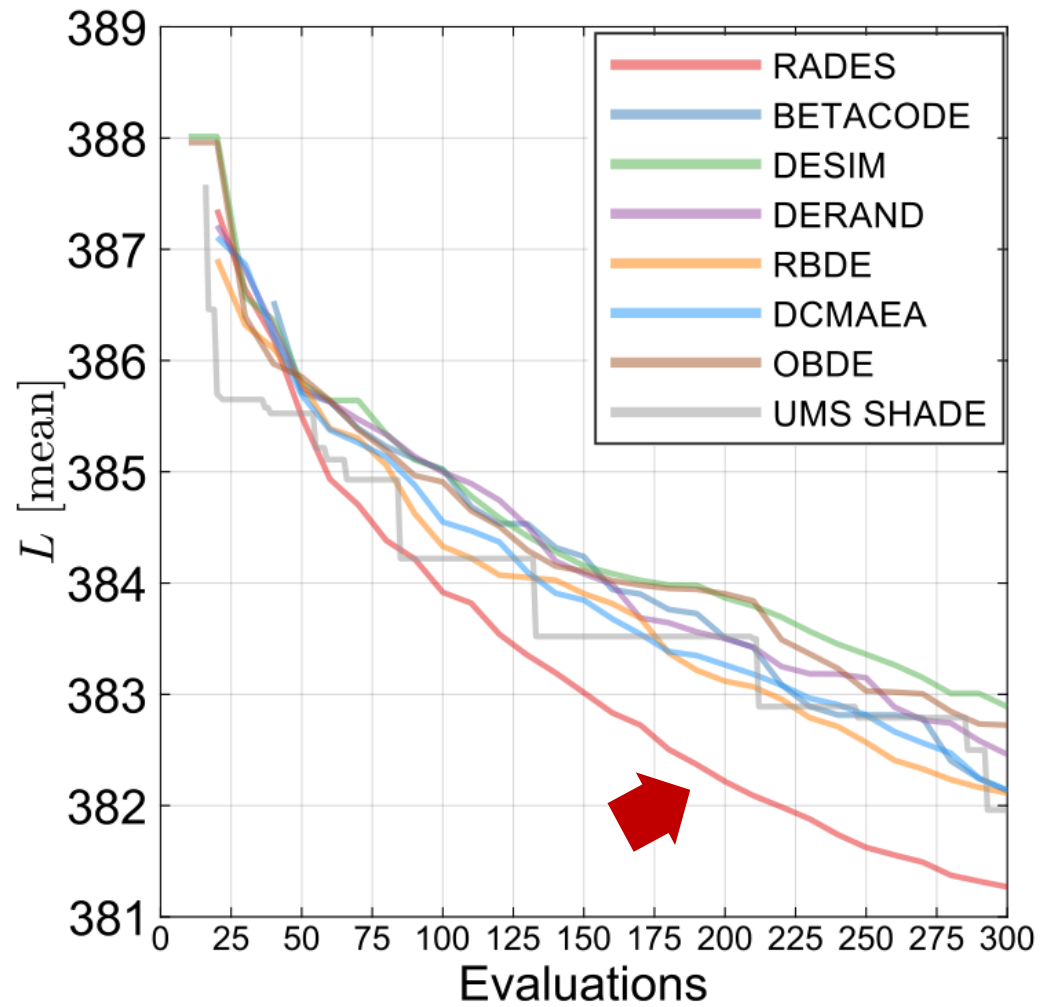
Number of cases of **underperformance**



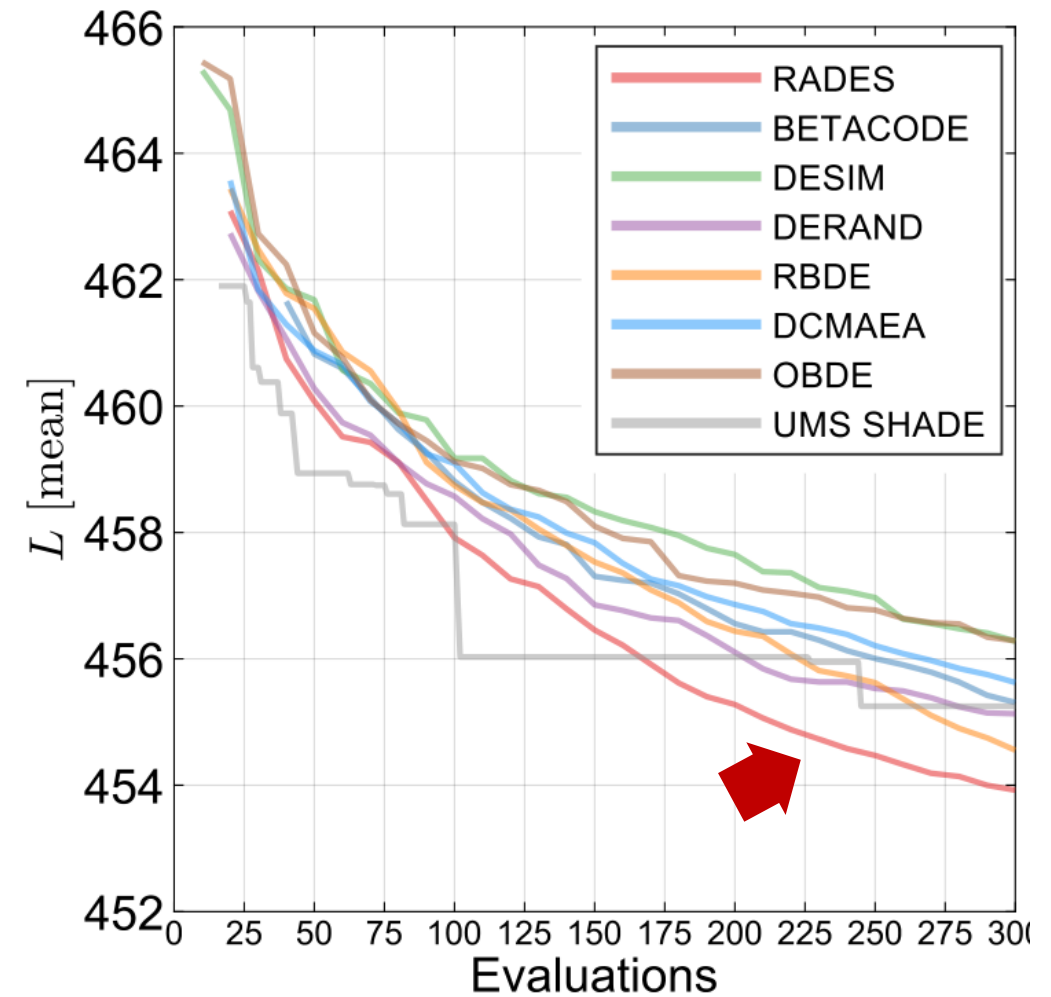
RADES outperforms or performs equally to other baselines

Optimization Convergence

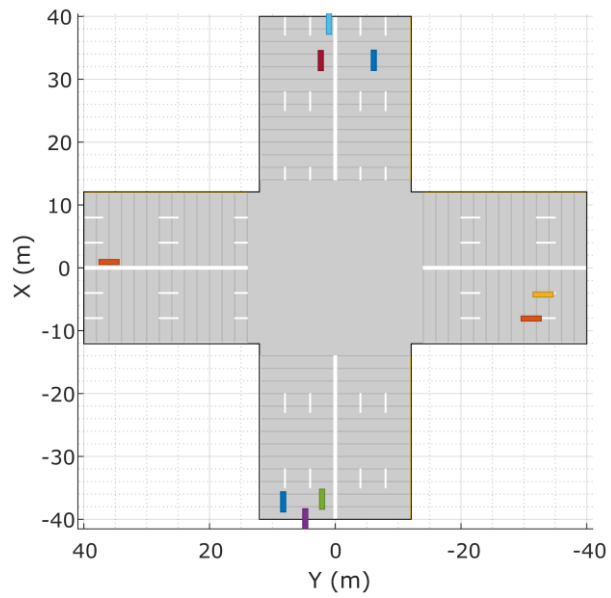
Example 1



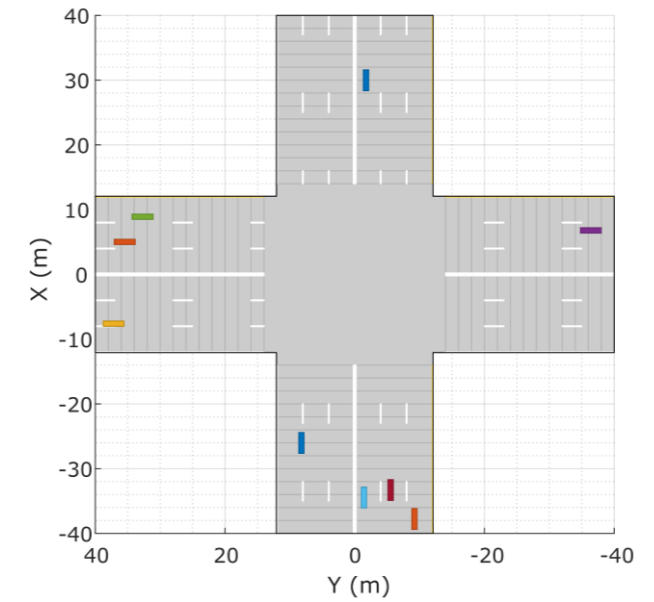
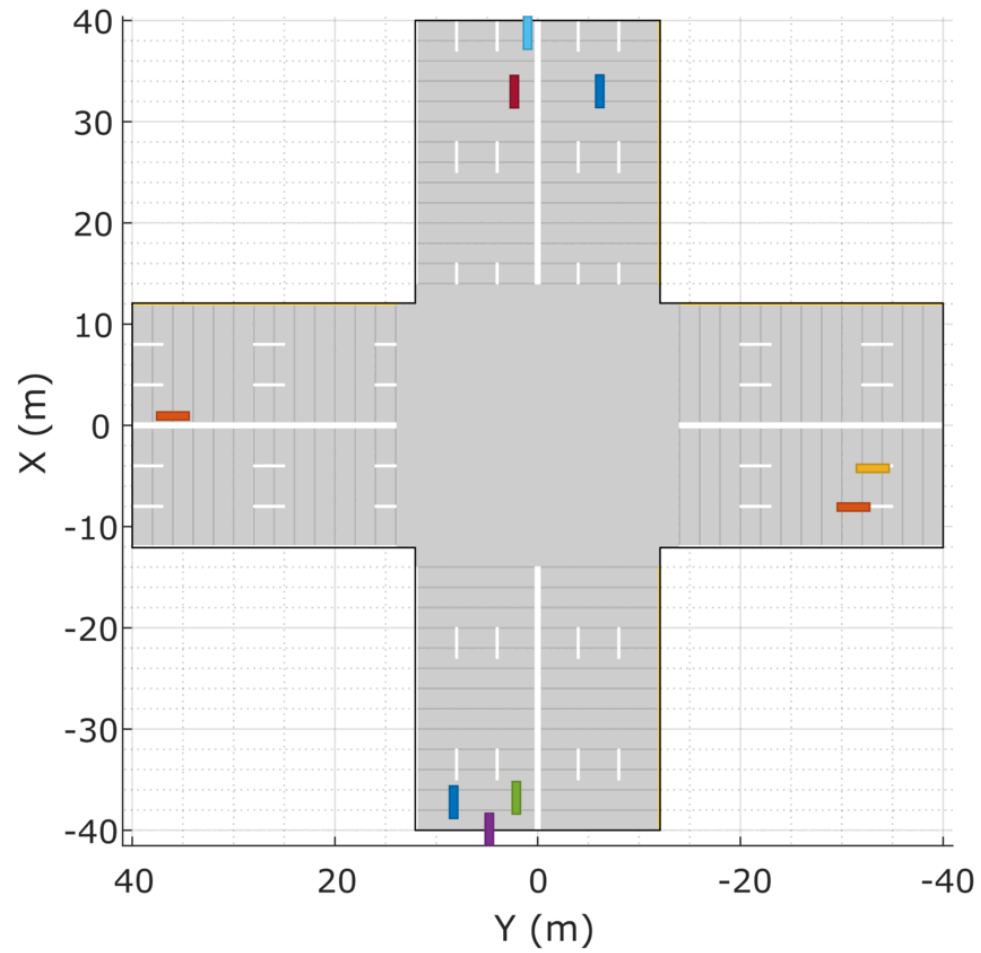
Example 2



Example



Origin



Destination

Conclusion

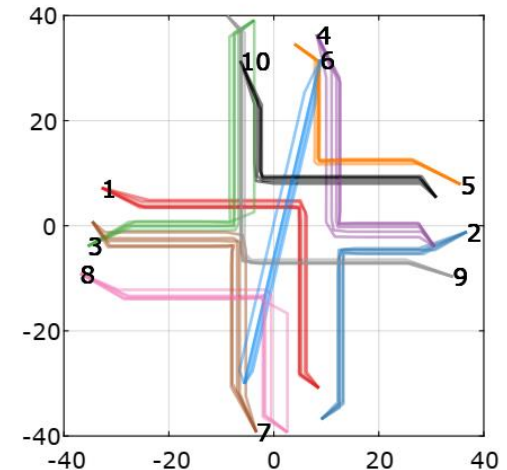
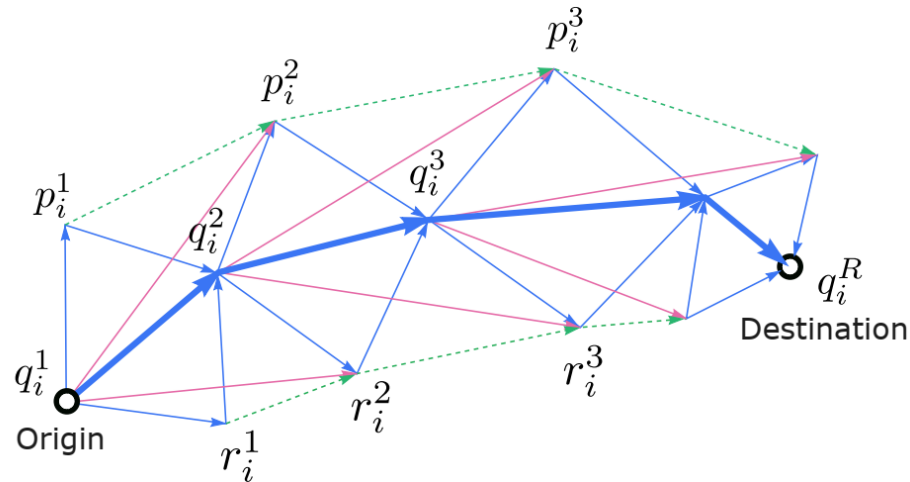
Final Notes

Results

- 🚩 Coordinated trajectory planning for multi-robots
- 🚩 Using lattice roadmaps and gradient-free optimization
- 🚩 Efficient convergence by proposed RADES to composite lattice paths

Future Work

- 🚩 Curvature
- 🚩 Arbitrary Environments



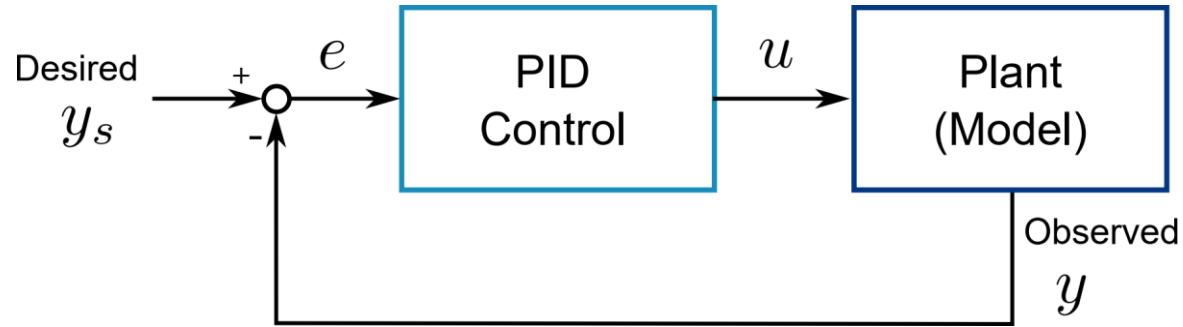
PID Tuning using Differential Evolution with Success-based Particle Adaptations

Victor Parque¹, Alaa Khalifa²

¹Hiroshima University, ²Menoufia University

PID Control

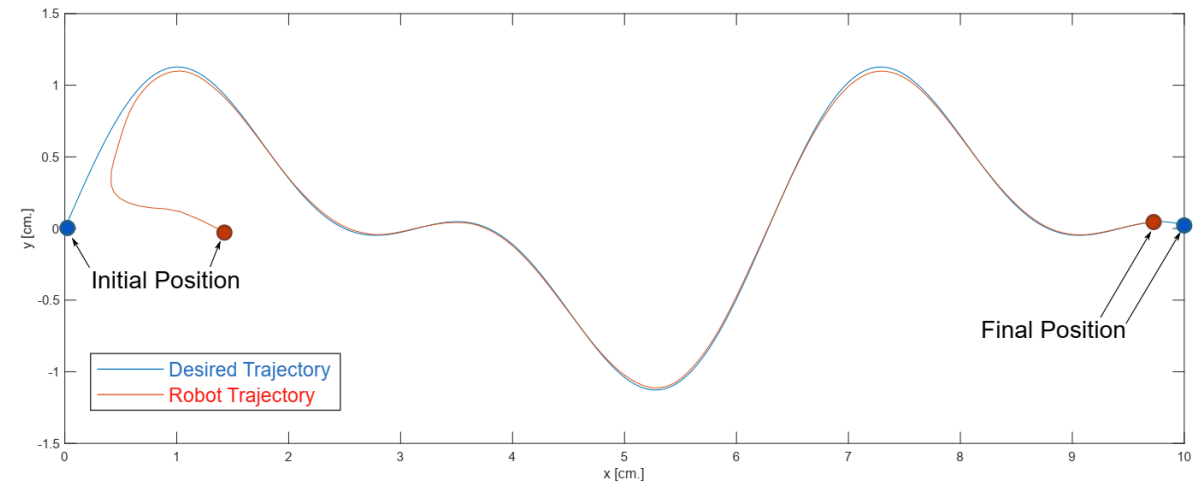
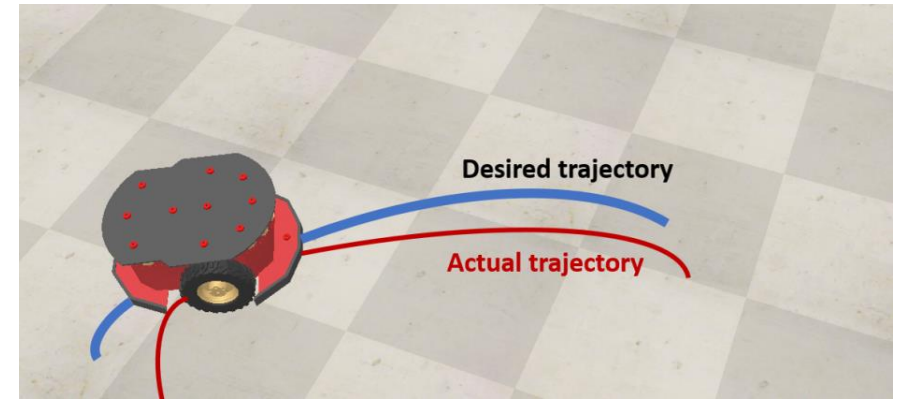
Tracking desired targets



$$u(t) = k_p e(t) + k_i \int_0^t e(\tau) d\tau + k_d \frac{de(t)}{dt}$$

$$e(t) = y_s(t) - y(t) \quad \mathbf{x} = [k_p \ k_i \ k_d]$$

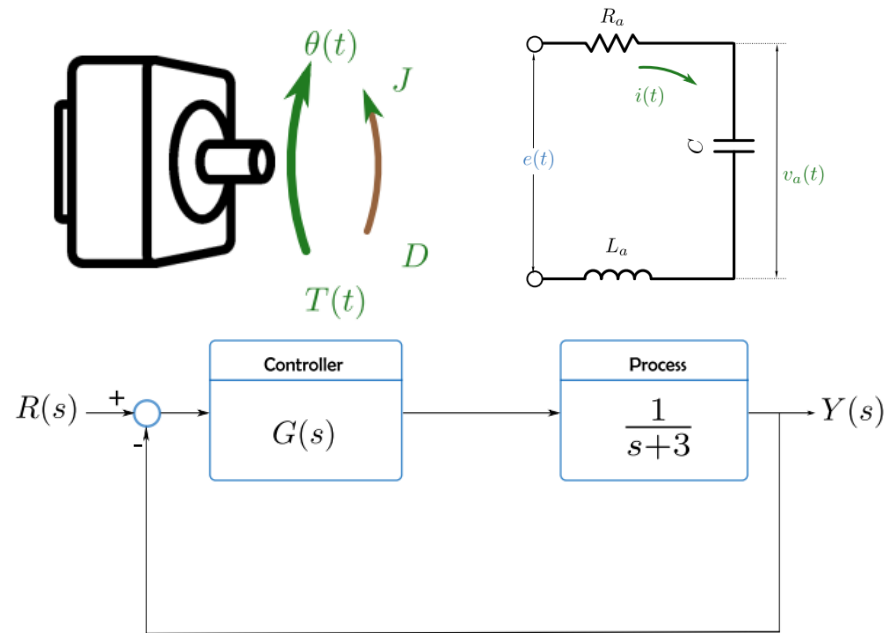
$$\text{IAE}(\mathbf{x}) = \int_0^{T_s} |e(t)| dt \quad \text{ITAE}(\mathbf{x}) = \int_0^{T_s} t |e(t)| dt \quad \text{ITSE}(\mathbf{x}) = \int_0^{T_s} t e(t)^2 dt \quad \text{ISE}(\mathbf{x}) = \int_0^{T_s} e(t)^2 dt$$



PID Control

Tracking desired targets

Dynamic Models

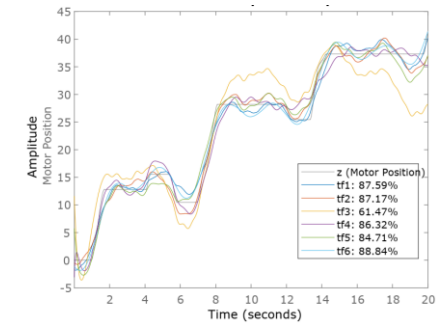
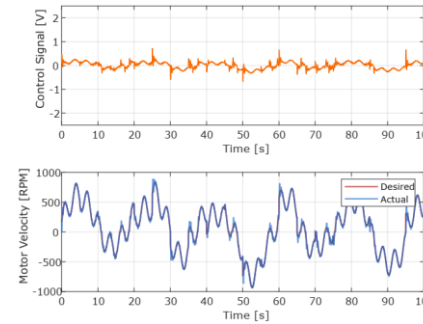
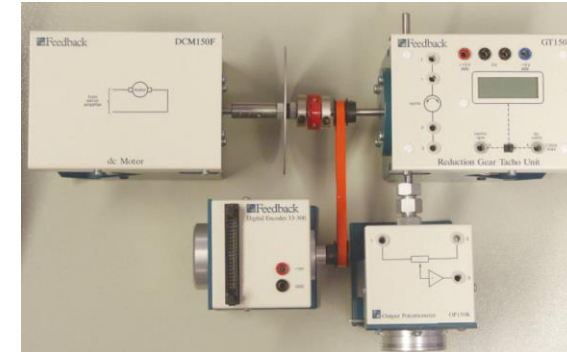


Principled



Sim2Real

Data-driven Models



Practical



Generalizability

How to design algorithms for generalizable PID tuning

PID Control

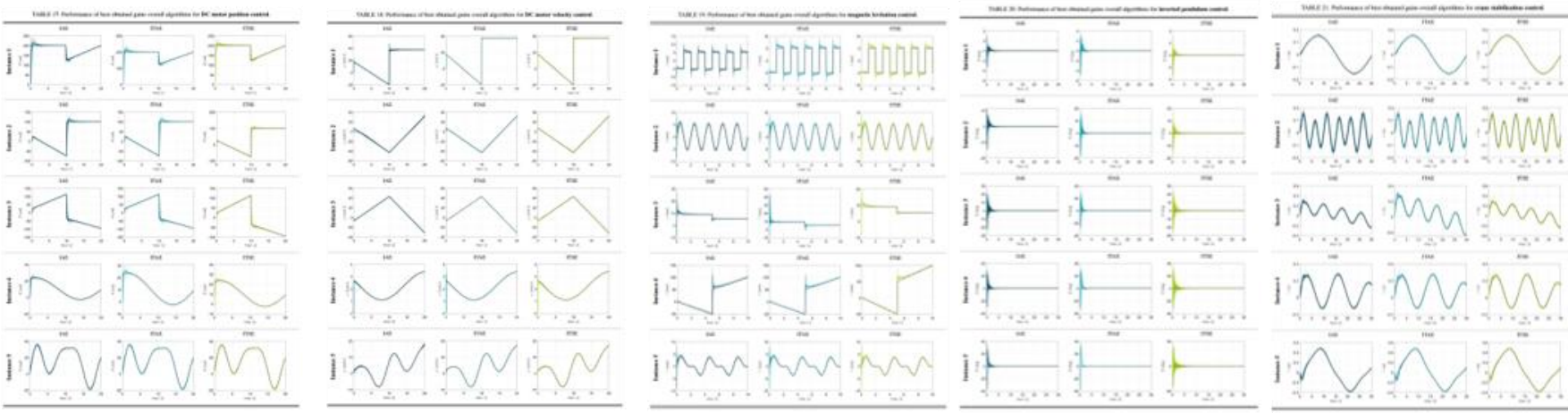
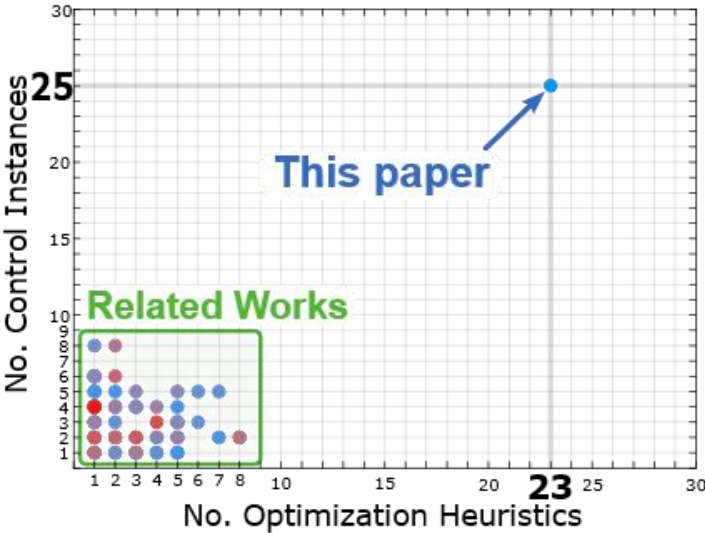
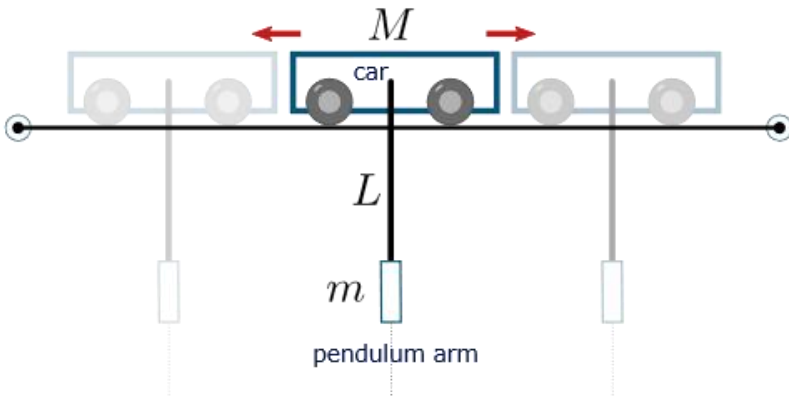
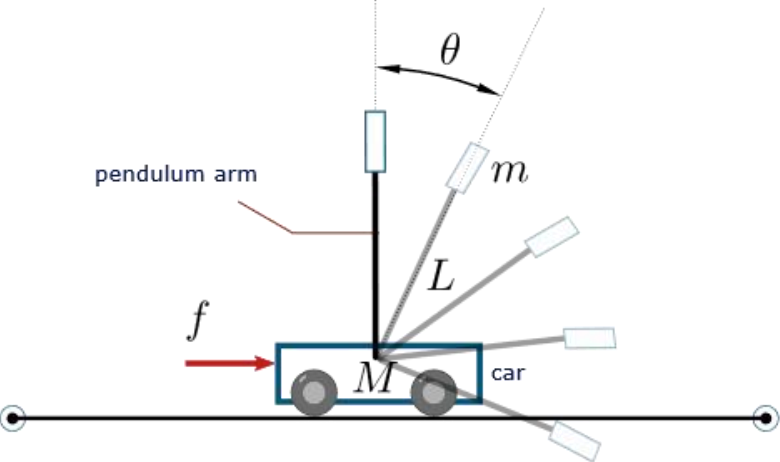
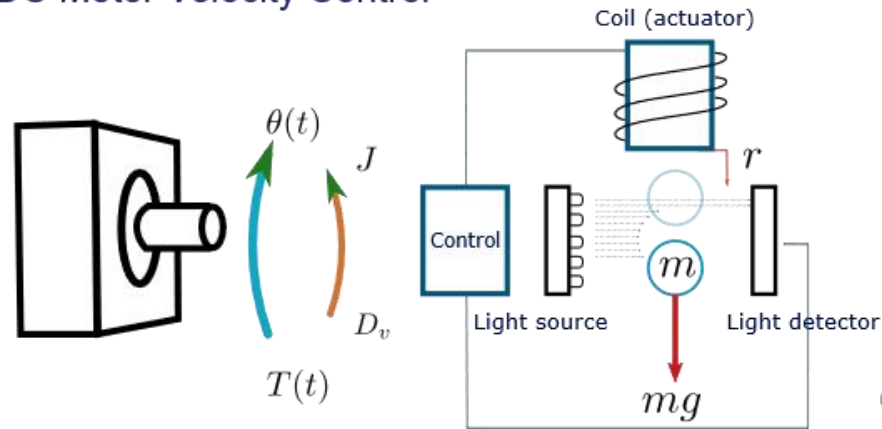
Towards generalizable frameworks

DC Motor Position Control
DC Motor Velocity Control

Magnetic Levitation Control

Inverted Pendulum Control

Crane Stabilization Control



PID Control

DEPA: Differential Evolution with Particle Adaptations

$$\mathbf{x}_{i,g+1} = \begin{cases} \mathbf{u}_{i,g}, & \text{if } f(\mathbf{u}_{i,g}) < f(\mathbf{x}_{i,g}) \\ \mathbf{x}_{i,g}, & \text{otherwise} \end{cases}$$

$$\mathbf{u}_{i,g} = \mathbf{x}_{i,g}^r + \mathbf{v}_{i,g}^*$$

$$\mathbf{v}_{i,g}^* = \omega \mathbf{v}_{i,g} + F_i(\mathbf{x}_{\text{pbest},g} - \mathbf{x}_{i,g}^r)r_1 + G_i(\mathbf{x}_{\text{gbest},g} - \mathbf{x}_{i,g}^r)r_2$$

$$\mathbf{v}_{i,g+1} = \begin{cases} \mathbf{v}_{i,g}^*, & \text{if } f(\mathbf{u}_{i,g}) < f(\mathbf{x}_{i,g}) \\ \mathbf{v}_{i,g}, & \text{otherwise} \end{cases}$$

$$\mathbf{x}_{i,g}^r \in_R \begin{cases} \mathcal{P}, & \text{if } q_i < Q \\ \mathcal{A}, & \text{otherwise} \end{cases}$$

$$\mathcal{A}_g = \begin{cases} \mathcal{P}, & \text{if } g = 0 \\ \mathcal{A}_g \cup \{\mathbf{u}_{i,g}\}, & \text{if } g > 0 \text{ and } f(\mathbf{u}_{i,g}) < f(\mathbf{x}_{i,g}) \end{cases}$$

Algorithm 1: DEPA

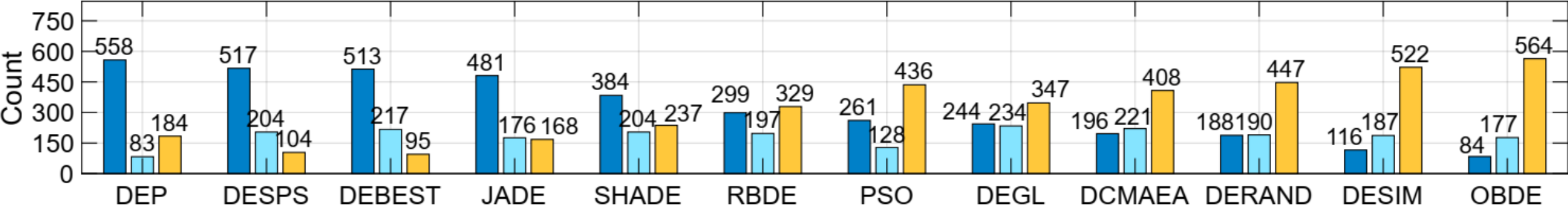
```
1  $FES = 0, g = 0, q_i = 0, k = 0;$ 
2 Generate a set of  $N$  individuals randomly as initial
  population set  $\mathcal{P}$ ;
3 Initialize the archive  $\mathcal{A}$  from the population set  $\mathcal{P}$ ;
4 Initialize the tuples  $\mathcal{M}_F^k$  and  $\mathcal{M}_G^k$ ;
5  $FES = FES + N$ ;
6 while  $FES \leq MaxFES$  do
7    $g = g + 1$ ;
8    $S_F = \{\}, S_G = \{\}$ ;
9   for  $i = 1$  to  $N$  do
10    Sample  $a_i \sim U[1, h], b_i \sim U[1, h]$ ;
11    Generate  $F_i$  and  $G_i$  using (14)-(15);
12  end
13 Find out the best individual  $\mathbf{x}_{\text{gbest},g}$  overall  $\mathcal{P}$ ;
14 for  $i = 1$  to  $N$  do
15   Update the  $i$ -th best individual  $\mathbf{x}_{\text{pbest},g}$ ;
16   Generate the trial vector  $\mathbf{u}_{i,g}$  using (9)-(12);
17   if  $f(\mathbf{u}_{i,g}) < f(\mathbf{x}_{i,g})$  then
18      $\mathbf{x}_{i,g+1} = \mathbf{u}_{i,g}, \mathbf{v}_{i,g+1} = \mathbf{v}_{i,g}^*$ ;
19      $\mathbf{u}_{i,g} \rightarrow \mathcal{A}$ ;
20     Delete an element from  $\mathcal{A}$  if  $|\mathcal{A}| > \lambda|\mathcal{P}|$ ;
21      $F_i \rightarrow S_F, G_i \rightarrow S_G$ ;
22      $q_i = 0$ ;
23   else
24      $\mathbf{x}_{i,g+1} = \mathbf{x}_{i,g}$ ;
25      $\mathbf{v}_{i,g+1} = \mathbf{v}_{i,g}$ ;
26      $q_i = q_i + 1$ ;
27   end
28    $FES = FES + 1$ ;
29 end
30 if  $S_F \neq \{\} \wedge S_G \neq \{\}$  then
31    $k = k + 1$ ;
32   Update  $\mathcal{M}_F^k$  and  $\mathcal{M}_G^k$  using (16) and (17);
33   Set  $k = 1$  if  $k > h$ ;
34 end
35 end
```

PID Control

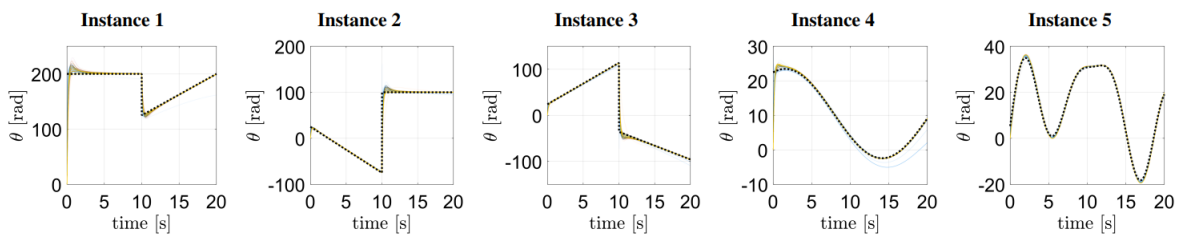
DEPA: Differential Evolution with Particle Adaptations

Overall Comparison

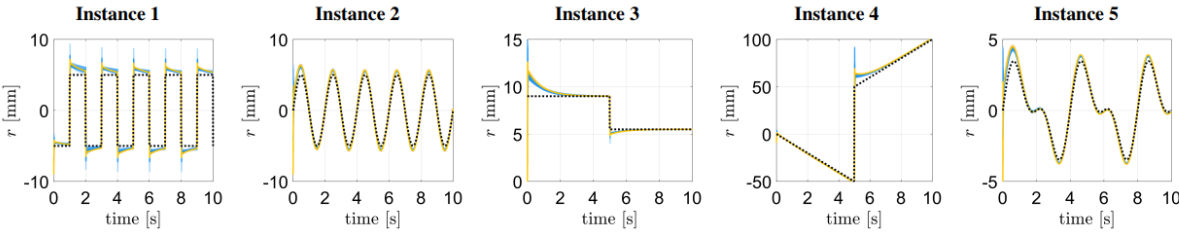
Outperformance cases Equal performance cases Underperformance cases



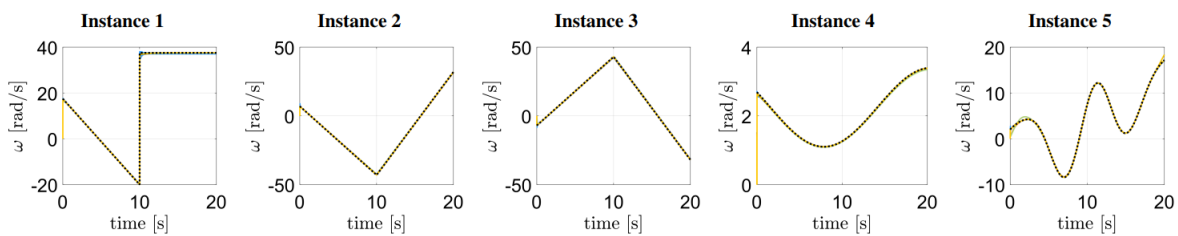
DC Motor Position



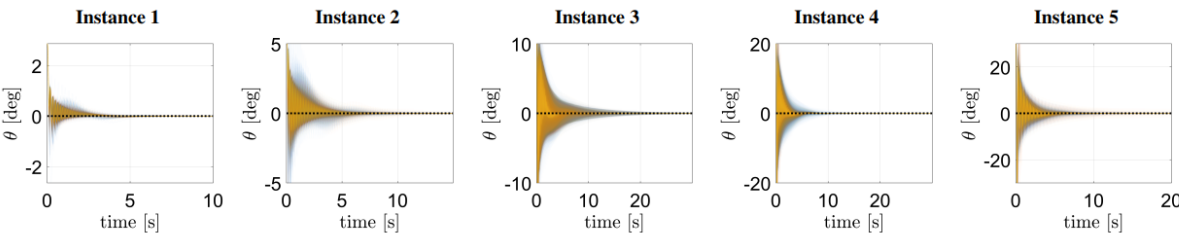
Magnetic Levitation



DC Motor Velocity

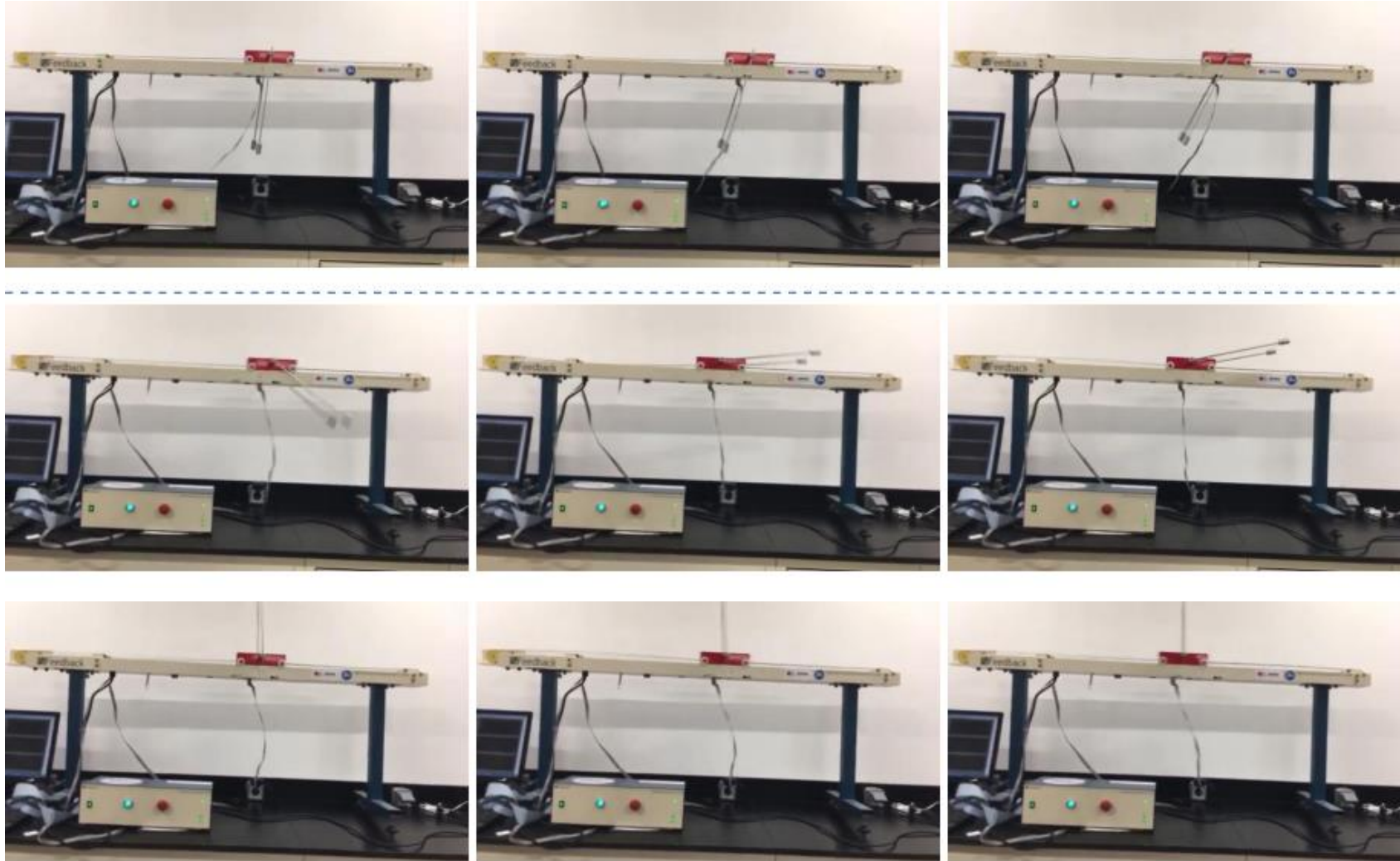


Inverted Pendulum

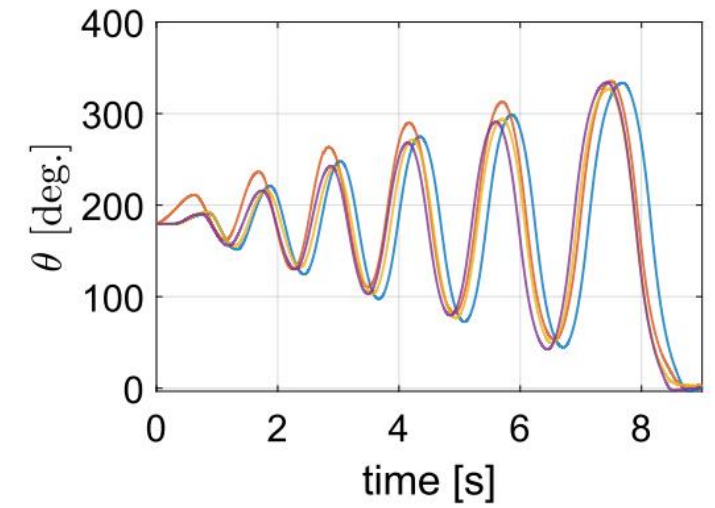


PID Control

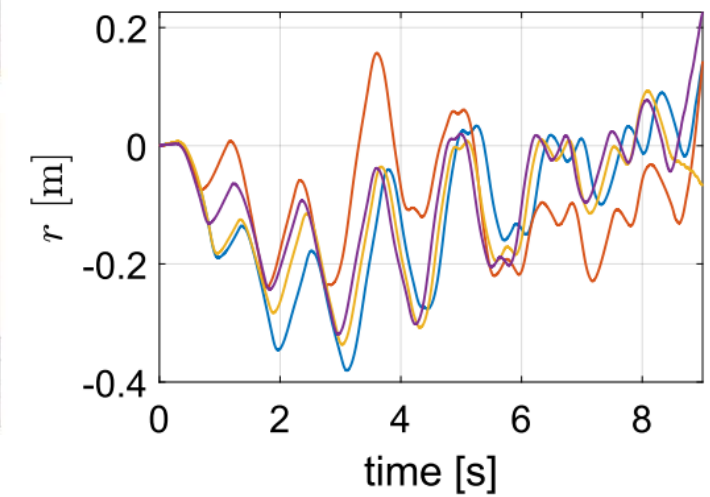
Inverted Pendulum



Pendulum angle

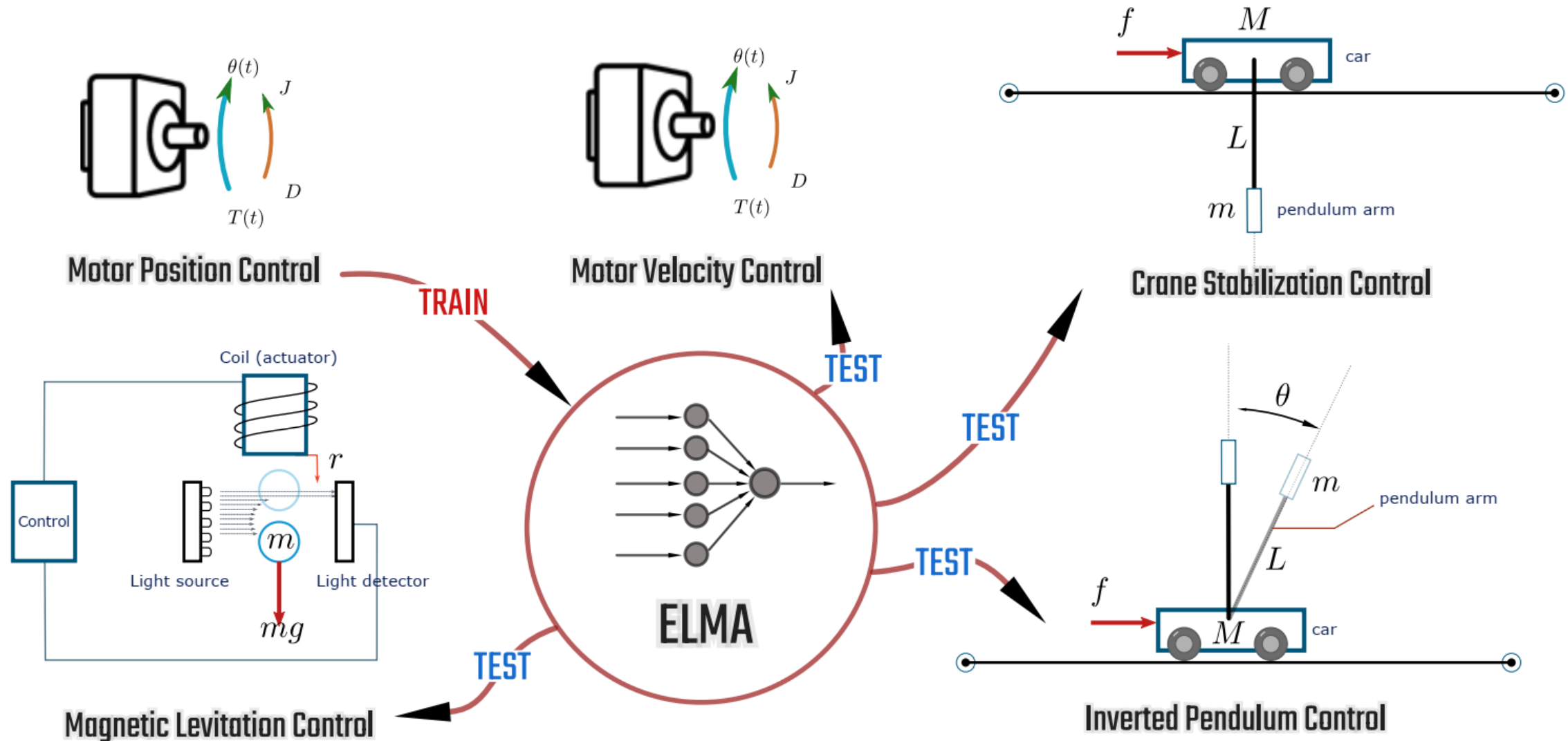


Car position



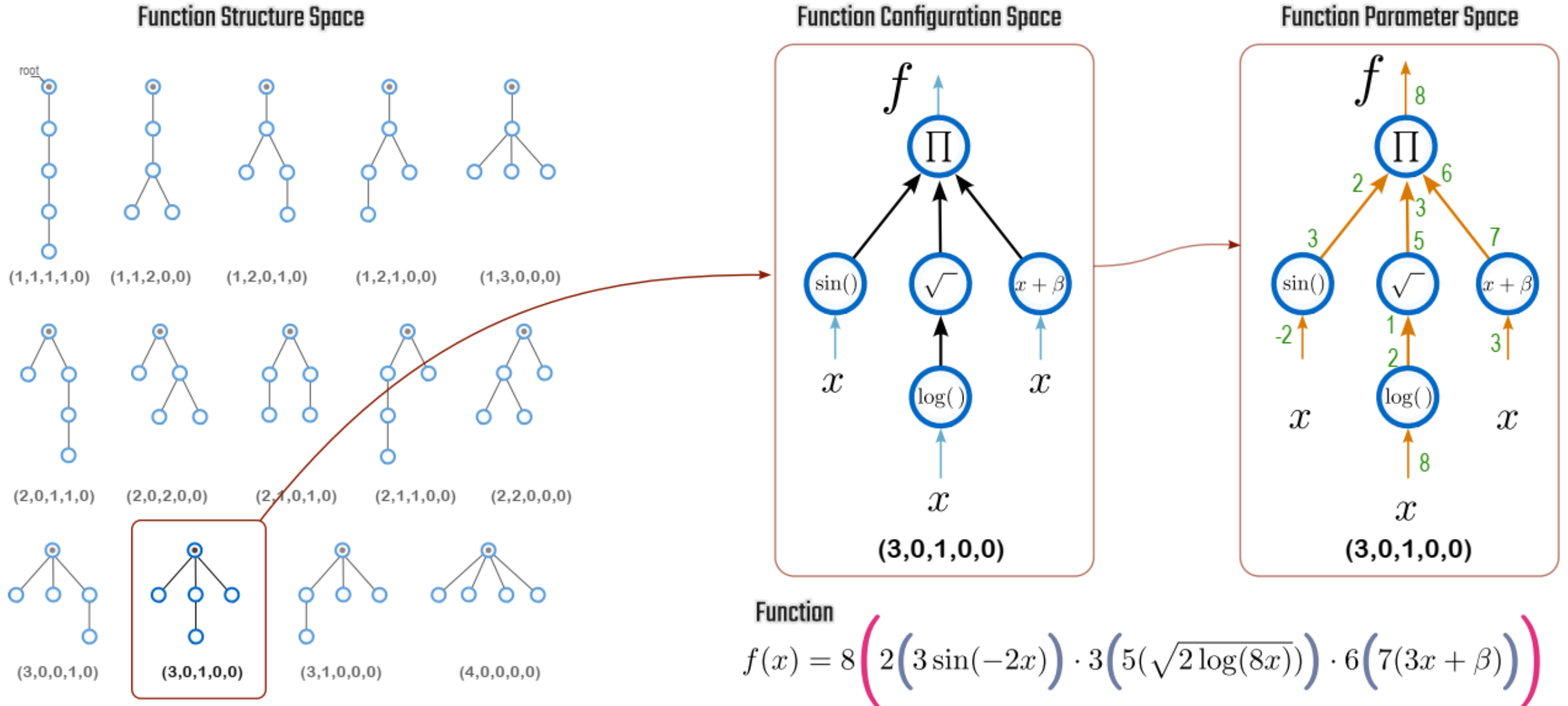
Learning Generalizable Controllers

ELMA: Extreme Learning Machine with Learnable Activation Functions



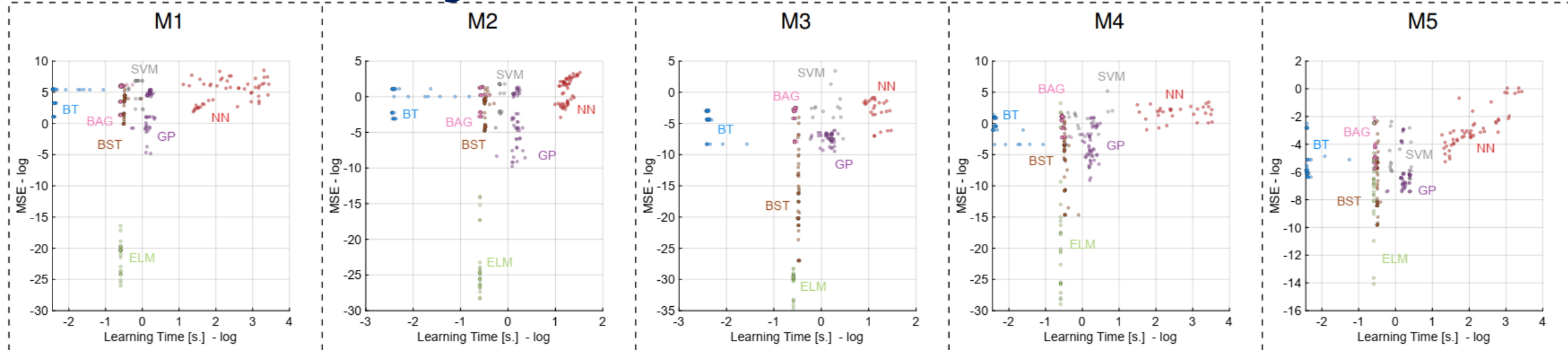
Learning Generalizable Controllers

ELMA: Extreme Learning Machine with Learnable Activation Functions

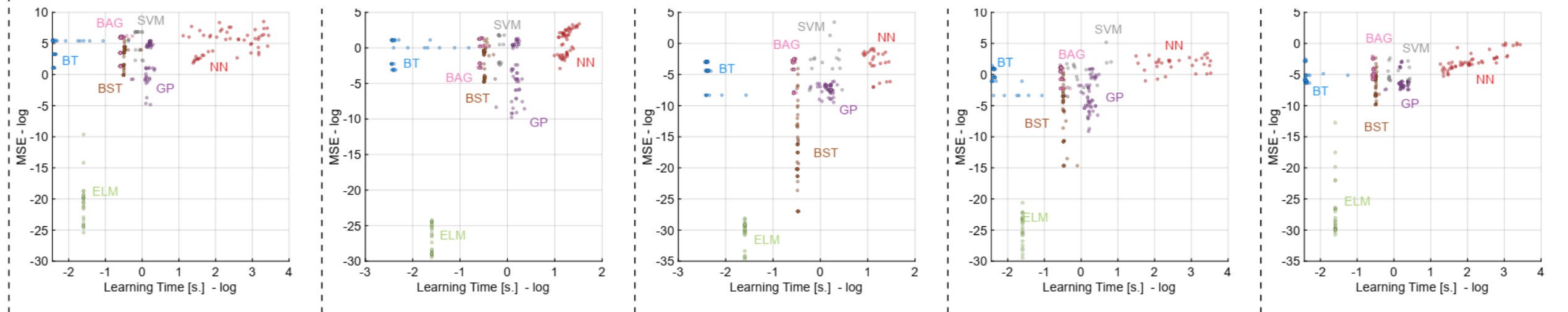


Learning Generalizable Controllers

ELMA: Extreme Learning Machine with Learnable Activation Functions



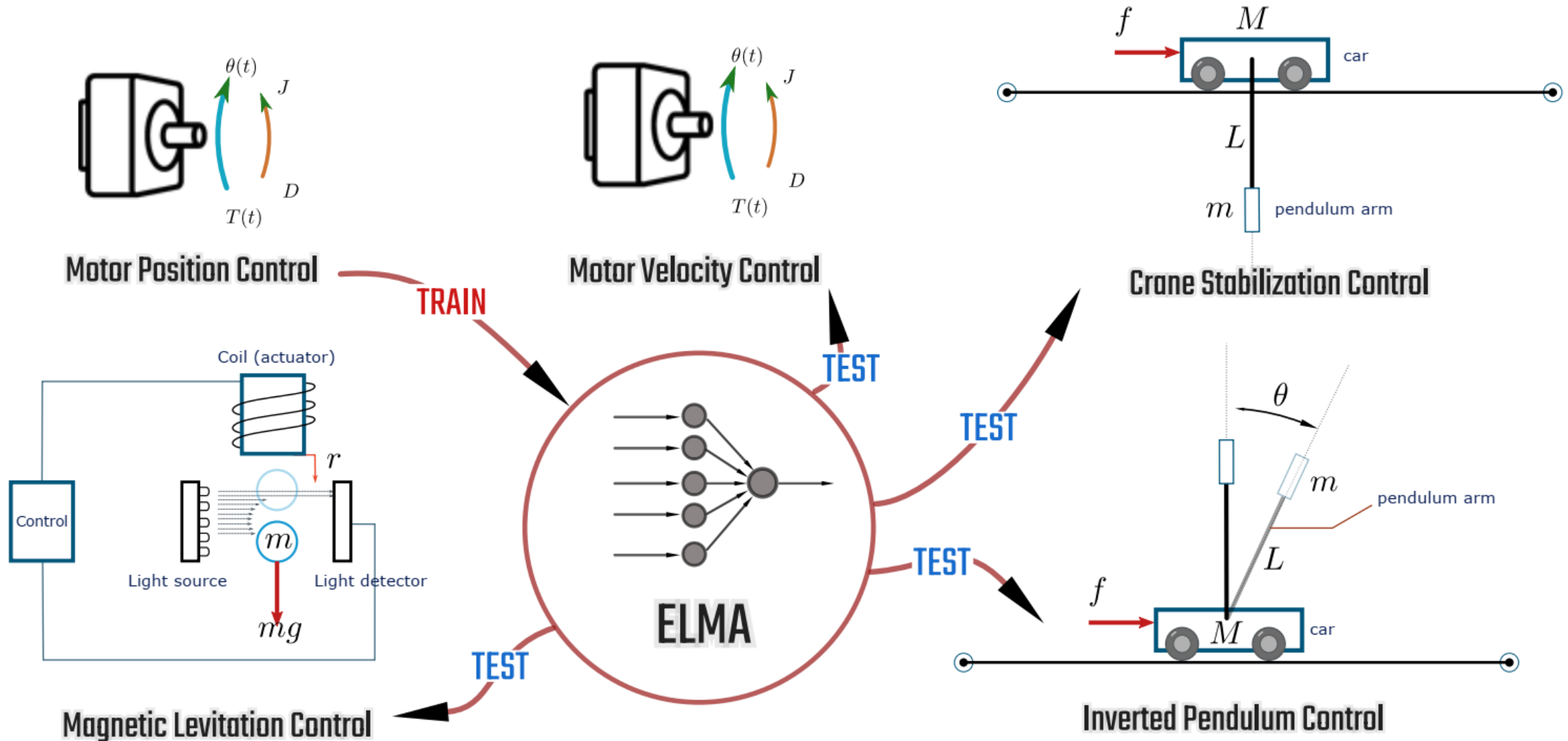
Performance of ELMA when activation functions are learned in M1: Motor Position Control.



Performance of ELMA when activation functions are learned in M5: Magnetic Levitation Control.

Learning Generalizable Controllers

ELMA: Extreme Learning Machine with Learnable Activation Functions



Thank you



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